QoS-Constrained Multi-path Routing for High-End Network Applications

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1 Introduction

2 Problem Formulation and the Proposed Algorithms

3 Numerical Results

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Motivation

- High-end applications have become dependent on global networks, with supercomputing and data-storage facilities widely distributed.
- It is known that multi-path routing can provide more aggregate bandwidth.
- Multiple paths may present differences in the end-to-end delay of each path, which causes jitter at the destination (Differential Delay).
- High speed memory is extremely expensive, and therefore cannot be over-provisioned.
An Example of Data Transmission over Multiple Paths

Request of 40 units from S to D

- Four possible paths $P_1, P_2, P_3$, and $P_4$ with delay $d$ and capacity $b$.
- Single shortest path: $P_2$
  Delay $40/b_2 + d_2 = 12$.
- Max the achievable bandwidth: $P_1$ and $P_3$
  Delay $\max\{20/b_1 + d_1, 20/b_3 + d_3\} = 11$
  Memory $(d_1 - d_3) \cdot b_3 = 18$.
- Min the differential delay: $P_1$ and $P_4$
  Delay $\max\{20/b_1 + d_1, 20/b_4 + d_4\} = 16$
  Memory $(d_1 - d_4) \cdot b_4 = 2$. 

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Given a connection request $r$ with source $s(r)$ and destination $d(r)$, optimize the achievable bandwidth for the requested connection while minimizing the cost incurred by the memory required at the destination due to differential delay among the multiple paths.
Our solution steps

1. Define the first $N$ shortest widest paths in the network.

2. Select a subset of paths that maximize the achievable bandwidth while taking into consideration the buffer (memory) cost.
Algorithm 1: Multipath path computation algorithm

Input: $G(V, E), (s, d), N$

1. Initialize an Empty Array of Paths $pathSet$;
2. For all $v_i \in V$ s.t. there exists a link $e_j \in E$ from $s$ to $v_i$, create a path from $s$ to $v_i$ and insert in $pathSet$;
3. Sort $pathSet$ in decreasing order of bandwidth;
4. While $count < N$ do
   1. Count = 0;
   2. For $i = 0$ to $pathSet$.length do
      1. If ($pathSet[i].destination == d$) then
         1. Increase count by 1;
         1. If($count == N$) break;
      2. Else
         1. $path = pathSet[i]$;
         1. Remove $pathSet[i]$ from $pathSet$;
         1. For each $e_j \in E$ attached to $path.destination$ do
            1. Let the vertices at the end of $e_j$ be $v_k$ and $path.endVertex$;
            1. If ($v_k \notin path.vertices$) then
               1. Create a new path by extending $path$ with $e_j$; Insert new path in $pathSet$ using insertion sort;
            1. End
         1. End
      1. End
   1. End
   2. If (no more paths can be extended) then
      1. Break;
   1. End
End
Maximize \[ \sum_{P \in (P)} C_F \cdot t_P - C_M \cdot M_r \]

Subject to:

\[ \forall e \in E : x_e = \sum_{P \in \mathcal{P} \land e \in P} t_P \]  \hspace{1cm} (1)

\[ \forall e \in E : x_e \leq c_e \]  \hspace{1cm} (2)

\[ M(r) = \sum_{P \in \mathcal{P}} t_P (d_{\tilde{P}} - d_P) \]  \hspace{1cm} (3)

\[ \forall P \in \mathcal{P} : t_P = 0 \text{ if } d_P > d_{\tilde{P}} \]  \hspace{1cm} (4)

\[ \forall P \in \mathcal{P} : t_P \geq 0 \text{ if } d_P \leq d_{\tilde{P}} \]  \hspace{1cm} (5)

\[ t_P > 0 \]  \hspace{1cm} (6)

\[ \sum_{P \in (P)} t_P \geq B_{\text{min}} \]  \hspace{1cm} (7)

\[ M_r \leq M_d \]  \hspace{1cm} (8)

\[ t_P - \text{ an integer variable for each path } P \in \mathcal{P} \]

\[ x_e - \text{ an integer variable for each link } e \in E \]

\[ \tilde{P} - \text{ The path in the solution set with the highest delay.} \]

\[ B_{\text{min}} = \frac{F}{D_{\text{max}}} \]

\[ F: \text{ total size of the data.} \]

\[ D_{\text{max}}: \text{ maximum delay.} \]
Multi-homing networks with three multi-path multi-domain routing schemes:

- multi-domain routing with full visibility;
- multi-domain routing with partial visibility;
- multi-path routing in a single preferred domain.
Networks Considered (NSFNet and Germany17)
Achievable Bandwidth vs Network Load

- wildest shortest single path
- CF=1, CM=1
- CF=1, CM=2
- CF=1, CM=5
- CF=1, CM=10

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Achievable Bandwidth of Different Algorithms (Germany17)

Achievable Bandwidth Comparison (Network Load=130 Erlang)

- Multipath Routing
- Widest Shortest Single Path

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Achievable Bandwidth of Different Schemes With Identical Network Loading In Both Domains (NSFNet and Germany17)

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Achievable Bandwidth Of Different Schemes With Skewed Network Loading. The load in the Germany17 is kept constant while the load in the NSFNet is varied.
Achievable Bandwidth of Different Schemes vs Delay Scaling Factor. The link delay in the NFSNet is scaled while that of the Germany17 is kept constant.
Achievable Bandwidth Of Different Schemes vs Memory Cost (NSFNet and Germany17)
Proposed solutions

- Multi-path routing to maximize bandwidth between a pair of nodes for applications requiring high data transfer rates.

- Multi-path computation algorithm which calculates the first $N$ shortest-widest paths.

- ILP formulation which can maximize the achievable bandwidth while minimizing the memory cost.
Results

- Multi-path routing can achieve significantly higher bandwidth as compared to traditional single path routing.

- multi-domain multi-path routing schemes can achieve significant increase in bandwidth even with partial visibility in a multi-homing environment.
Future Work

- Decrease the complexity of multipath calculation.
- Develop heuristic algorithms to find near-optimal solutions.
Thank you!
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