

Name:

Student ID:

**Question 1** {5 marks}

(i) Cite the phases that are present and the phase compositions for the following alloys:

2.12 kg Zn and 1.88 kg Cu at 500°C

(ii) Determine the relative amounts (in terms of mass fractions) of the phases for this alloy at 500°C.

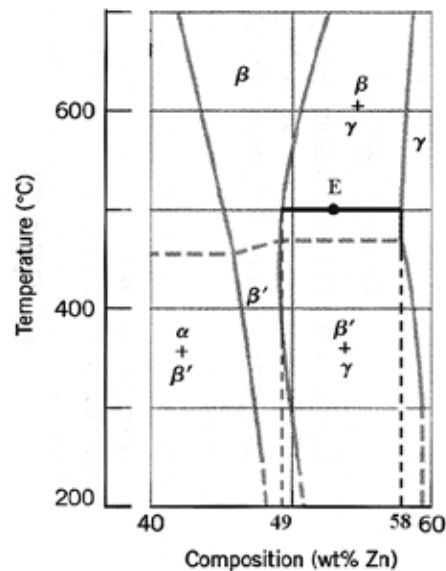
**Solution:**

For an alloy composed of 2.12 kg Zn and 1.88 kg Cu and at 500°C, we must first determine the Zn and Cu concentrations, as

$$C_{\text{Zn}} = \frac{2.12 \text{ kg}}{2.12 \text{ kg} + 1.88 \text{ kg}} \cdot 100 = 53 \text{ wt\%}$$

$$C_{\text{Cu}} = \frac{1.88 \text{ kg}}{2.12 \text{ kg} + 1.88 \text{ kg}} \cdot 100 = 47 \text{ wt\%}$$

That portion of the Cu-Zn phase diagram (Figure 9.19) that pertains to this problem is shown below; the point labeled "E" represents the 53 wt% Zn-47 wt% Cu composition at 500°C.



(i) Point E lies within the  $\beta + \gamma$  phase field. A tie line has been constructed at 500°C; its intersection with the  $\beta/\beta + \gamma$  phase boundary is at 49 wt% Zn, which corresponds to the composition of the  $\beta$  phase. Similarly, the tie-line intersection with the  $\beta + \gamma/\gamma$  phase boundary

occurs at 58 wt% Zn, which is the composition of the  $\gamma$  phase. Thus, the phase compositions are as follows:

$$C_{\beta} = 49 \text{ wt\% Zn-51 wt\% Cu}$$

$$C_{\gamma} = 58 \text{ wt\% Zn-42 wt\% Cu}$$

(ii) Inasmuch as the composition of the alloy  $C_0 = 53 \text{ wt\% Zn}$  and application of lever rule leads to

$$W_{\beta} = \frac{C_{\gamma} - C_0}{C_{\gamma} - C_{\beta}} = \frac{58 - 53}{58 - 49} = 0.56$$

$$W_{\gamma} = \frac{C_0 - C_{\beta}}{C_{\gamma} - C_{\beta}} = \frac{53 - 49}{58 - 49} = 0.44$$

### Question 2 {5 Marks}

Consider 2.5 kg of austenite containing 0.65 wt% C, cooled to just below 727°C.

- How many kilograms each of total ferrite and cementite form?
- How many kilograms each of pearlite and the proeutectoid phase form?

### Solution:

- For this portion of the problem, we are asked to determine how much total ferrite and cementite form. For ferrite, application of lever rule yields

$$W_{\alpha} = (C_{\text{Fe}_3\text{C}} - C_0) / (C_{\text{Fe}_3\text{C}} - C_{\alpha}) = (6.70 - 0.65) / (6.70 - 0.022) = 0.91$$

which corresponds to  $(0.91)(2.5 \text{ kg}) = 2.275 \text{ kg}$  of total ferrite.

Similarly, for total cementite,

$$W_{\text{Fe}_3\text{C}} = (C_0 - C_{\alpha}) / (C_{\text{Fe}_3\text{C}} - C_{\alpha}) = (0.65 - 0.022) / (6.70 - 0.022) = 0.09$$

Which corresponds to  $(0.09)(2.5 \text{ kg}) = 0.225 \text{ kg}$  of total cementite.

- Now consider the amounts of pearlite and proeutectoid ferrite. Using Equation 9.20

$$W_{\text{p}} = (C_0' - 0.022) / 0.74 = (0.65 - 0.022) / 0.74 = 0.85$$

This corresponds to  $(0.85)(2.5 \text{ kg}) = 2.12 \text{ kg}$  of pearlite. Also, from Equation 9.21,

$$W_{\alpha'} = (0.76 - 0.65) / 0.74 = 0.15$$

Or, there are  $(0.15)(2.5 \text{ kg}) = 0.38 \text{ kg}$  of proeutectoid ferrite.