



Composite Materials

ISSUES TO ADDRESS...

- What are the classes and types of composites?
- Why are composites used instead of metals, ceramics, or polymers?
- How do we estimate composite stiffness & strength?

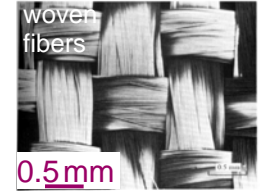


Composites Classification

- **Composites:** Multiphase material with significant proportions of each phase.

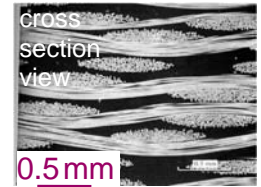
Matrix:

- The continuous phase
- Purpose is to:
 - transfer stress to other phases
 - protect phases from environment
- Classification: MMC, CMC, PMC



Dispersed phase:

- Purpose: enhance matrix properties.
 - MMC: increase σ_y , TS, creep resist.
 - CMC: increase Kc
 - PMC: increase E, σ_y , TS, creep resist.
- Classification: Particle, fiber, structural



Particulates Composites

Particle-reinforced Fiber-reinforced Structural

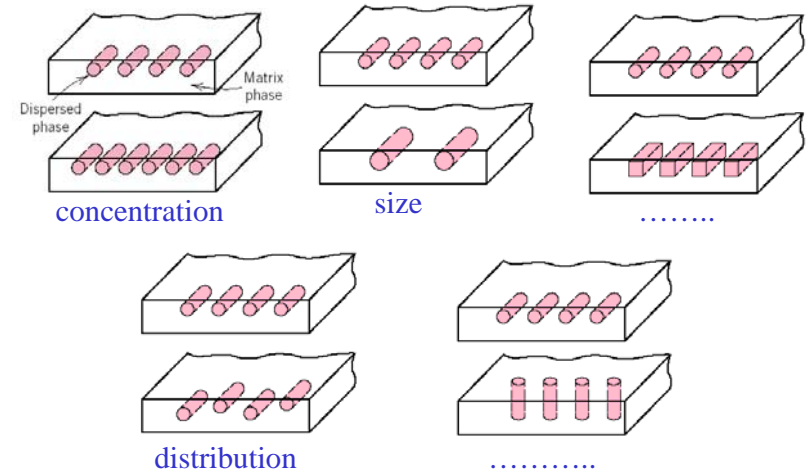
Examples:

- ✓ Spheroidite steel
 - matrix: Ferrite (α) ductile
 - particles: cementite (Fe_3C) brittle
 - 60 μm
- ✓ WC/Co cemented carbide
 - matrix: cobalt ductile
 - particles: WC brittle, hard
 - $V_m: 10-15 vol\%$
 - 600 μm
- ✓ Automobile tires
 - matrix: rubber compliant
 - particles: C stiffer
 - 0.75 mm



Particulates Composites

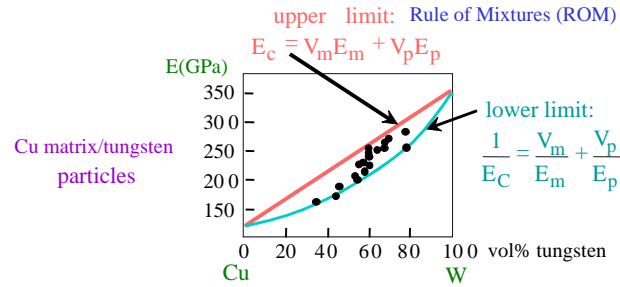
Properties of particulates composites depend on:





Particulates Composites

- Elastic modulus of composites, E_c :
- two approaches:



- Application to other properties:
 - Electrical conductivity, σ_e : Replace E by σ_e .
 - Thermal conductivity, k: Replace E by k.

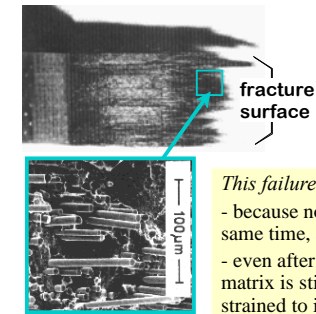
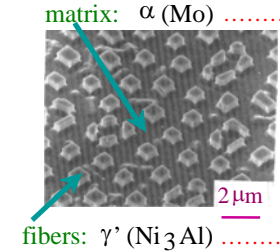


Fiber Composites

Particle-reinforced fiber-reinforced Structural

(1) Aligned Continuous fibers

- Examples:
 - ✓ Metal: γ (Ni₃Al)- α (Mo)
 - ✓ Glass reinforced with SiC fibers formed by glass slurry
 $E_{\text{glass}} = 76\text{GPa}$; $E_{\text{SiC}} = 400\text{GPa}$.



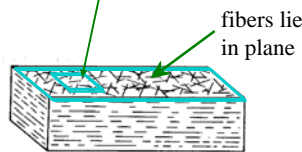
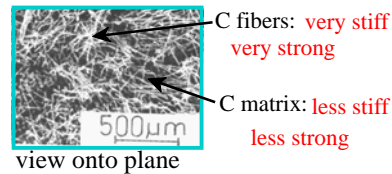
This failure is not catastrophic
 - because not all fibers fail at the same time, and
 - even after fibers fail the matrix is still intact until it is strained to its fracture point.



Fiber Composites

(2) Discontinuous, random 2D fibers

- Example: Carbon-Carbon
 - uses: disk brakes, gas turbine exhaust flaps, nose cones.



- Other variations:
 - ✓ Discontinuous, random 3D
 - ✓ Discontinuous, 1D



Fiber Composites

- Critical fiber length for effective stiffening & strengthening:

Fiber strength in tension

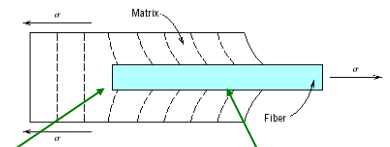
$$l_c = \frac{\sigma_f d}{2\tau_c}$$

Labels: $\sigma_f d$ is Fiber strength in tension, d is Fiber diameter, $2\tau_c$ is shear strength of fiber-matrix interface.

For glass and carbon composites, l_c is often around 1mm (20 - 150 x d_f)

Fibers need to be long enough to carry load.

How does fiber strengthening work?
 Transfer load from matrix to strong/stiff fiber. Requires a good

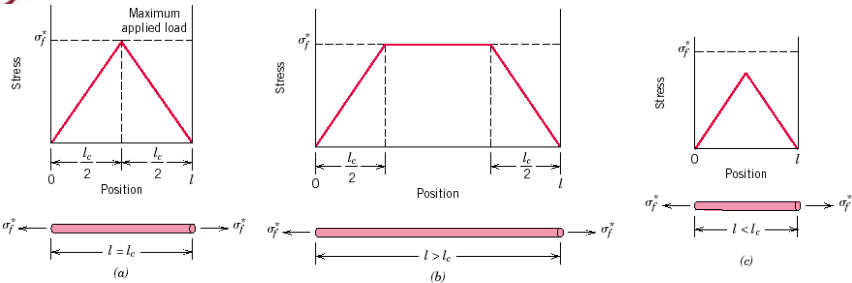


No load is transferred at fiber ends

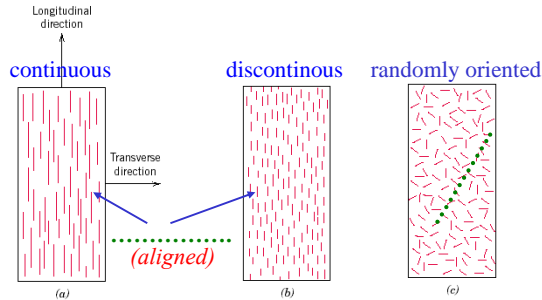
Load is transferred along fiber sides



Fiber Composites



When:
 $l > 15 l_c$ "continuous" fibers
 $l \sim 10 l_c$ "discontinuous" fibers
 $l < l_c$ not acting as fibers (particles).



Rule of Mixtures (RoM)

Volume of composite = Vol. of fibers + Vol. of matrix
Volume fraction of fibers: $V_f = \text{vol. of fibers} / \text{vol. of composite}$
Volume fraction of matrix: $V_m = \text{vol. of matrix} / \text{vol. of composite}$
 $V_f + V_m = 1$ $V_m = (1 - V_f)$

Thus density of composite can be written as:

$$\rho_c = V_f \rho_f + V_m \rho_m \quad \text{or} \quad \rho_c = V_f \rho_f + (1 - V_f) \rho_m$$

Elastic Properties: Longitudinal loading

load carried by composite = loads carried by two phases:

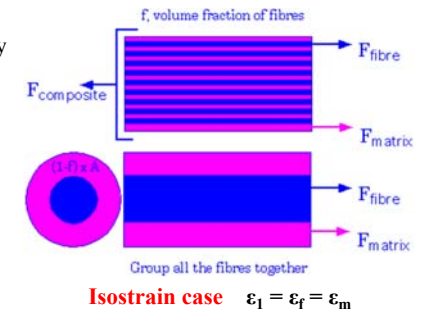
$$F_c = F_m + F_f \quad \text{since} \quad F = \sigma A$$

$$\sigma_c A_c = \sigma_m A_m + \sigma_f A_f \quad \text{Divide by } A_c$$

$$\sigma_c = \sigma_m \frac{A_m}{A_c} + \sigma_f \frac{A_f}{A_c}$$

Area fraction = vol. fraction (if all fibers have the same length)

$$\sigma_c = \sigma_m V_m + \sigma_f V_f$$



Elastic Properties: Longitudinal loading

$$\epsilon_c = \epsilon_m = \epsilon_f$$

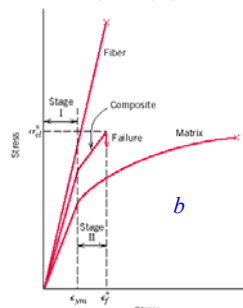
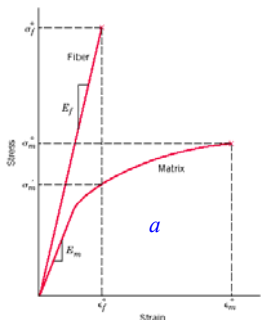
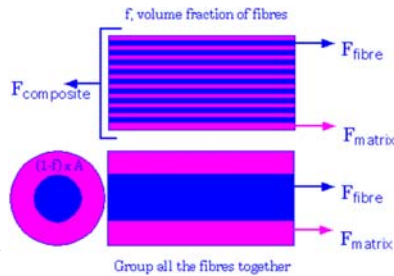
All stretch by same amount

$$\sigma_c = \sigma_m V_m + \sigma_f V_f$$

$$\frac{\sigma_c}{\epsilon_c} = \frac{\sigma_m}{\epsilon_m} V_m + \frac{\sigma_f}{\epsilon_f} V_f$$

$$E_c = E_m V_m + E_f V_f \quad \text{or} \quad E_c = E_m (1 - V_f) + E_f V_f$$

And ratio of loads in fibre and matrix : $\frac{F_f}{F_m} = \frac{E_f V_f}{E_m V_m}$



- (a) brittle fiber and ductile matrix.
- (b) stress-strain curve for an aligned fiber-reinforced composite that is exposed to a uniaxial stress applied in the direction of alignment.



Elastic Properties: Transverse loading

Isostress case $\sigma_c = \sigma_f = \sigma_m$

$$\epsilon_c A_c = \epsilon_m A_m + \epsilon_f A_f \quad \text{From RoM}$$

$$\text{but } \epsilon = \sigma / E$$

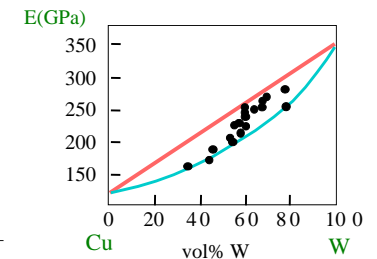
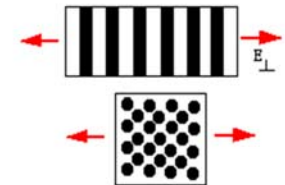
$$\Rightarrow \frac{\sigma}{E_{ct}} = \frac{\sigma}{E_m} V_m + \frac{\sigma}{E_f} V_f \quad \text{where } E_{ct} \text{ is the transverse modulus.}$$

(recall $\sigma_c = \sigma_f = \sigma_m$)

$$\frac{1}{E_{ct}} = \frac{1}{E_m} V_m + \frac{1}{E_f} V_f$$

which can be rearranged to:

$$E_{ct} = \frac{E_m E_f}{V_m E_f + V_f E_m} = \frac{E_m E_f}{(1 - V_f) E_f + V_f E_m}$$

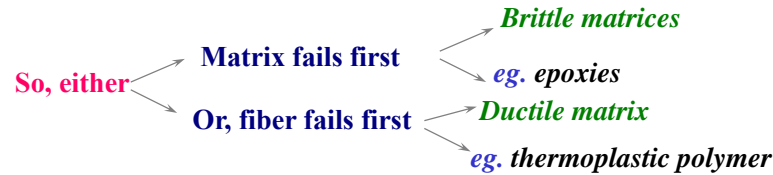




Strength of Aligned Cont. Fiber Composites

Matrix } Same strain
Fiber }

Composite will fail at lower fracture strain



If we assume that strain-to-failure of fiber is less than strain-to-failure of matrix as is most common: i.e. $\epsilon_f^* < \epsilon_m^*$

Then we can estimate the longitudinal strength of the composite as:

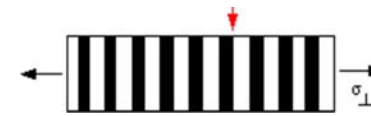
$$\sigma_{cl}^* = \sigma_m' (1 - V_f) + \sigma_f^* V_f$$

Where σ_m' is the stress in the matrix when the fibers fail.



Transverse Strength

Fiber-Matrix interface



- The transverse strength of unidirectional composites is usually very low.
- Fibers can actually act as rather than as reinforcements.
- Transverse strength can be approximated as the matrix strength in many cases.

Material	Longitudinal Tensile Strength (MPa)	Transverse Tensile Strength (MPa)
Glass-Polyester	700	20
Carbon (High Modulus)-Epoxy	1000	35
Kevlar-Epoxy	1200	20

The Fiber Content for Each is Approximately 50 Vol%

Typical Longitudinal and Transverse Tensile Strengths for three Unidirectional Fiber-Reinforced Composites.



Discontinuous & Aligned Fiber Composites

Reinforcement efficiency is lower than that for continuous fibers but the composites are common for

- Modulus of elasticity can be up to of continuous fiber composite
- Tensile strength can be up to of continuous fiber composite

when $\ell > \ell_c$, the longitudinal strength, σ_{cd}^* is given by :

$$\sigma_{cd}^* = \sigma_f^* V_f \left(1 - \frac{\ell_c}{2\ell}\right) + \sigma_m' (1 - V_f)$$

where σ_f^* and σ_m' represent the fiber fracture strength and the matrix stress at fiber failure respectively.

If the fiber length is less than the critical length, $\ell < \ell_c$, then :

$$\sigma_{cd}^* = \frac{\ell \tau_c}{d} V_f + \sigma_m' (1 - V_f)$$

where,
 d = fiber diameter
 τ_c = the of either fiber - matrix bond strength or matrix shear strength



Discontinuous & Randomly Oriented Fiber Composites

When fiber orientation is random and the fibers are short, a "RoM" expression is used for the elastic modulus using an factor, K (which is less than unity- usually between 0.1 - 0.6).

$$E_{cd} = K E_f V_f + E_m V_m$$

Fiber Orientation	Stress Direction	Reinforcement Efficiency
All fibers parallel	Parallel to fibers	1
	Perpendicular to fibers	0
Fibers randomly and uniformly distributed within a specific plane	Any direction in the plane of the fibers	$\frac{3}{8}$
Fibers randomly and uniformly distributed within three dimensions in space	Any direction	$\frac{1}{6}$

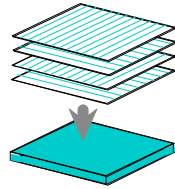


Structural Composites

Particle-reinforced Fiber-reinforced **Structural**

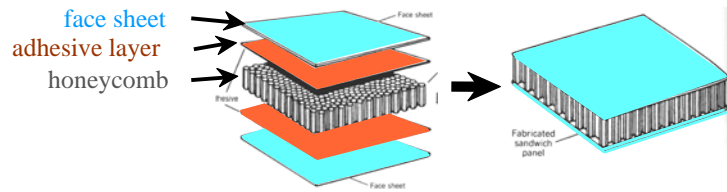
- Stacked and bonded **fiber-reinforced sheets**

- stacking sequence: e.g., 0/90
- **benefit:** balanced, **in-plane stiffness**



- Sandwich panels**

- low density, honeycomb core
- **benefit:** small weight, **large bending stiffness**



Example

A continuous and aligned carbon fiber-epoxy composite consists of 60 vol% fibers. The moduli of elasticity are 700GPa and 3GPa for the fiber and the matrix respectively. Calculate the longitudinal and transverse composite modulus of elasticity? Compare the result with that of steel ($E = 207 \text{ Gpa}$)? Calculate the density of the composite if the density of carbon fiber is 1.8 g/cm^3 and of the epoxy is 1.2 g/cm^3 ?



Next time:

Fracture Mechanics