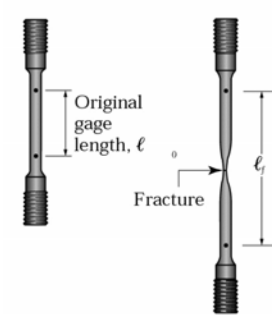
Review of Mechanical Properties

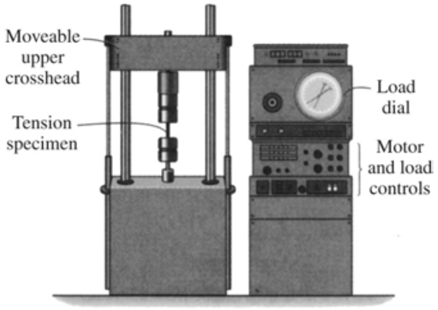
Outline

- Tensile test
- True stress - true strain (flow curve)
- mechanical properties:
  - *Resilience*
  - *Ductility*
  - *Toughness*
  - *Hardness*

Tensile-Test Specimen and Machine

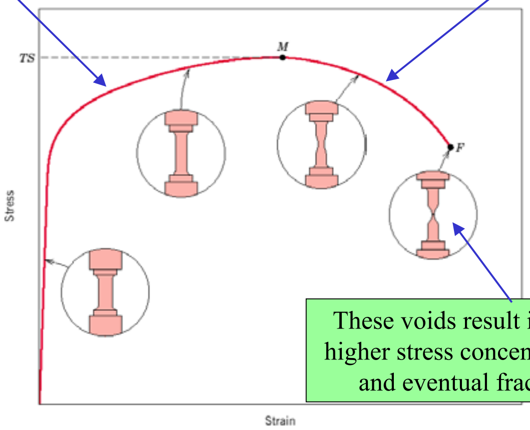


A standard tensile-test specimen before and after pulling, showing original and final gage lengths



A typical tensile-testing machine

Mechanical Behaviour



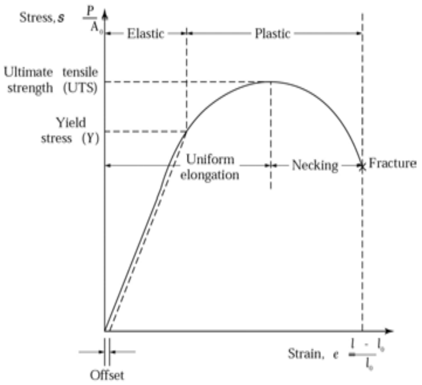
As plastic deformation proceeds, the force increases due to ……………….

As more of the stress becomes concentrated in the neck, formation of ……… occur

These voids result in even higher stress concentrations and eventual fracture

---

Stress-Strain Curve



A typical stress- strain curve obtained from a tension test, showing various features.

- Engineering stress

  $\sigma = P/A_o$

- Engineering strain

  $e = (l - l_o) / l_o$

- Measures of ductility

  % elongation

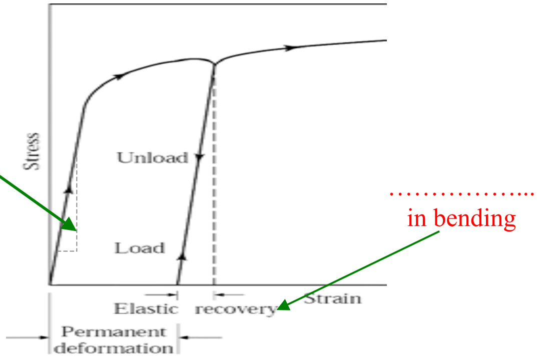
  $(l_f - l_o) / l_o \times 100$

  % Reduction area

  $(A_f - A_o) / A_o \times 100$

Loading and Unloading of Tensile-Test Specimen

E = ……..



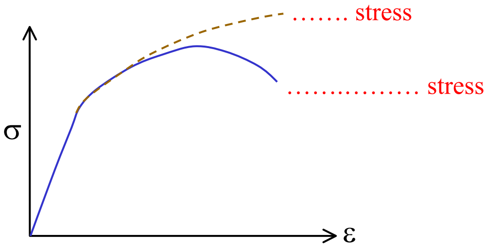
Note that, during unloading, the curve follows a path parallel to the original elastic slope.

Schematic illustration of the loading and the unloading of a tensile- test specimen.

Engineering Stress vs. True Stress

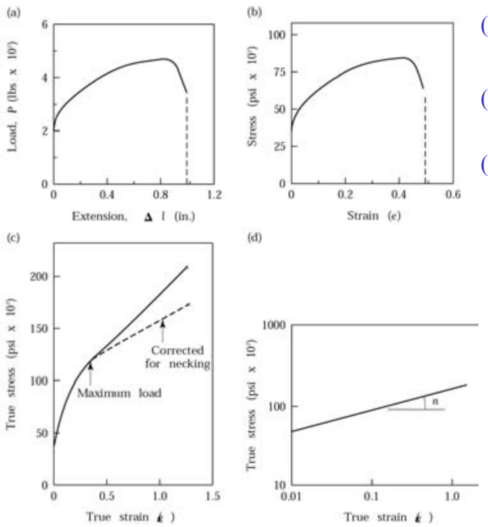
Since the actual cross-sectional area is reduced, use of the initial area gives a lower value than the actual one (the ratio is A_o/A_c).

- True stress, $\sigma = P/A_c$
  - P: load
  - A_c: current area
- True strain, $\varepsilon = \ln (l_c/l_o)$
  - l_c: current length
  - l_o: original length



- Even though the true stress-strain curve gives a more accurate picture of the breaking strength of a material, it is difficult to obtain measurements of *the actual area in real-time*.
- Usually, the reported values are the engineering stress.
- True fracture strength > tensile strength
  - ✓ *but the engineering σ - ε diagram does not show this*

Construction of True Stress-True Strain Curve



(a) Load-elongation curve in tension testing of a stainless steel specimen.

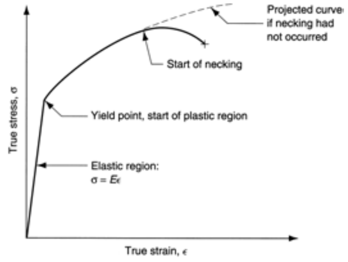
(b) Engineering stress-engineering strain curve, drawn from the data in Fig. a.

(c) True stress-true strain curve, drawn from the data in Fig. b.

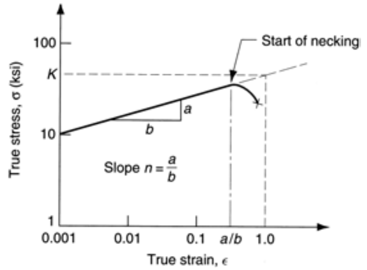
Note that this curve has a positive slope, indicating that the material is becoming stronger as it is strained.

(d) True stress-true strain curve plotted on log-log paper and based on the corrected curve in Fig. c. The correction is due to the triaxial state of stress that exists in the necked region of a specimen.

True Stress-True Strain Curve



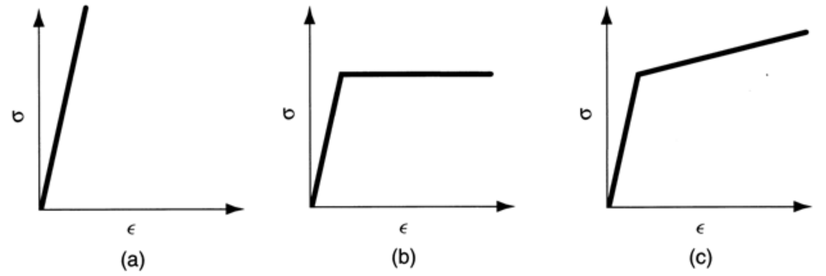
True stress-strain curve



True stress-strain curve plotted on log-log scale

- $\sigma = K\,\varepsilon^n$ Because it is a straight line in a log-log plot
  - K: strength coefficient
  - n: strain-hardening exponent
- The ……… the slope the stronger when material is strained

Categories of Stress-Strain Relationship



Perfectly elastic

- Mech. behavior ↔ *E*
- No plastic flow
- Brittle materials:

- ceramics, many cast irons, and thermosetting polymers

Elastic and perfectly plastic

- *Stiffness defined by E*
- *Once Y reached, deforms plastically at same stress level*
- *Flow curve: K = Y, n = 0*
- *Metals behave like this when heated to sufficiently high temp. (above recrystallization)*

Elastic and strain hardening

- *Hooke's Law in elastic region, yields at Y*
- *Flow curve: K > Y, n > 0*
- *Most ductile metals behave this way when cold worked*

Resilience

Ability of material to absorb energy during **elastic** deformation and then to **give it back** when unloaded.

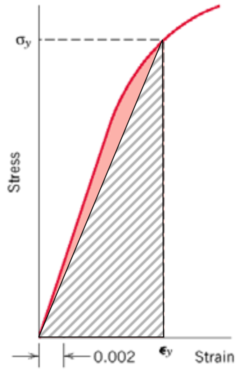
- Measured with **Modulus of Resilience**, **U_r**
- **U_r,** is area under **σ - ε** curve up to yielding:

$$U_r = \int_0^{\varepsilon_y} \sigma \, d\varepsilon$$

- Assuming a **linear elastic** region:

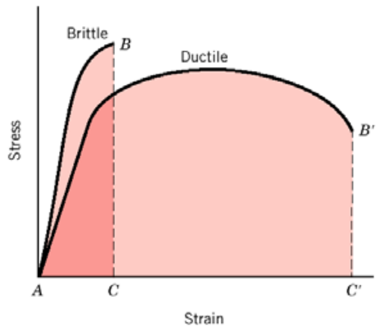
$$U_r = \frac{1}{2}\sigma_y \varepsilon_y = \frac{1}{2}\sigma_y\left(\frac{\sigma_y}{E}\right) = \frac{\sigma_y^2}{2E}$$

- Units are J/m^3



TOUGHNESS

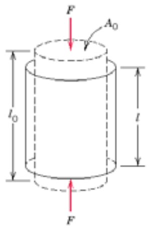
Toughness is the material's ability to absorb energy before **fracture**

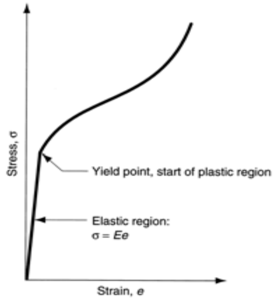


- Toughness is the **area under σ - ε curve up to fracture**.
  - *- Similar to Resilience (same units J/m^3).*
  - *- Larger area ⇒ **tougher** material.*
- So tough materials have a **combination of ……….. and …………**
- Can be measured by an impact test *(MECH 321)*.

Compression Test

- by convention, stress and strain are negative
- used for measuring strength of *brittle materials* and for calculating *forces required in manufacturing processing* which involve compressive deformation



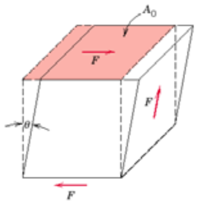


Typical engineering stress-strain curve for a compression test

- Shape of plastic region is different from tensile test because cross-section increases
- Calculated value of eng. stress is ……….
- Although differences exist between eng. σ-ε curves in tension and compression, the true σ-ε curves are *nearly identical*
- Since tensile test results are more common, flow curve values (*K* and *n*) from tensile test data, however, can be applied to compression operations

Shear Test

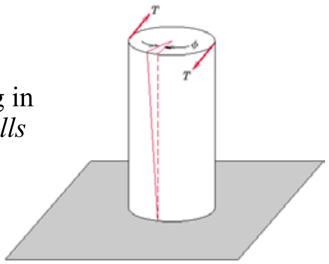
- Shear stress is $\tau = F/A_o$ and γ (*shear strain*) is tangent of shear angle, θ
- $\tau = G\gamma$, G is shear modulus
- Shear tests are often used to measure adhesive bonding, riveted joints etc



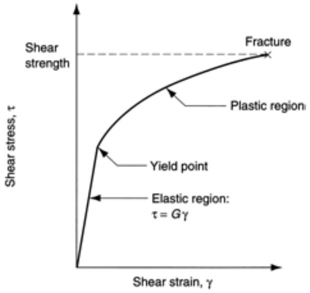
Also, shear stress and strain can be obtained using a torsion test

Torsion Test

- *Torsion* is a variation of shear occurring in *machine axles, drive shafts and twist drills*
- $T = f(\tau)$ and $\gamma = f(\phi)$



Torsion Test



Typical shear stress-strain curve from a torsion test

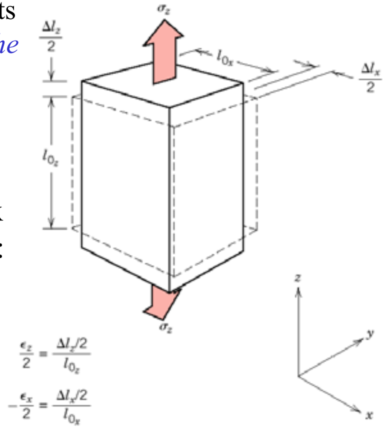
- Relationship similar to flow curve
  - Shear stress at fracture = *shear strength*
  - Shear strength can be estimated from tensile strength: $S \cong 0.7(TS)$
- Since cross-sectional area of test specimen in torsion test does not change as in tensile and compression, engineering stress-strain curve for shear ≅ true stress-strain curve
- For most materials, $G \cong 0.4E$

Poisson's Ratio

- When pulled in tension (Z), a sample gets longer and thinner, i.e., *a contraction in the width (X) and breadth (Y)*
  - *if compressed gets fatter*
- **Poisson's ratio** defines how much strain occurs in the lateral directions (x & y) when strained in the (z) direction:

$$\upsilon = -\frac{\text{lateral strain}}{\text{longitudinal strain}}$$

$$\nu = -\frac{\varepsilon_x}{\varepsilon_z} = -\frac{\varepsilon_y}{\varepsilon_z}$$



- Typical values = 0.2 to 0.5
- For isotropic materials

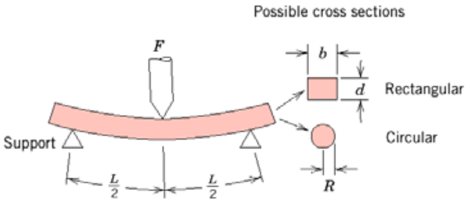
$$E = 2G(1+\nu)$$

Some materials are anisotropic so E & G vary with direction (*e.g. composite materials and single crystals*)

Testing of Brittle Materials

- ➢ Recall: Hard brittle materials (*e.g., ceramics*) possess elasticity but little or no plasticity.
- ➢ Ceramics are not normally tested in tension because:
  - it is difficult to machine to the required geometry
  - it is difficult to grip brittle materials without inducing fracture
  - ceramics typically fail after only ~ 0.1% strain

For these reasons, the mechanical properties are determined using a different approach, the ……………………..:



- specimen geometry is either circular or rectangular cross section
- during the test, the top surface is under compression while the bottom surface is under tension
- maximum tensile stress occurs on the bottom surface, just below the top loading point

HARDNESS

Hardness is a measure of the material's resistance to localized plastic deformation (e.g. dent or scratch)

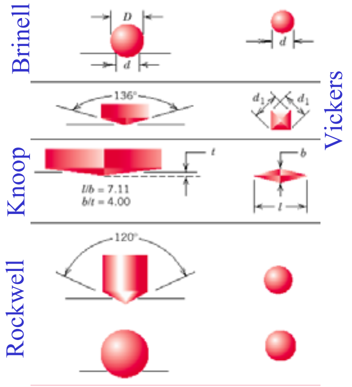
Qualitative Hardness:

- Moh's scale, determined by the ability of a material to scratch another material:
from 1 (softest = talc) to 10 (hardest = diamond)

Quantitative Hardness:

- Different types of quantitative hardness test has been designed
  - Rockwell
  - ………..
  - ………..
  - ………..

HARDNESS



- Usually a small indenter (sphere, cone, or pyramid) is forced into the surface of a material under conditions of controlled magnitude and rate of loading.
- The depth or size of indentation is measured.
- The tests somewhat approximate, but popular because they are easy and non-destructive (except for the small dent).

$$HB = \frac{2P}{\pi D[D - \sqrt{D^2 - d^2}]}$$

Where,
P (the applied load) is in kg,
D is the indenter's diameter
d is the diameter of the resulted indentation

Correlation between Hardness and Tensile Strength

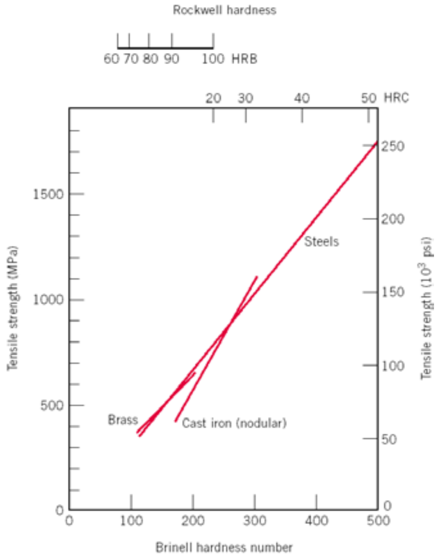
- Both tensile strength and hardness are a measure of a materials resistance to ……………………….

⇒ expect a correlation

- usually TS and HB scale

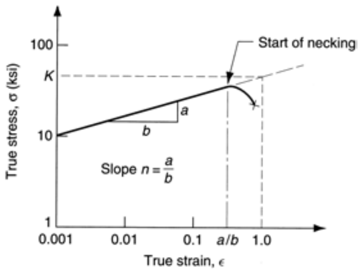
TS (MPa) = 3.45 x HB

TS (psi) = 500 x HB



Example

A metal obeys the Hollomon relationship and has a UTS of 300 MPa.
To reach maximum load requires an elongation of 35%. Find K and n.



True stress-strain curve plotted on log-log scale

Note:
Mechanical Properties of polymers will be explained
when we talk about mechanical shaping of polymers.

Next time:

Fundamentals of Metal Forming