

Sol/hint for Q.1 (ELEC 311-Summer 2013)

```

> id1:=1E-3*4*(2.5-V1-1)^2;
                                     id1 := .004 (1.5 - V1)^2
> id2:=1E-3*4*(-V2-1)^2;
                                     id2 := .004 (-V2 - 1)^2
> y1:=V2-id2*1200+2.5;
                                     y1 := V2 - 4.800 (-V2 - 1)^2 + 2.5
> solve(y1,V2);
                                     -1.464472669, -.3271939973

```

For MN2, VGS must be > VTH. But VGS|MN2=-V2, and VTH=1V. So -V2>1V, V2<-1, accepted V2=-1.46 V (approx).

```

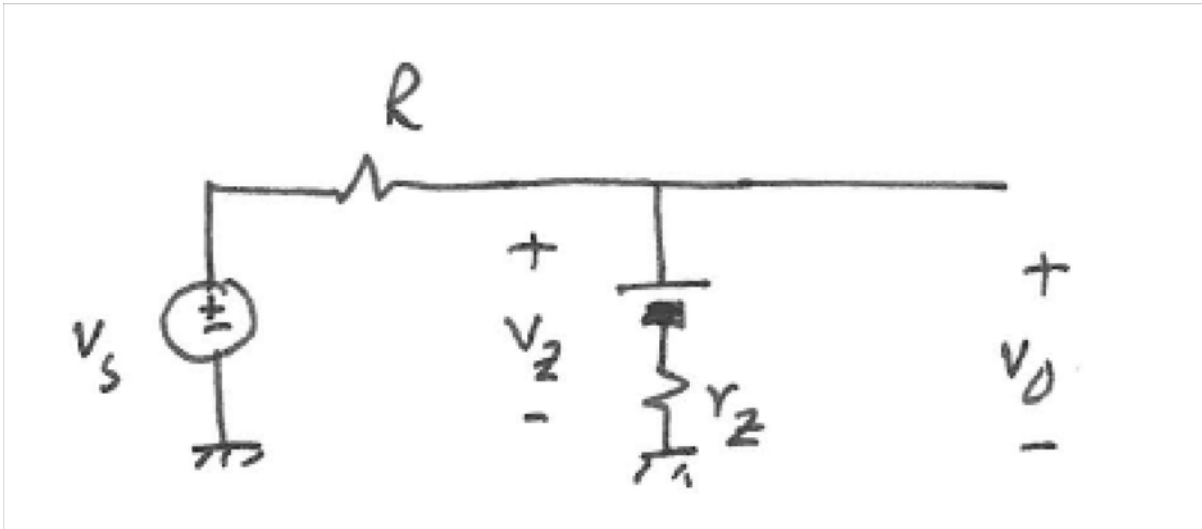
> V2:=-1.46;
                                     V2 := -1.46
> id2:=4E-3*(-V2-1)^2;
                                     id2 := .0008464
> id1:=id2;
                                     id1 := .0008464
> y2:=id1-4E-3*(1.5-V1)^2;
                                     y2 := .0008464 - .004 (1.5 - V1)^2
> solve(y2,V1);
                                     1.040000000, 1.960000000

```

Since VGS of MN1 has to be >VTH, our choice for V1 will be V1=1.04V
So solutions are V1=1.04V, V2=-1.46

Sol/hint for Q.2

(a) The equivalent circuit is (hand-drawing)



(b) $V_z := V_{zo} + I_z * r_z;$

$$V_z := V_{zo} + I_z r_z$$

> **Vz:=6.8;**

$$V_z := 6.8$$

> **Iz:=5E-3;**

$$I_z := .005$$

> **rz:=20;**

$$r_z := 20$$

> **y:=Vz-Vzo-Iz*rz;**

$$y := 6.700 - V_{zo}$$

> **solve(y,Vzo);**

$$6.700000000$$

> **Vzo:=6.7;**

$$V_{zo} := 6.7$$

Line regulation is: $\frac{\Delta V_o}{\Delta V_i} = \frac{\Delta V_z}{\Delta V_i} = \frac{r_z}{r_z + R_{line}}$

> **Rline:=500;**

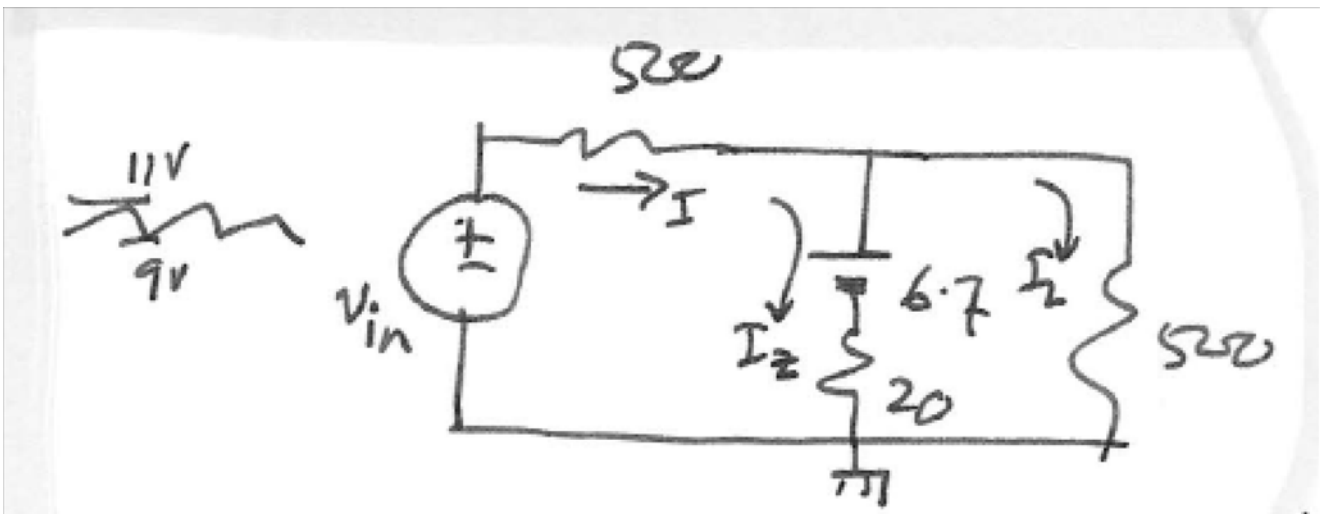
$$R_{line} := 500$$

> **LR:=rz/(rz+Rline);**

$$LR := \frac{1}{26}$$

Line regulation is 1/26, i.e., 38.46 mV/V

(c) With 500 ohms as load, the equivalent circuit is (hand drawing):



If we solve this circuit for I_z , it will turn out that I_z is negative, i.e., the Zener is OFF. Thus

> **Iline:=(Vin-Vload)/Rline;**

$$I_{line} := \frac{1}{500} V_{in} - \frac{1}{500} V_{load}$$

> $V_{load} := V_{zener};$

$$V_{load} := V_{zener}$$

$$V_{zener} = I_z * r_z + V_{z0}$$

$$I_z + I_{load} = I_{line} = V_{in}/500 - V_{zener}/500, \text{ while } I_{load} = V_{zener}/500;$$

Substituting the values $V_{in}=10V$, $V_{z0}=6.7V$, $r_z=20$, solving for I_z will reveal $I_z < 0$.

With the Zener OFF, the output voltage is $V_{in} * (500)/(500+500) = 5V$ for nominal $V_{in} = 10V$

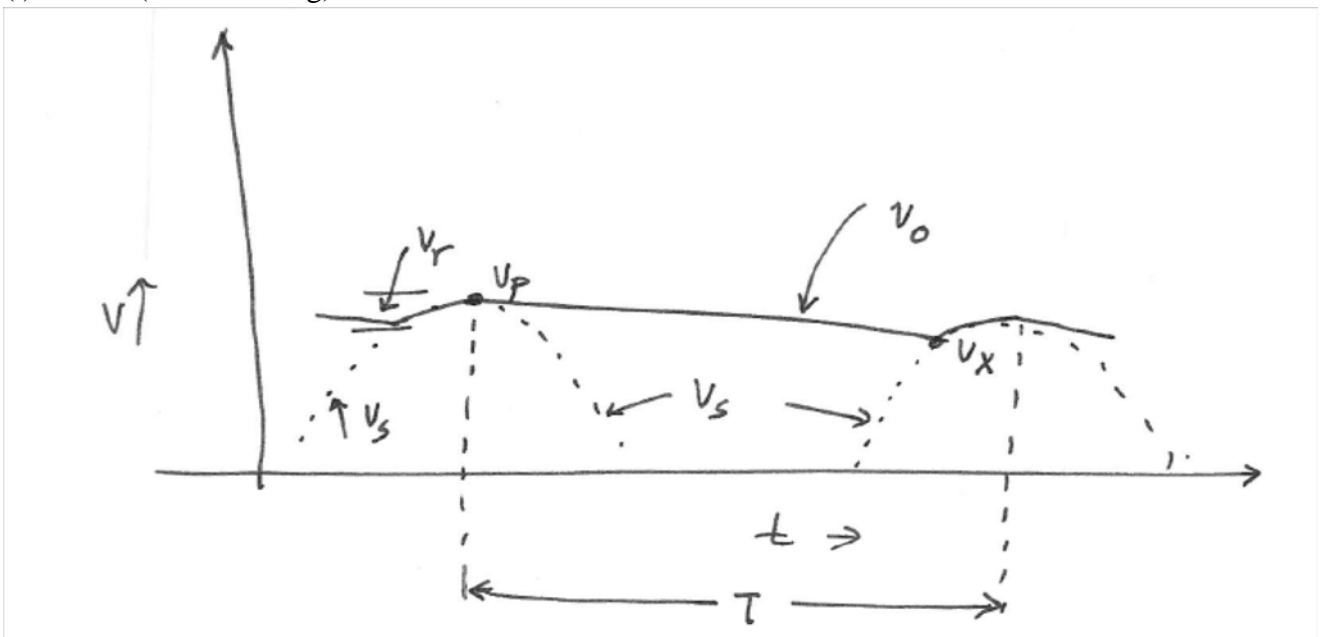
Q.3(a):

(i) DC component = $V_m/\pi = 60/3.142 = 19.1$ volts

(ii) PIV = $0 - (-60) = 60$ volts

Q.3(b):

(i) Sketch (hand drawing)



(ii) The time constant $CR = 100,000 * 1E-5 = 1$ sec. The supply period is : $2 * \pi / (120 * \pi) = 1/60 = 16.7$ m sec. So $CR \gg$ supply period.

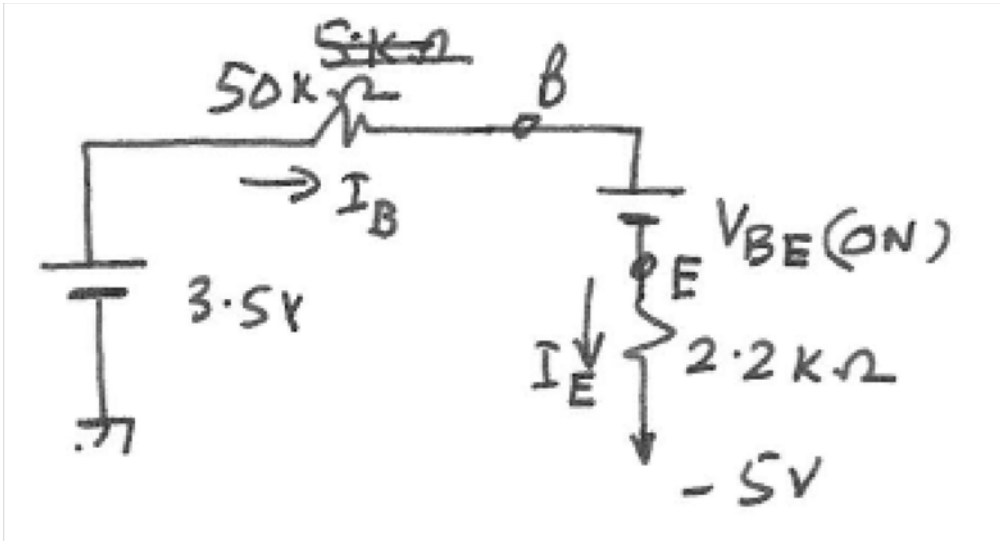
In each cycle, V_o starts from $V_p = 60V$, and decays at the time-constant rate of 1 sec for (approx.) a time of one whole period, i.e., 16.7 m sec. The decayed value is (discharge equation for a simple RC circuit): $60 \exp(-16.7E-3/1) = 60 * (1 - 0.0167) = 59V$ (approx.)

The DC value at output is : $(1/2)[60 + 59] = 59.5V$

The ripple is $60 - 59 = 1V$ pk-pk

(iii) To halve the ripple, we increase the capacitance to double the value, i.e., 20 micro farads.

Q.4: First we need to find I_{dc} , i.e., DC analysis. Consider the base-emitter loop for the DC voltages (hand drawing)



$$y := 3.5 - (I_E/100) * 50E3 - 0.7 - I_E * 2200 + 5;$$

$$y := 7.8 - 2700.000000 I_E$$

> solve (y, I_E);

$$.0028888888889$$

> I_E := 2.9E-3;

$$I_E := .0029$$

> I_C := I_E * beta / (beta + 1);

$$I_C := .0029 \frac{\beta}{\beta + 1}$$

> beta := 99;

$$\beta := 99$$

> I_Cnow := I_C;

$$I_{Cnow} := .002871000000$$

> I_C = 2.87E-3;

$$I_C = .00287$$

> gm := 0.00287 / .025;

$$g_m := .1148000000$$

> r_pi := beta / gm;

$$r_{\pi} := 862.3693380$$

> r_pi := 862.3693380;

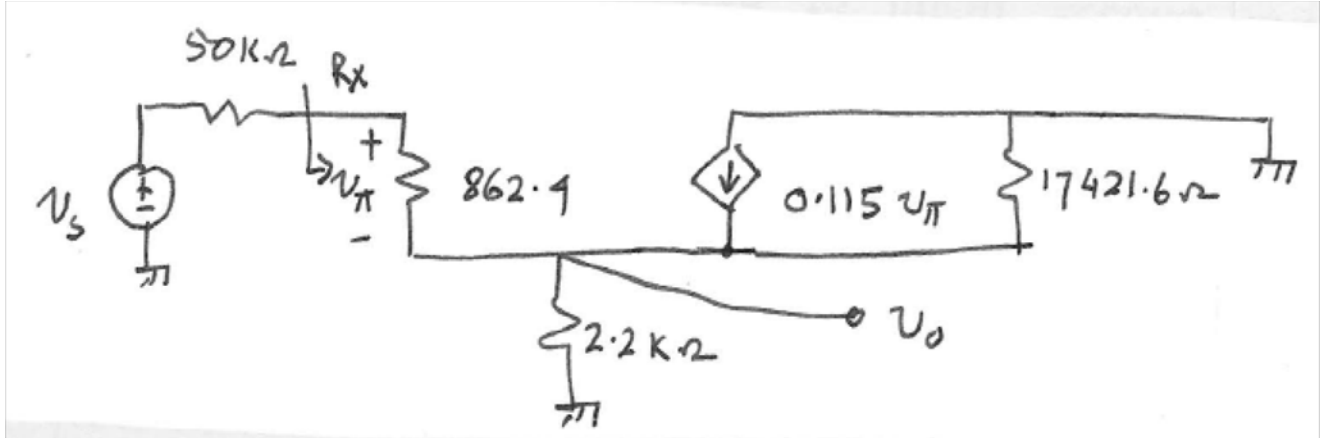
$$r_{\pi} := 862.3693380$$

> r_o := 50 / .00287;

$$r_o := 17421.60279$$

>

The ac equivalent circuit is (hand drawing)



> **RE:=2200;**

RE := 2200

> **Rx:=862.4+100*(RE*ro)/(RE+ro);**

Rx := 196195.7097

> **vb:=Rx*vs/(Rx+50000);**

vb := .7969095397 vs

> **RL:=100*(RE*ro)/(RE+ro);**

RL := 195333.3097

> **vo:=vb*RL/Rx;**

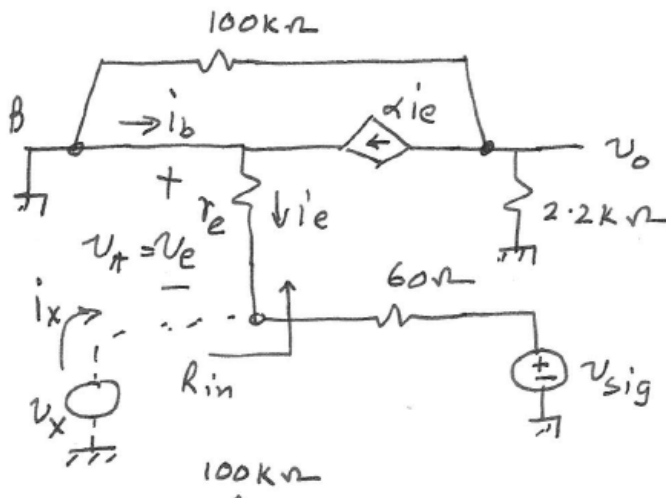
vo := .7934066353 vs

Voltage gain is $v_o/v_s = 0.79$

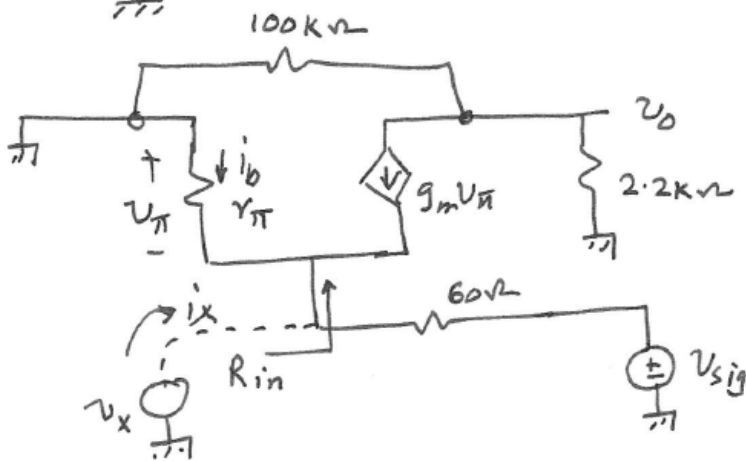
Q.5:

(a) Consider the ac equivalent circuit (T-model and PI-model). Using the dummy source v_x and the

dummy current i_x , we get $R_{in} = \frac{v_x}{i_x} = r_e = \frac{r_\pi}{1+\beta}$



$$\begin{aligned}
 -i_x - i_e &= 0 \\
 i_x &= -i_e \\
 v_x &= -v_e = -i_e r_e \\
 R_{in} &= \frac{v_x}{i_x} = r_e
 \end{aligned}$$



$$\begin{aligned}
 -i_x - i_b - g_m v_\pi &= 0 \\
 i_x &= -i_b - g_m i_b r_\pi \\
 &= -(1 + \beta) i_b \\
 i_b &= v_\pi / r_\pi \\
 v_x &= -v_\pi \\
 \frac{v_x}{i_x} = R_{in} &= \frac{r_\pi}{1 + \beta}
 \end{aligned}$$

From the given schematic $0.5\text{mA} = I_E = I_C + I_B$. So $I_C = (49/50) * 0.5\text{mA} = 0.49\text{mA}$

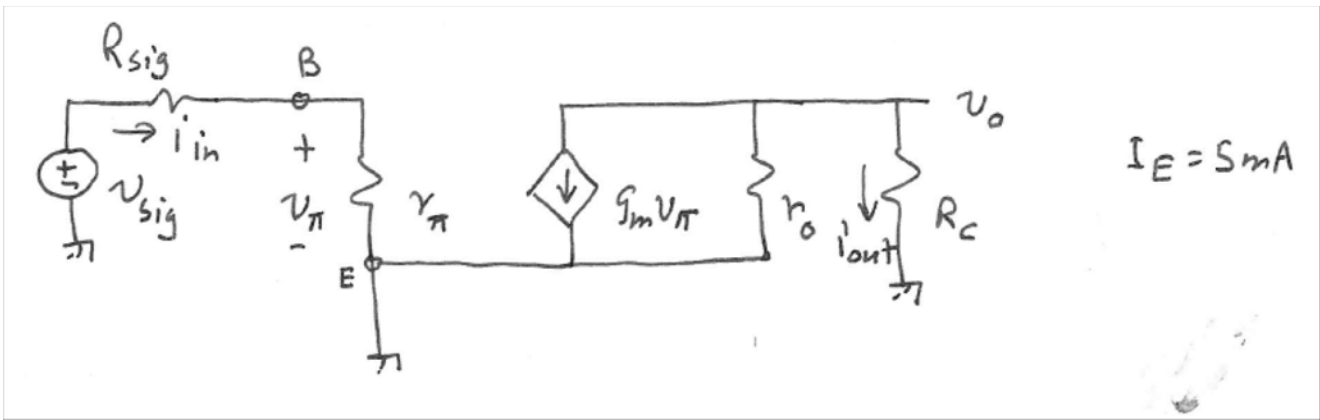
$$g_m = 0.0196\text{ mho}; r_\pi = \frac{\beta}{g_m} = 2500$$

$R_{in} = 50\text{ ohms}$ (i.e., Thermal voltage divided by I_E).

(b) From the equivalent circuit $v_e = v_\pi = \frac{50}{50 + 60} v_{sig}$ has to be $< V_T$ (i.e., 25 mV)

Then $v_s = v_{sig}$ has to be $< \frac{25 \times 110}{50}\text{ mV} = 55\text{ mV}$

Q.6: The equivalent circuit is (hand drawing):



IE:=.005;

IE := .005

> beta:=100;

β := 100

> IC:=IE*beta/(1+beta);

IC := .004950495050

> VA:=50;

VA := 50

> ro:=VA/IC;

ro := 10100.00000

> gm:=IC/.025;

gm := .1980198020

> rpi:=beta/gm;

rpi := 504.9999999

Put the above values in the equivalent circuit.

(a) The voltage gain is: $\frac{v_o}{v_{sig}} = -g_m \frac{r_o R_C}{r_o + R_C} \times \frac{r_\pi}{r_\pi + R_{sig}}$

Substituting the values

> x1:=(ro*1000)/(ro+1000);

x1 := 909.9099099

> x2:=rpi/(rpi+10000);

x2 := .04807234649

> gain:=-gm*x1*x2;

gain := -8.661684053

Voltage gain is -8.66 V/V

(b)

> iout:=vo/1000;

$i_{out} := \frac{1}{1000} v_o$

```

> iin:=vsig/(rpi+10000);
                               iin := .00009519276535 vsig
> igain:=iout/iin;
                               igain := 10.50500000  $\frac{v_o}{vsig}$ 
> i_gain:=10.505*gain;
                               i_gain := -90.99099098

```

Small signal current gain is -90.99 A/A

Q.7: Using several of the the given data

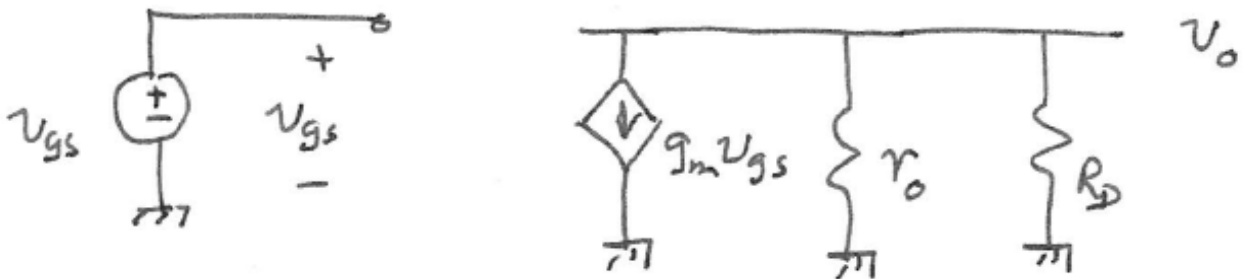
```

> K:=.005;
                               K := .005
> WLratio:=2;
                               WLratio := 2
> Vov:=0.7-0.5;
                               Vov := .2
> gm:=K*WLratio*Vov;
                               gm := .0020

```

(a) The ac transconductance is 0.002 mho

(b) The ac equivalent circuit is (hand drawing):



The DC current is $(I_D) = K \frac{W}{2L} V_{ov}^2 = .005 \times \frac{2}{2} \times 0.2^2$ (assuming saturation region of operation)

```

> ID:=K*(WLratio/2)*Vov^2;
                               ID := .0002000000000
> VD:=2-ID*5000;
                               VD := 1.000000000
> VDS:=VD;
                               VDS := 1.000000000

```

VDS=1V is > Vov (=0.2V), so the operation in saturation region is confirmed.

```

> Vax:=50;

```


$$V_{Ax} := 50$$

$$> \text{rox} := V_{Ax} / I_D;$$

$$\text{rox} := 250000.0000$$

$$> R_D := 5000;$$

$$R_D := 5000$$

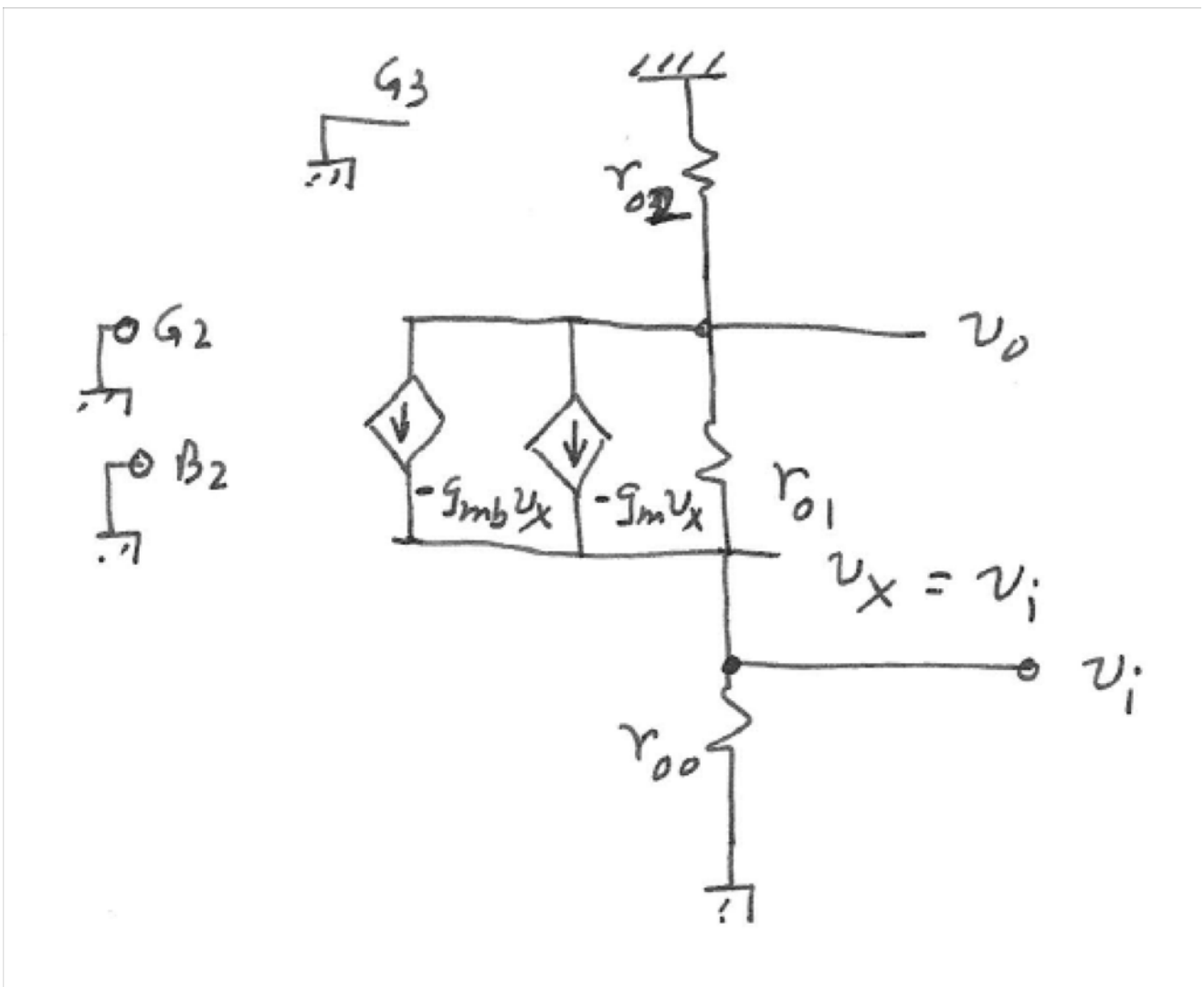
$$> V_{\text{gain}} := -g_m * (\text{rox} * R_D) / (\text{rox} + R_D);$$

$$V_{\text{gain}} := -9.803921569$$

The small signal voltage gain is -9.8 V/V

Q.8

The ac equivalent circuit is (hand drawing):



KCL at v_o node (note $v_x = v_i$, the input signal voltage)

$$\frac{v_o}{r_{o2}} - (g_m + g_{mb})v_i + \frac{v_o - v_i}{r_{o1}} = 0$$

> **y:=vo/ro2-(gm+gmb)*vi+(vo-vi)/ro1;**

$$y := \frac{v_o}{r_{o2}} - (g_m + g_{mb})v_i + \frac{v_o - v_i}{r_{o1}}$$

> **solve(y,vo);**

$$\frac{v_i (r_{o1} g_m + r_{o1} g_{mb} + 1) r_{o2}}{r_{o1} + r_{o2}}$$

> **gain:=(ro1*gm+ro1*gmb+1)*ro2/(ro1+ro2);**

$$\text{gain} := \frac{(r_{o1} g_m + r_{o1} g_{mb} + 1) r_{o2}}{r_{o1} + r_{o2}}$$

The voltage gain is: $\frac{v_o}{v_i} = \frac{1.2 g_m r_{o1} + 1}{\frac{r_{o1}}{r_{o2}} + 1}$ (since, $g_{mb} = 0.2 g_m$)