

## **Phase equilibria and thermodynamics of the Mg-Si-Li system and remodeling of the Mg-Si system**

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### **Abstract**

The ternary Li-Mg-Si phase relations were established using high purity samples prepared by levitation melting. Analysis was done using X-ray powder diffraction (XRD), optical metallography and differential thermal analysis (DTA) in customized sealed tantalum crucibles. Three ternary intermetallic phases were confirmed in this system:  $\tau_1$  ( $\text{Li}_8\text{MgSi}_6$ ),  $\tau_2$  ( $\text{Li}_{12}\text{Mg}_3\text{Si}_4$ ), and  $\tau_3$  ( $\text{Li}_2\text{MgSi}$ ). The  $\text{LiMg}_2\text{Si}$  phase reported previously is not a separate phase but the interstitial solid solution of Li in the binary  $\text{Mg}_2\text{Si}$  phase,  $\text{Li}_x\text{Mg}_2\text{Si}$ , at the maximum  $x \approx 0.91 \pm 0.05$ . Ternary liquidus data and phase transformations were also measured.

A thermodynamic assessment of the ternary Li-Mg-Si system was worked out in parallel to the experimental study and used to select the relatively small number of our key experiments. The final consistent thermodynamic description is well supported by the present experimental data. It was found that the published thermodynamic parameter sets for the binary Mg-Si subsystem produce an artificial inverted liquid miscibility gap at higher temperature. This system was remodeled to obtain data that could be reliably extrapolated to various temperatures and the ternary system. The experimentally supported calculated phase equilibria in the entire composition and temperature range of the Li-Mg-Si system are presented, including the liquidus surface and invariant reactions. Gradual changes in a monovariant eutectic/peritectic reaction type occur in this system. The intricacies involved due to solid solutions and the failure of the classical tangent criterion are discussed for some ternary alloys.

## 1 Introduction

The search for new magnesium alloys is primarily driven by the demand for further weight reduction in automotive industry. Present magnesium die casting alloys are based on the Mg-Al system. To achieve a better creep resistance the Mg-Al based alloys should usually have a low Al-content and show the formation of stable intermetallic particles. A well known alloying addition is silicon. Commercial Mg-Al-Si die casting alloys as AS41 and AS21 show improved creep resistance. On the other hand, in researched Mg-Al-Li alloys the Li addition produces a further density reduction and increasing of ductility. Small amounts of Li (<4 wt.%) also increase the corrosion resistance. The interactions of both alloying elements in the quaternary Mg-Al-Li-Si system are not known. For a focused development of new alloys in that system, the phase equilibria are needed together with the underlying thermodynamic data. The tool of computational thermodynamics can be used based on that, as demonstrated for the development of other new magnesium alloys [2001Sch]. The consistent generation of these data using both experimental work and thermodynamic calculations was the global aim of this work.

This study was done in the framework of the generation of a multicomponent database for magnesium alloys. The ternary Li-Mg-Si system is also needed as an important subsystem for Mg-Li-Al-Si-X alloys. Since published experimental data about the Li-Mg-Si system are very limited, a particular experimental investigation was carried out in parallel with the thermodynamic modeling in this work. This procedure allowed selecting the ternary key samples. Scrutinizing the published binary thermodynamic datasets resulted in the need to remodel the binary Mg-Si subsystem since an artificial inverted liquid miscibility gap at higher temperature was detected. The comprehensive comparison of the experimental Mg-Si data with the calculation from the new model is also presented in this work.

## 2 Literature data

### 2.1 Ternary constitutional data

The few experimental investigations of the Li-Mg-Si system published in literature [1986Nes, 1992Pav1, 1992Pav2] presented altogether five ternary phases of various compositions. The isothermal section of the phase diagram at 200°C was studied by [1992Pav2]. They prepared alloys by arc melting in a purified Ar atmosphere using a Li-Mg master alloy [1992Pav2]. Pure metals were also used for the preparation of alloys with a purity Li – 98.2 wt.%, Mg – 99.98 wt.% and Si – 99.9999 wt.%. Annealing was carried out in Ta containers at 200°C for 240 h. X-ray powder diffraction was used for the phase analysis. Four ternary phases  $\text{Li}_5\text{MgSi}_4$ ,  $\text{Li}_{12}\text{Mg}_3\text{Si}_4$ ,  $\text{Li}_2\text{MgSi}$  and  $\text{LiMg}_2\text{Si}$  were reported in this system [1992Pav2]. All the phases have no significant solubility. In addition, no ternary solubility of binary phases was reported.

The crystal structures of three of the four phases were determined by X-ray powder diffraction. The crystal structure of the  $\text{Li}_5\text{MgSi}_4$  phase was not determined. Earlier [1986Nes] reported the monoclinic phase  $\text{Li}_8\text{MgSi}_6$  ( $\text{Li}_{53.33}\text{Mg}_{6.77}\text{Si}_{40}$ ) which has similar composition to  $\text{Li}_5\text{MgSi}_4$  ( $\text{Li}_{50}\text{Mg}_{10}\text{Si}_{40}$ ). It may be assumed that both compositions describe the same phase and  $\text{Li}_8\text{MgSi}_6$  is the real composition of the phase. It will be shown later that the phase  $\text{LiMg}_2\text{Si}$  actually corresponds to the solution phase  $\text{Li}_x\text{Mg}_2\text{Si}$  extending from binary  $\text{Mg}_2\text{Si}$ .

### 2.2 Thermodynamics of binary systems Li-Mg and Li-Si

No thermodynamic data for the ternary Li-Mg-Si system could be found in literature. The parameter sets for the binary sub-systems given in the literature are discussed below.

The thermodynamic model for the Li-Mg system is taken from the evaluation of Saunders presented in COST 507 database [1998Sau], see Fig. 1. These data were also

presented in [1990Sau]. DTA investigations, activity and enthalpy measurements of liquid phase were used for the optimization. The calculated phase diagram shows an excellent agreement with literature data. A detailed discussion and comparison with experimental data is presented in [1990Sau].

Two sets of parameters were published for the binary Li-Si system [1995Bra]. In the first assessment of [1995Bra] the chemical potential values for the solid two-phase regions are in good agreement with the experimental values. However, the liquidus in the region of the  $\text{Li}_{12}\text{Si}_7$  and  $\text{Li}_7\text{Si}_3$  phases shows significant deviation from the experimental points using the same partial Gibbs energies. In the second assessment, these potential values were neglected [1995Bra]. A better agreement with the experimental phase diagram data is shown, but unrealistic values for the parameters are produced. In the present study, the first assessment of [1995Bra] was preferred because of the more realistic Gibbs energies. The calculated phase diagram is given in Fig. 2.

### **3 Remodeling of the Mg-Si system**

A new modeling of the Mg-Si phase diagram was necessary, because both of the thermodynamic models presented in recent publications [1997Feu, 2000Yan] exhibit an inverted miscibility gap of the liquid phase at higher temperatures, which are shown in Figs. 3 and 4. These inverted miscibility gaps are considered artifacts produced by unsuitable temperature dependencies of liquid phase parameters. Such a behavior cannot be accepted, especially for an extrapolation of the binary thermodynamic model into the ternary system at various temperatures.

Therefore, the Mg-Si system was remodeled to obtain a phase diagram without an artificial miscibility gap. As a starting point, the assessment of [2000Yan] was used. After correction of the thermodynamic model and reducing the number of parameters the calculated phase diagram shows still a good agreement with the results of experimental investigations, see Figs. 5 and 6. No artificial miscibility gap occurs in the liquid even if calculating up to 6000°C, not shown in Fig. 5. The thermodynamic description of the liquid phase is also in good agreement with experimental thermodynamic data given in Figs. 7, 8 and 9. It should be noted that the slope of the integral enthalpy of mixing at the Mg-rich side in Fig. 8, seemingly not steep enough, should be even less steep considering the partial enthalpy data of [1997Feu] given in Fig. 9. This inconsistency within the experimental enthalpy data indicate that probably a larger error might be associated with these data, justifying the larger deviation seen in Figs. 8 and 9 and also justifying a more simple thermodynamic description of the liquid phase.

Only one binary phase  $\text{Mg}_2\text{Si}$  forms in Mg-Si system. It melts congruently and has no detectable homogeneity range. The solid solubility of Mg in (Si) is considered negligible. On the base of X-ray analysis it was shown [1940Kle] that the solubility of Si in (Mg) should be less than 0.1 at.% Si. Raynor [1940Ray] reported the maximum solubility of Si in (Mg) at  $\approx 0.003$  at.% Si. This is in good agreement with the results of [1959Yue], who reported a value of 0.0028 at.% Si from modified zone-melting technique. By contrast, [1977Sch] claimed a larger solubility of  $\approx 0.17$  at.% Si in (Mg) on the base of DTA investigation given in Fig. 6, but since this data is in contradiction with the more direct observations it was not accepted for the modeling. The thermodynamic equations are given in section 6.

### **4 Ternary experimental investigation**

To determine a liquidus surface and invariant reactions and to check the ternary phase stability in the Li-Mg-Si system eight key samples were prepared in the present study, as given in Table 1. The phase analysis was performed by X-ray powder diffraction (XRD) and optical metallography using as-cast alloys as well as samples after DTA treatment. Differential thermal analysis (DTA) was used for the polythermal investigation.

Starting materials were magnesium chips (99.98 mass%, Alfa), lithium bulk material (99.9 mass%, Chemetall, Frankfurt) and silicon chips (99.9998 mass%, Wacker). The elements were weighed and mixed in a glove-box with Ar atmosphere and pressed under a pressure of 100 MPa into small pellets of around 0.5 g. Alloys were prepared from that by levitation melting under purified argon atmosphere. Heating power was controlled carefully to avoid evaporation. Weight loss was found less than 1 mass % after levitation melting.

For XRD analysis the alloys were powdered in a hand mill and mixed with inert oil to avoid oxidation. Powders could only be produced for Mg-poor samples but not for the highly ductile Mg-rich samples. These samples were polished to obtain a flat surface for X-ray measurements. The X-ray powder diffractometer Siemens D-5000 with  $\text{CoK}\alpha$ - radiation was used for measurements. The routine measurements were performed with a step  $0.02^\circ$  of  $2\theta$  and 3 seconds exposition time in the point. The obtained diffraction patterns were analyzed quantitatively in comparison with simulated X-ray spectra using the program PowderCell 2.1 [1999PC].

Liquidus temperatures and multiphase reactions of the system were investigated by DTA. The samples were sealed under pure argon at 1 bar in specially adapted tantalum containers using electric arc welding. Evaporation and oxidation of the samples was completely avoided with this technique. This procedure enables reproducible DTA signals that cannot be obtained otherwise. As a reference,  $\text{Al}_2\text{O}_3$  in another sealed Ta crucible was used. The differential thermal analysis was performed using a Netzsch DTA 404. The heating and cooling rates were 5 and 1 K/min. No reactions with the crucibles were observed. For all samples several heating and cooling runs were performed. After thermal analysis, the alloys were again examined by XRD using the same procedures as described above.

## 5 Results

### 5.1 Solid state phase relations

All sample compositions with the identified phases are given in Table 1. Two series of samples were prepared and investigated. The first series of samples, "a" to "d", see Fig. 10, was prepared to check the compositions of ternary intermetallic phases reported in literature. The X-ray examination of samples confirmed the formation of the reported phases  $\tau_1$ ,  $\tau_2$  and  $\tau_3$  as given in Table 2. The second series of samples, "e" to "h", was prepared to investigate in more detail the liquidus surface and the phase relations in the Mg-rich corner.

Three ternary compounds  $\text{Li}_8\text{MgSi}_6$ ,  $\text{Li}_{12}\text{Mg}_3\text{Si}_4$ ,  $\text{Li}_2\text{MgSi}$  were confirmed, denoted as  $\tau_1$ ,  $\tau_2$  and  $\tau_3$ , respectively. The corresponding samples "a" to "c" showed traces of additional phases, as presented in Table 1. This supports the finding of [1992Pav] that the ternary phases  $\tau_1$ ,  $\tau_2$  and  $\tau_3$  are stoichiometric because of inevitable deviations from the nominal composition. The lattice parameters of the ternary phases determined in our study as shown in Table 2 agree perfectly well with published data [1992Pav2]. This also indicates that all the ternary phases have negligible ranges of homogeneity. The  $\text{LiMg}_2\text{Si}$  phase reported by [1992Pav2] was found to be the solid solution of Li in the  $\text{Mg}_2\text{Si}$  phase, denoted as  $\text{Li}_x\text{Mg}_2\text{Si}$  in the present work. This solid solution was detected by X-ray powder diffraction as well as by metallography. The microstructure of the sample "e" with the composition  $\text{Li}_{14}\text{Mg}_{58}\text{Si}_{28}$  ( $\text{Li}_{0.5}\text{Mg}_2\text{Si}$ ) is presented in Fig. 11. It shows an essentially homogeneous phase ( $\text{Li}_x\text{Mg}_2\text{Si}$ ) with trace amounts of (Mg), thus proving the solid solubility of  $\text{Li}_x\text{Mg}_2\text{Si}$ . This sample would have been located in the

center of the two-phase field "LiMg<sub>2</sub>Si + Mg<sub>2</sub>Si" assumed by [1992Pav2], which is obviously not present. This ternary solubility of the Mg<sub>2</sub>Si binary compound was detected up to ≈23 at.% Li, corresponding to a composition Li<sub>x</sub>Mg<sub>2</sub>Si with x≈0.91 with an error of probably ± 0.05. This limit was estimated using Vegard's law, but since the lattice parameter variation is very small, we could not estimate the limit of solubility more accurately. The crystallographic parameters of the accepted ternary compounds and the Li<sub>x</sub>Mg<sub>2</sub>Si solid solution are presented in Table 2. All the phases detected in samples "a" to "h" after the final slow cooling of the DTA cycles using XRD as well as metallography, see Table 1, are in perfect agreement with the calculated phase equilibria as discussed later.

## 5.2 Polythermal investigation

The first series of thermal analysis measurements was carried out to determine the melting temperature of ternary compounds and the invariant temperatures near the liquidus. Therefore, alloys with the composition of the ternary phases presumed in literature were prepared. All samples were measured several times to verify the results. A preliminary thermodynamic model was then constructed and used to calculate the most important phase equilibria. Since the compositions of samples had small deviations from the stoichiometric compositions of ternary phases, it was possible to detect also some of the phase transformations below the melting points of samples "a" to "c" as given in Table 3.

A second series of sample compositions, "d" to "h", were selected to investigate the Mg-rich corner. Alloy compositions and the DTA results together with the calculated values and their interpretation are presented in Table 3.

In order to compare the calculated phase relations in the Li-Mg-Si system with experimental data several polythermal sections were calculated and presented in Figs. 12 to 16. The phase relations in the Mg-rich region are shown in the latter two Figures, 15 and 16. The metallographic analysis of as-cast samples "g" and "f", marked in Fig. 15, show a perfect agreement with the calculated phase diagram as demonstrated by their microstructure in Figs. 17 and 18. These samples were "etched" simply by storing for 20 h in dry air, resulting in a darkening of phases with increasing Li-content. This nicely develops the two-phase structure in Fig. 17 and the three-phase structure in Fig. 18.

## 6 Thermodynamic modeling

The Gibbs energy function  $G_i^{0,\phi}(T) = G_i^\phi(T) - H_i^{SER}$  for the element  $i$  ( $i=Li, Mg, Si$ ) in the  $\phi$  phase ( $\phi = bcc$  (Li),  $hcp$  (Mg), diamond (Si) or liquid) is described by the equation:

$$G_i^{0,\phi}(T) = a + b \cdot T + c \cdot T \cdot \ln T + d \cdot T^2 + e \cdot T^3 + f \cdot T^{-1} + g \cdot T^7 + h \cdot T^{-9} \quad (\text{Eq. 1})$$

where  $H_i^{SER}$  is the molar enthalpy of the stable element reference (SER) at 298.15 K and 1 bar, and  $T$  is the absolute temperature. The Gibbs energy functions for Li, Mg and Si are taken from the SGTE compilation by Dinsdale[1991Din].

The liquid,  $hcp$  (Mg) and  $bcc$  (Li) solution phases are described by the substitutional solution model. For the liquid Mg-Si phase the molar Gibbs energy is expressed by the following equation:

$$\begin{aligned} G^{Liq} &= x_{Mg} G_{Mg}^{0,Liq} + x_{Si} G_{Si}^{0,Liq} \\ &+ RT(x_{Mg} \ln x_{Mg} + x_{Si} \ln x_{Si}) \\ &+ x_{Mg} x_{Si} (L_{Mg,Si}^{0,Liq} + L_{Mg,Si}^{1,Liq} (x_{Mg} - x_{Si}) + L_{Mg,Si}^{2,Liq} (x_{Mg} - x_{Si})^2 + \dots) \end{aligned} \quad (\text{Eq. 2})$$

in which  $R$  is the gas constant and  $x_{Mg}$  and  $x_{Si}$  are the molar fractions of Mg and Si. The interaction parameters  $L^0$ ,  $L^1$  and  $L^2$  may be linearly temperature dependent and are to be optimized. The phases hcp (Mg) and bcc (Li) are described by analogous equations. The ternary data are calculated using a Redlich-Kister/Muggianu type extrapolation from the binary sets, as given explicitly in [2001Sch], which is reasonable for these chemically not too asymmetric components. No additional ternary interaction parameters were used for any of these phases.

The binary compound  $Mg_2Si$  was modeled as stoichiometric phase referred to the stable elements, and the Gibbs energy (per mol of atoms) is given by :

$$G_{Mg:Si}^{0,Mg_2Si} = \frac{2}{3} G_{Mg}^{0,hcp} + \frac{1}{3} G_{Si}^{0,diamond} + A^{Mg_2Si} + B^{Mg_2Si} \cdot T \quad (\text{Eq. 3})$$

where the parameters  $A^{Mg_2Si}$  and  $(-B^{Mg_2Si})$  correspond to the enthalpy and entropy of formation, respectively.

The  $Li_xMg_2Si$  phase, extending from the binary  $Mg_2Si$ , was modeled as interstitial solid solution,  $(Mg)_2(Si)_1(Va,Li)_1$ , since the ternary solubility of this compound was experimentally detected to be directed towards pure Li. That means the Mg/Si ratio is constant in that phase. The Gibbs energy (per mol of sites) of this three-sublattice line compound is expressed by

$$G^{Li_xMg_2Si} = y_{Va} G_{Mg:Si:Va}^{0,Li_xMg_2Si} + y_{Li} G_{Mg:Si:Li}^{0,Li_xMg_2Si} + \frac{1}{4} \cdot R \cdot T (y_{Va} \cdot \ln y_{Va} + y_{Li} \cdot \ln y_{Li}) \quad (\text{Eq. 4})$$

in which  $y_{Va}$  and  $y_{Li}$  are the site fractions of vacancies and Li on the third sublattice. The parameters  $G_{Mg:Si:*}^{0,Li_xMg_2Si}$  (also called compound energies) express the Gibbs energy of the stoichiometric end members of the  $Li_xMg_2Si$  phase. Specifically,  $G_{Mg:Si:Va}^{0,Li_xMg_2Si} = \frac{3}{4} G_{Mg:Si}^{0,Mg_2Si}$  is the Gibbs energy of binary  $Mg_2Si$ , see (Eq. 3). The factor 3/4 accounts for the fact that the phase  $(Mg)_2(Si)_1(Va)_1$  has (3 atoms/ 4 sites) in contrast to the phase  $(Mg)_2(Si)_1$ . The only adjustable parameter,  $G_{Mg:Si:Li}^{0,Li_xMg_2Si}$ , is that of a fictive end member compound at 25 at.% Li, slightly beyond the solubility limit of  $\approx 23$  at.% Li for the  $Li_xMg_2Si$  phase. This parameter is sufficient to describe the stability of  $Li_xMg_2Si$  and thus the interactions within the third sublattice are taken to be ideal in the  $Li_xMg_2Si$  structure, as given in Eq. (4). Ternary solubilities of other binary phases were not found and therefore neglected for the calculation.

The ternary phases  $\tau_1$ ,  $\tau_2$  and  $\tau_3$  are modeled as stoichiometric compounds, by simply extending Eq. (3) to the component Li with the reference state  $G_{Li}^{0,bcc}$ . No homogeneity ranges were modeled since experimentally no solubilities were observed.

The binary Mg-Si parameters were optimized as detailed in section 3. Using the binary data sets, the ternary Li-Mg-Si phase diagram was first calculated by extrapolation without considering the ternary phases. The solid state phase relations found in our experimental work and the measured liquidus temperatures were used to determine the linear temperature dependence of the Gibbs energy functions for the ternary phases. The single thermodynamic parameter of the  $Li_xMg_2Si$  solution phase was adjusted to meet both the liquidus temperatures measured in the Mg-rich region and the experimentally observed maximum solubility of  $\approx 23$  at.% Li. The software Pandat [2002Chen] was used for the calculation.

The comparison between measured and calculated transition temperatures is presented in Table 3 and in Figs. 12 to 16. The calculated ternary invariant reactions are presented in Table 4. The thermodynamic parameters assessed in the present work are given in Table 5. The calculated liquidus surface and the calculated isothermal section of the Li-Mg-Si phase diagram are presented in Figs. 19 to 22. In Fig. 19, the primary liquidus field of  $\text{Li}_{12}\text{Si}_7$  is extremely small and located near the binary edge of the phase diagram. Visible on the liquidus surface in that region is merely the primary field of  $\tau_1$ .

## 7 Discussion

The existence of three ternary phases  $\tau_1$  ( $\text{Li}_8\text{MgSi}_6$ ),  $\tau_2$  ( $\text{Li}_{12}\text{Mg}_3\text{Si}_4$ ) and  $\tau_3$  ( $\text{Li}_2\text{MgSi}$ ) was confirmed during the investigation of the Mg-Li-Si system. Also confirmed was the previous finding [1992Pav2] that all these phases show negligible ranges of homogeneity.

It was determined by X-ray diffraction and by metallographic investigation that the  $\text{LiMg}_2\text{Si}$  phase reported in [1992Pav2] is approximately the maximum of the solid solution of Li in the binary  $\text{Mg}_2\text{Si}$  phase,  $\text{Li}_x\text{Mg}_2\text{Si}$  at  $x \approx 0.91 \pm 0.05$ . This was also corroborated by DTA measurements, since the liquidus point of the sample "e", ( $\text{Li}_{14}\text{Mg}_{58}\text{Si}_{28}$  or  $\text{Li}_{0.5}\text{Mg}_2\text{Si}$ ), is higher than the liquidus point of the sample "d", ( $\text{Li}_{25}\text{Mg}_{50}\text{Si}_{25}$  or  $\text{Li}_{1.0}\text{Mg}_2\text{Si}$ ), see Fig. 14 or Table 3.

The type of solution of Li must be considered to be interstitial because of three reasons: (i) the structure type originally reported [1992Pav2] for  $\text{LiMg}_2\text{Si}$  ( $\text{MnCu}_2\text{Au}$ ) has Li on interstitial sites in  $\text{Mg}_2\text{Si}$ ; (ii) the numerical simulation of the X-ray spectra assuming these Li interstitials in  $\text{Li}_x\text{Mg}_2\text{Si}$  using the program PowderCell 2.1 [1999PC] agrees well with the experimental spectra but not so well if we assume a substitutional solution; and (iii) the direction of solubility range in the ternary is a straight line from  $\text{Mg}_2\text{Si}$  towards Li, which means that the ratio Mg/Si is constant, as proven by the microstructure of the  $\text{Li}_x\text{Mg}_2\text{Si}$  ( $x=0.5$ ) sample presented in Fig. 11, which shows an almost single phase constitution. Therefore a sublattice model  $(\text{Va},\text{Li})_1(\text{Mg})_2(\text{Si})_1$  was selected for that phase. The  $\text{Li}_x\text{Mg}_2\text{Si}$  phase is the only occurrence of ternary solid solubility in a binary phase found in the Li-Mg-Si system.

The solid state equilibria at 200°C in Fig. 22 are partially also supported by the findings of [1992Pav2], noting that instead of " $\text{LiMg}_2\text{Si} + \text{Mg}_2\text{Si}$ " only the single phase range  $\text{Li}_x\text{Mg}_2\text{Si}$  exists. Another difference is that  $\tau_3$  coexists with Li-Si phases whereas a conflicting tie line  $\tau_2 + \tau_1$  was reported by [1992Pav2]. However, the X-ray spectra of these phase assemblies are very complex and interpretation may be inconclusive. In addition, the present thermodynamic modeling had shown that a  $\tau_2 + \tau_1$  tie line could only be modeled with a much lower stability of  $\tau_3$ , resulting in a loss of the key equilibrium  $\tau_3 + (\text{Mg})$ . This  $\tau_3 + (\text{Mg})$  equilibrium is firmly established by the XRD analysis of slowly cooled sample "f", Table 1, the microstructure of the as-cast sample, Fig. 18, and the secondary DTA effect at  $U_7$ , Fig. 15. It could be even noted from Fig. 15 or the sequence of Figs. 20 to 22 that in sample "f" the amount of  $\tau_3$  should increase during cooling from 600°C to 200°C while the amount of  $\text{Li}_x\text{Mg}_2\text{Si}$  decreases.

Whereas the phase  $\tau_3$  in sample "f" is essentially formed from the liquid phase, this is not the case for sample "h". Solidification of "h" is completed at 620°C, producing  $(\text{Mg}) + \text{Li}_x\text{Mg}_2\text{Si}$ , the phases actually found in that sample as calculated in Fig. 16. However, the calculated phase equilibria indicate a low temperature precipitation of  $\tau_3$  at the expense of  $\text{Li}_x\text{Mg}_2\text{Si}$  in the range 325 to 219°C for alloy "h". This shift of the three-phase equilibrium  $(\text{Mg}) + \text{Li}_x\text{Mg}_2\text{Si} + \tau_3$  to higher Mg-composition is clearly seen in Figs. 21 and 22. This solid state transformation is probably too slow to occur in the about 100 minutes of the DTA

experiment in that range. This is the only disagreement of the calculated 200°C isotherm with the observed phases in any of the samples.

In order to discuss the DTA results, especially the secondary and higher effects following the primary solidification, it is instructive to closer examine Fig. 12. The vertical line at 25 at.% Mg, which might be mistaken as the single phase line compound  $\tau_3$ , is actually composed of densely packed multiphase equilibria. In the upper part it is the  $L + \tau_3 + \text{Li}_x\text{Mg}_2\text{Si}$  equilibrium. This is the reason why this line ends at 968°C and does not touch the liquidus line. This maximum corresponds to  $e_1$  on the eutectic line between  $\tau_3$  and  $\text{Li}_x\text{Mg}_2\text{Si}$ , given in Fig. 19. That is, the vertical section in Fig. 12 does not cut exactly through the stoichiometry of  $\tau_3$  but at a slightly lower Li-content. This shift also applies to sample "c", within the 1 mass% weight loss accuracy. This is seen by the second DTA signal at 948°C, Table 3 and Fig. 12, which in this temperature range could be associated only with entering the  $L + \tau_3 + \text{Li}_x\text{Mg}_2\text{Si}$  equilibrium, and also by the third signal at 551°C where the trace amount of residual liquid solidifies in the probably delayed reaction U7,  $L + \text{Li}_x\text{Mg}_2\text{Si} \leftrightarrow \tau_3 + (\text{Mg})$ , calculated and present in Fig. 12. This interpretation of DTA data is clearly supported by the XRD analysis of sample "c" showing mainly  $\tau_3$  with traces of  $\text{Li}_x\text{Mg}_2\text{Si}$  and (Mg), see Table 1. This example also shows that a slightly off-stoichiometric sample can convey more information, if linked to a thermodynamic modeling, than a straight  $\tau_3$  sample, which would have shown simply the congruent melting point.

The history of sample "a", plotted in Fig. 12, is much more straightforward to follow and detailed in Table 3. This sample is composed essentially of  $\tau_1$  with traces of  $\tau_3$ , left over from an incomplete peritectic reaction close to  $p_1$ , see Table 1. The minute amount of (Si), expected to be produced in the final transition type reaction U<sub>2</sub>, could not be detected by XRD.

Following this detailed example it becomes evident that also for the samples "b" to "h" the interpretation of the DTA signals and the phases identified is supported consistently by the calculated phase equilibria in the vertical sections, Figs. 13 to 16, the liquidus surface and the isothermal sections in Figs. 19 to 22. It would be virtually impossible to understand quantitatively and consistently the solidification and melting behavior of these samples without the calculated phase diagram. This is also important for the practical application to a preparation of the intermetallic phases with high purity. In order to control trace amounts of foreign phases, the entire ternary phase diagram has to be known.

The slight off-stoichiometry is also the reason why the pack of vertical lines in Fig. 13 at 25 at.% Mg does not extend up to the congruent melting point of  $\tau_3$ . Again, entering the  $L + \text{Li}_x\text{Mg}_2\text{Si} + \tau_3$  field results in the second thermal effect experienced by sample "c".

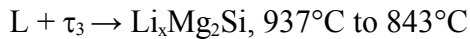
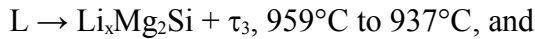
The attempts to model the  $\text{Li}_x\text{Mg}_2\text{Si}$  solution phase according to the rather high melting point of sample "d" in Fig. 14 produced a too high and too large liquidus surface of  $\text{Li}_x\text{Mg}_2\text{Si}$  and unreliable phase transformations and solid state equilibria in the Mg-rich corner. It was considered more important to meet the liquidus points in the Mg-rich region, Figs. 15 and 16, where the additional agreement with the secondary DTA effects provides an important check of the overall consistency of the data.

Figure 14 displays a sharp corner in the phase boundary  $L + \text{Li}_x\text{Mg}_2\text{Si} / L + \text{Li}_x\text{Mg}_2\text{Si} + \tau_3$  around 953°C and 54 at.% Mg. One might expect a solidus line of  $\text{Li}_x\text{Mg}_2\text{Si}$  extending from around that point to the melting point of pure  $\text{Mg}_2\text{Si}$ . However, this line exists only on the exact stoichiometric section Li-Mg<sub>2</sub>Si. The section in Fig. 14 ends at the slightly more Mg-rich point  $\text{Mg}_{66.7}\text{Si}_{33.3}$  and therefore no solidus line can exist. The  $L + \text{Li}_x\text{Mg}_2\text{Si}$  field exists well below 953°C with a very small amount of residual liquid until the extremely narrow  $L + \text{Li}_x\text{Mg}_2\text{Si} + (\text{Mg})$  equilibrium, where the second DTA effect of sample "e" occurs and the small amount of (Mg) precipitates, seen in Fig. 11 and also by XRD.

It is interesting to note that the  $L + \text{Li}_x\text{Mg}_2\text{Si} / L + \text{Li}_x\text{Mg}_2\text{Si} + \tau_3$  phase boundary below the sharp corner moves backwards to lower Mg-content. That means that the reaction type of



solidification must change gradually from eutectic,  $L \rightarrow Li_xMg_2Si + \tau_3$ , to peritectic,  $L + \tau_3 \rightarrow Li_xMg_2Si$ , in that region. This is verified by the solidification path of an alloy on the section in Fig. 14, just a little left of that corner. Let us follow the alloy with 53.3 at.% Mg, 20.09 at.% Li and 26.61 at.% Si, that enters the three phase field at 959°C and leaves it again at 843°C. At both ends the amount of  $\tau_3$  is zero, so it must have a maximum in between. Indeed, the calculation shows this maximum at 937°C with a molar phase fraction of 0.013 for  $\tau_3$ . It also shows the monotonic growth of  $Li_xMg_2Si$  and consumption of L during cooling from 959 to 843°C. Thus, if we place the consumed phases to the left and the growing phases to the right of the arrow, we have the reactions



for the selected alloy. The solidification continues with  $L \rightarrow Li_xMg_2Si$ , 843 to 606°C.

This is a nice real example of the intricacies involved in gradually changing reaction types, discussed in general terms by Hillert [1998Hil]. Specifically, it is *not* decisive to look if an extended line of a tangent to the monovariant line  $e_1$  in Fig. 19 crosses between the compositions of  $\tau_3$  and  $Li_xMg_2Si$ . The transition for the alloy with 53.3 at.% Mg discussed above occurs at 937°C with a liquid composition of 50 at.% Mg along line  $e_1$ . Here, the classical textbook criterion of the tangent gives the wrong impression of an ongoing eutectic type reaction  $e_1$ . The transition point also depends on alloy composition. For sample "d" on Fig. 14 with 50 at.% Mg the maximum of  $\tau_3$  production occurs at 758°C, corresponding to a liquid composition of 72 at.% Mg along line  $e_1$  in Fig. 19. Again, at this point the plotted tangent crosses between the compositions of  $\tau_3$  and  $Li_xMg_2Si$ , giving no indication for the actually changing reaction type.

The reason for the failure of the classical tangent criterion is that the  $Li_xMg_2Si$  *solid composition also moves*. Therefore, the eutectic/peritectic transition also depends on the overall alloy composition in the three-phase field and may occur at different temperatures. The only practical way to detect the transition is to calculate the solidification path and phase amounts for a given alloy. Only if both solid phase compositions are fixed does the classical tangent criterion hold true for this transition.

## 8 Conclusion

The thermodynamic parameters for the binary Mg-Si subsystem were remodeled in order to avoid an artificial inverted liquid miscibility gap at higher temperature. This was necessary to obtain data that could be reliably extrapolated to various temperatures and into the ternary system.

Using XRD, optical metallography and DTA three ternary phases were confirmed:  $\tau_1$  ( $Li_8MgSi_6$ ),  $\tau_2$  ( $Li_{12}Mg_3Si_4$ ), and  $\tau_3$  ( $Li_2MgSi$ ). The  $LiMg_2Si$  phase reported in [1992Pav2] is not a separate phase but the interstitial solid solution of Li in the binary  $Mg_2Si$  phase,  $Li_xMg_2Si$  at the maximum  $x \approx 0.91 \nabla 0.05$ . Ternary liquidus data and phase transformations were also measured.

A thermodynamic assessment of the ternary Li-Mg-Si system was worked out in parallel to the experimental study and used to select the relatively small number of our key experiments. The final consistent thermodynamic model is well supported by the present experimental data and the published phase relations at 200°C [1992Pav2]. The three solution phases liquid, (Mg) and (Li) are sufficiently described by extrapolations of their binary thermodynamic models without ternary interactions. Only the three ternary phases and the  $Li_xMg_2Si$  solution had to be modeled.

Solidification and phase transformations occurring in samples slightly off the stoichiometry of the ternary intermetallic phases are rather intricate. It is demonstrated that this intricate behavior can be quantitatively understood using a number of calculated ternary phase diagram sections and invariant reactions. This knowledge may be also important in the processing of these intermetallic phases and the control of trace amounts of foreign phases.

It is also shown that the gradual change from eutectic,  $L \rightarrow Li_xMg_2Si + \tau_3$ , to peritectic,  $L + \tau_3 \rightarrow Li_xMg_2Si$ , monovariant reaction type transition depends on the overall alloy composition in the three-phase field and may occur at different temperatures. The classical tangent criterion fails, since not only the liquid but also the  $Li_xMg_2Si$  solid composition moves with temperature.

If lithium is added to magnesium alloys containing small amounts of Si, it dissolves at a higher fraction in the  $Mg_2Si$  phase compared to the (Mg) matrix. At higher lithium addition the ternary phase  $\tau_3$  ( $Li_2MgSi$ ) starts forming.

### Acknowledgment

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## **Figure captions:**

Fig. 1. Calculated phase diagram of the Li-Mg system using parameters of [1990Sau]

Fig. 2. Calculated phase diagram of the Li-Si system using parameters of [1995Bra]

Fig. 3. Calculated phase diagram of the Mg-Si system using parameters of [1997Feu], producing an unrealistic liquid miscibility gap

Fig. 4. Calculated phase diagram of the Mg-Si system using parameters of [2000Yan], producing an unrealistic liquid miscibility gap

Fig. 5. Calculated phase diagram of the Mg-Si system (this work). The unrealistic inverted liquid miscibility gap at higher temperature does not occur, even if calculating beyond 4000° C.

Fig. 6. Calculated Mg-rich side of the Mg-Si phase diagram (this work)

Fig. 7. Activity of Mg in liquid Mg-Si alloy at 1077°C referred to Mg(l)

Fig. 8. Enthalpy of the liquid phase at 1077°C, referred to Mg(l) and Si(l)

Fig. 9. Partial enthalpy of solution of Si in the liquid phase at 1077°C, referred to Si(l)

Fig. 10. Calculated isothermal section of the Li-Mg-Si phase diagram at 200°C; details of the investigated samples are given in Table 1; details of phase fields are given in Fig. 22.

Fig. 11. Microstructure of the as-cast sample “e” with the composition  $\text{Li}_{14}\text{Mg}_{58}\text{Si}_{28}$  showing the  $\text{Li}_x\text{Mg}_2\text{Si}$  solid solution (grey) and small amount of (Mg) (light) in agreement with phase equilibria of Fig. 10.

Fig. 12. Calculated polythermal section compared to the DTA measurements for samples “a” and “c”. The section deviates slightly from stoichiometric compositions at  $\tau_1$  and  $\tau_3$ .

Fig. 13. Calculated polythermal section compared to the DTA measurements for samples “b” and “c”. The section deviates slightly from stoichiometric compositions at  $\tau_2$  and  $\tau_3$ .

Fig. 14. Calculated polythermal section compared to the DTA measurements for samples “d” and “e”. This section is slightly more Mg-rich than the section Li-Mg<sub>2</sub>Si.

Fig. 15. Calculated partial polythermal section of the Li-Mg-Si system at 10 at.% Si compared to the DTA measurements for samples “f” and “g”.

Fig. 16. Calculated partial polythermal section of the Li-Mg-Si system at 8 at.% Li compared to the DTA measurements for sample “h”.

Fig. 17. Microstructure of Mg<sub>80</sub>Li<sub>10</sub>Si<sub>10</sub> as-cast sample “g” after 20 h on dry air

Fig. 18. Microstructure of Mg<sub>70</sub>Li<sub>20</sub>Si<sub>10</sub> as-cast sample “f” after 20 h on dry air

Fig. 19. Li-Mg-Si phase diagram: calculated liquidus surface. Invariant reactions and fields of primary crystallization are marked.

Fig. 20. Calculated isothermal section of Li-Mg-Si phase diagram at 600°C

Fig. 21. Calculated isothermal section of Li-Mg-Si phase diagram at 400°C

Fig. 22. Calculated isothermal section of Li-Mg-Si phase diagram at 200°C

Table 1. Sample compositions and identified phases.

Sample No.	Composition [at.%]			Identified phases after DTA heat treatment of 1 K/min*
	Li	Mg	Si	
a	53.3	6.7	40	$\tau_1 + [(\tau_3)]$
b	63	16	21	$\tau_2 + [(Li)] + ?$
c	50	25	25	$\tau_3 + [Li_xMg_2Si] + [(Mg)]$
d	25	50	25	$Li_xMg_2Si + [(Mg)] + [\tau_3]$
e	14	58	28	$Li_xMg_2Si + [(Mg)]$
f	20	70	10	$(Mg) + Li_xMg_2Si + \tau_3$
g	10	80	10	$(Mg) + Li_xMg_2Si$
h	8	90	2	$(Mg) + Li_xMg_2Si$

\*- Sequence indicates the amount of phases. Square brackets [] show a very small amount of a phase

Table 2. Accepted ternary solid phases of the Li-Mg-Si system.

Phase / stability range	Structure type	Pearson symbol	Space group	Lattice parameters, nm			Ref.
				a	b	c	
$\tau_1, Li_8MgSi_6$ < 683°C	$Li_8MgSi_6$	mP96	$P2_1/m$	1.2701	0.4347	1.0507 $\gamma=107.58^\circ$	1986Nes a)
$\tau_2, Li_{12}Mg_3Si_4$ < 674°C	$Li_{12}Mg_3Si_4$	cI76	$I\bar{4}3d$	1.0688			1992Pav1 1992Pav2 a)
$\tau_3, Li_2MgSi$ < 995°C	$CuHg_2Ti$	cF16	$F\bar{4}3m$	0.637			1992Pav2 a)
$Li_xMg_2Si$ < 1081°C x = 0 to 0.91	$MnCu_2Al$	cF16	$F4\bar{3}m$	0.635 to 0.638			this work

a) The lattice parameters of the ternary phases were confirmed in this work. The temperature limits were determined in this work both experimentally and by calculation.

Table 3. DTA measurements compared to thermodynamic calculations

Sample No.	Heating rate [K/min]	DTA signals heating <sup>a)</sup> [°C]	DTA signals cooling <sup>a)</sup> [°C]	Assessed temp. <sup>b)</sup> [°C]	Calc. temp. [°C]	Phase limits <sup>c)</sup> or invariant reactions
„a“	5	m811	o811	811	837	L/L+ $\tau_3$
	5		o687	688	683	p <sub>1</sub> : L+ $\tau_3$ = $\tau_1$
	1		o689 o688			
	5	o684	o 661	679	679	U <sub>2</sub> : L+ $\tau_3$ = $\tau_1$ +(Si)
	1	o679 o678	o 664 o 664			
„b“	5	m654	o630	644	674	? L+ $\tau_3$ / L+ $\tau_3$ + $\tau_2$
	1	m649 m644	o644 o640			
	5	o452	o443	450	455	U <sub>9</sub> : L+ $\tau_3$ = $\tau_2$ +(Li)
	1	o450 o449	o446 o446			
„c“	5	m996	o990	996	995	L/L+ $\tau_3$
		o948	o947	948	964	L+ $\tau_3$ / L+ Li <sub>x</sub> Mg <sub>2</sub> Si+ $\tau_3$
		m552 m556 m553	o550 o551 o550	551	597	? U <sub>7</sub> : L+ Li <sub>x</sub> Mg <sub>2</sub> Si = $\tau_3$ +(Mg)
„d“	5	m1073	o1062	1067	1023	L/L+Li <sub>x</sub> Mg <sub>2</sub> Si
	1	m1067 m1070	o1064			
	5	o607	o609	608	597	U <sub>7</sub> : L+Li <sub>x</sub> Mg <sub>2</sub> Si = $\tau_3$ +(Mg)
	1	o607 o607 o608	o608 o608 o609			
„e“	5	o1076	o1076	1076	1060	L/L+Li <sub>x</sub> Mg <sub>2</sub> Si
	5	o629	o628	629	629	L+Li <sub>x</sub> Mg <sub>2</sub> Si/ L+Li <sub>x</sub> Mg <sub>2</sub> Si+(Mg)
„f“	5	m902	o892	892	877	L/L+Li <sub>x</sub> Mg <sub>2</sub> Si
	5	o605	o 605	605	597	U <sub>7</sub> : L+ Li <sub>x</sub> Mg <sub>2</sub> Si = $\tau_3$ +(Mg)
		o602	o 603			
		o601	o 604			
1	o598	o 605				
„g“	5	m900	o 896	899	903	L/L+Li <sub>x</sub> Mg <sub>2</sub> Si
	1	m900 m899	o 898 o 899			
	5	o622	o 619	621	623	L+Li <sub>x</sub> Mg <sub>2</sub> Si+(Mg)/ Li <sub>x</sub> Mg <sub>2</sub> Si+(Mg)
	1	o619 o620	o 621 o 621			
„h“	5		o 676	674	692	L/L+Li <sub>x</sub> Mg <sub>2</sub> Si
	1		o 674 o 672			
	5	o618	o 618	617	620	L+(Mg)+Li <sub>x</sub> Mg <sub>2</sub> Si/ (Mg)+Li <sub>x</sub> Mg <sub>2</sub> Si
	1	o613 o613	o 617 o 617			

<sup>a)</sup> m – peak maximum, o – peak onset

<sup>b)</sup> Estimated DTA error:  $\pm 4$  K

<sup>c)</sup> This interpretation of DTA signals is supported by phase analysis

Table 4. The calculated ternary invariant reactions

Reaction	Type	T, °C	Composition of liquid (at.%)		
			Li	Mg	Si
$L \leftrightarrow \tau_3$	congruent	995	50	25	25
$L \leftrightarrow \tau_3 + Li_xMg_2Si$	e <sub>1</sub>	968	37.26	36.91	25.84
$L \leftrightarrow \tau_3 + Li_7Si_3$	e <sub>2</sub>	741	68.85	1.31	29.84
$L \leftrightarrow \tau_3 + Li_{13}Si_4$	e <sub>3</sub>	721	74.59	1.91	23.51
$L \leftrightarrow \tau_3 + Li_{13}Si_4 + Li_7Si_3$	E <sub>1</sub>	719	73.37	1.58	25.04
$L + Li_xMg_2Si \leftrightarrow (Si) + \tau_3$	U <sub>1</sub>	696	49.76	4.96	45.28
$L + \tau_3 \leftrightarrow \tau_1$	p <sub>1</sub>	683	54.06	2.04	43.89
$L + \tau_3 \leftrightarrow \tau_1 + (Si)$	U <sub>2</sub>	679	51.58	3.45	44.97
$L + \tau_3 \leftrightarrow \tau_2$	p <sub>2</sub>	675	79.46	4.40	16.15
$L + \tau_3 \leftrightarrow \tau_2 + Li_{13}Si_4$	U <sub>3</sub>	675	79.47	4.27	16.25
$L + \tau_3 \leftrightarrow Li_7Si_3 + \tau_1$	U <sub>4</sub>	660	60.64	0.76	38.60
$L + Li_7Si_3 \leftrightarrow \tau_1 + Li_{12}Si_7$	U <sub>5</sub>	629	59.52	0.11	40.36
$\tau_3 + (Si) \leftrightarrow \tau_1 + Li_xMg_2Si$	U <sub>6</sub>	608	-	-	-
$L \leftrightarrow \tau_1 + Li_{12}Si_7 + (Si)$	E <sub>2</sub>	604	56.68	0.03	43.29
$L + Li_xMg_2Si \leftrightarrow \tau_3 + (Mg)$	U <sub>7</sub>	597	18.77	80.05	1.18
$L + Li_{13}Si_4 \leftrightarrow \tau_2 + Li_{22}Si_5$	U <sub>8</sub>	592	83.84	5.05	11.11
$L \leftrightarrow \tau_3 + (Li)$	e <sub>4</sub>	584	27.67	71.19	1.13
$L \leftrightarrow \tau_3 + (Mg) + (Li)$	E <sub>3</sub>	583	23.79	75.29	0.91
$L + \tau_3 \leftrightarrow \tau_2 + (Li)$	U <sub>9</sub>	455	62.74	36.12	1.13
$L + \tau_2 \leftrightarrow Li_{22}Si_5 + (Li)$	U <sub>10</sub>	318	80.27	19.21	0.51



Table 5: Thermodynamic parameters assessed in the present work for the binary Mg-Si and ternary Li-Mg-Si systems in (J/mol of atoms or sites), phase descriptions bcc = (Li), hcp = (Mg). The complete dataset of the ternary system may be obtained on request by sending an email to the corresponding author.

$$L_{Mg,Si}^{0,Liquid} = -70055 + 24.98 \cdot T$$

$$L_{Mg,Si}^{1,Liquid} = -1300$$

$$L_{Mg,Si}^{2,Liquid} = +6272$$

$$L_{Mg,Si}^{0,hcp} = -7148.79 + 0.894 \cdot T$$

$$G_{Mg:Si:Va}^{0,LixMg2Si} = -16177.5 + 3.8967 \cdot T + 0.5 \cdot G_{Mg}^{0,hcp} + 0.25 \cdot G_{Si}^{0,diamond}$$

$$G_{Mg:Si:Li}^{0,LixMg2Si} = -20000 + 0.5 \cdot G_{Mg}^{0,hcp} + 0.25 \cdot G_{Si}^{0,diamond} + 0.25 \cdot G_{Li}^{0,bcc}$$

$$G_{Li:Mg:Si}^{0,Li2MgSi} = -25000 + 0.05 \cdot T + 0.5 \cdot G_{Li}^{0,bcc} + 0.25 \cdot G_{Mg}^{0,hcp} + 0.25 \cdot G_{Si}^{0,diamond}$$

$$G_{Li:Mg:Si}^{0,Li12Mg3Si4} = -23500 + 2.2 \cdot T + 0.631579 \cdot G_{Li}^{0,bcc} + 0.157895 \cdot G_{Mg}^{0,hcp} + 0.210526 \cdot G_{Si}^{0,diamond}$$

$$G_{Li:Mg:Si}^{0,Li8MgSi6} = -25000 + 4.2 \cdot T + 0.533333 \cdot G_{Li}^{0,bcc} + 0.066667 \cdot G_{Mg}^{0,hcp} + 0.4 \cdot G_{Si}^{0,diamond}$$

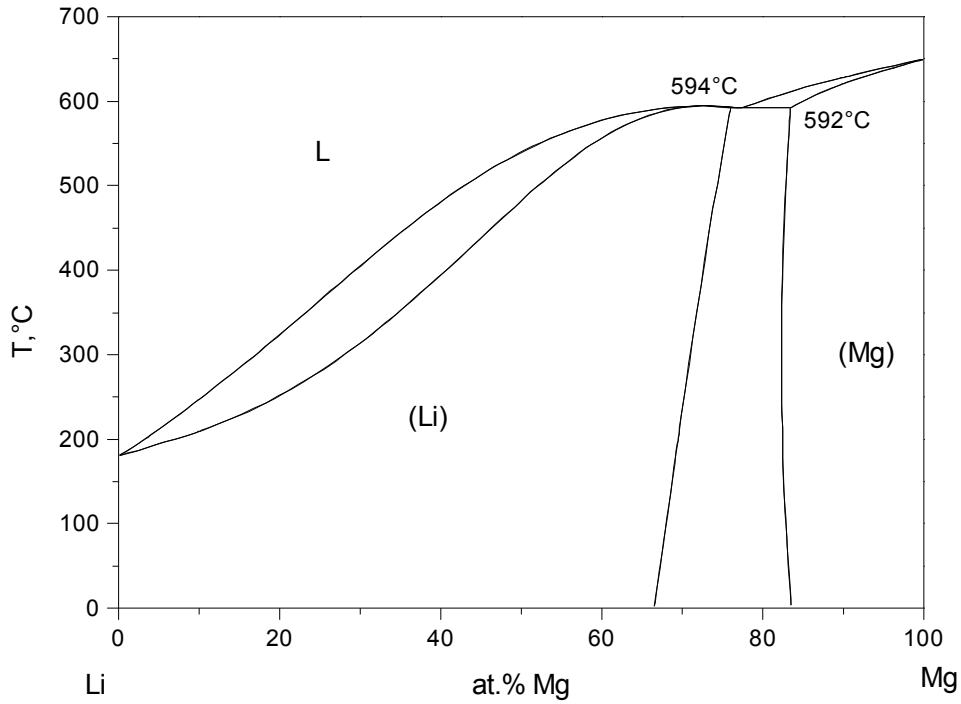


Fig. 1. Calculated phase diagram of the Li-Mg system using parameters of [1990Sau]

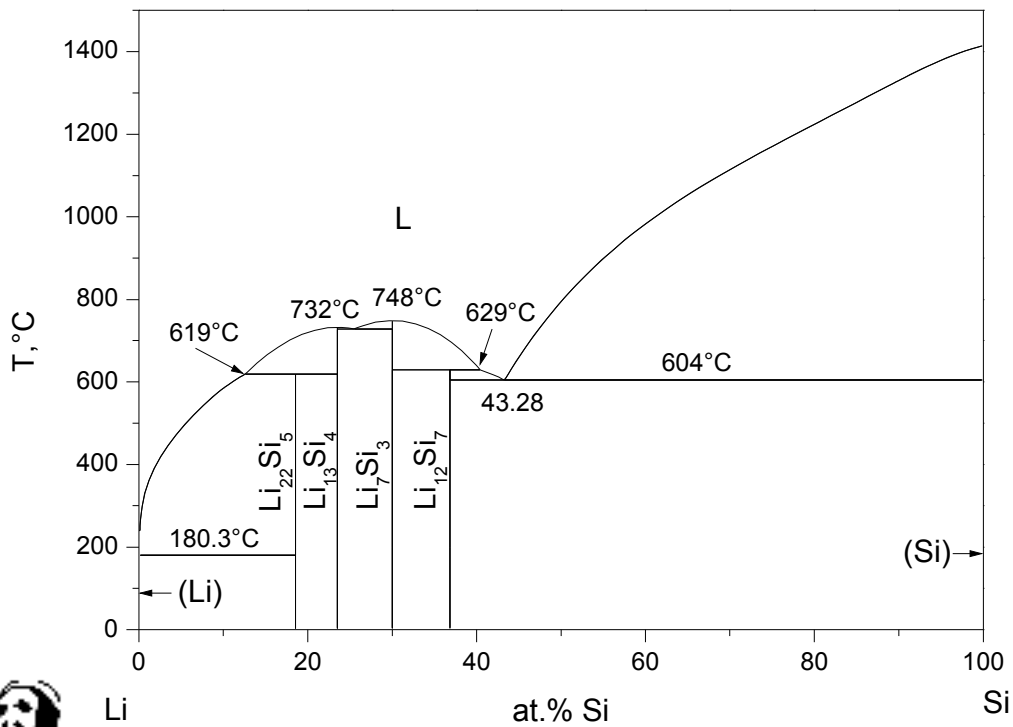


Fig. 2. Calculated phase diagram of the Li-Si system using parameters of [1995Bra]

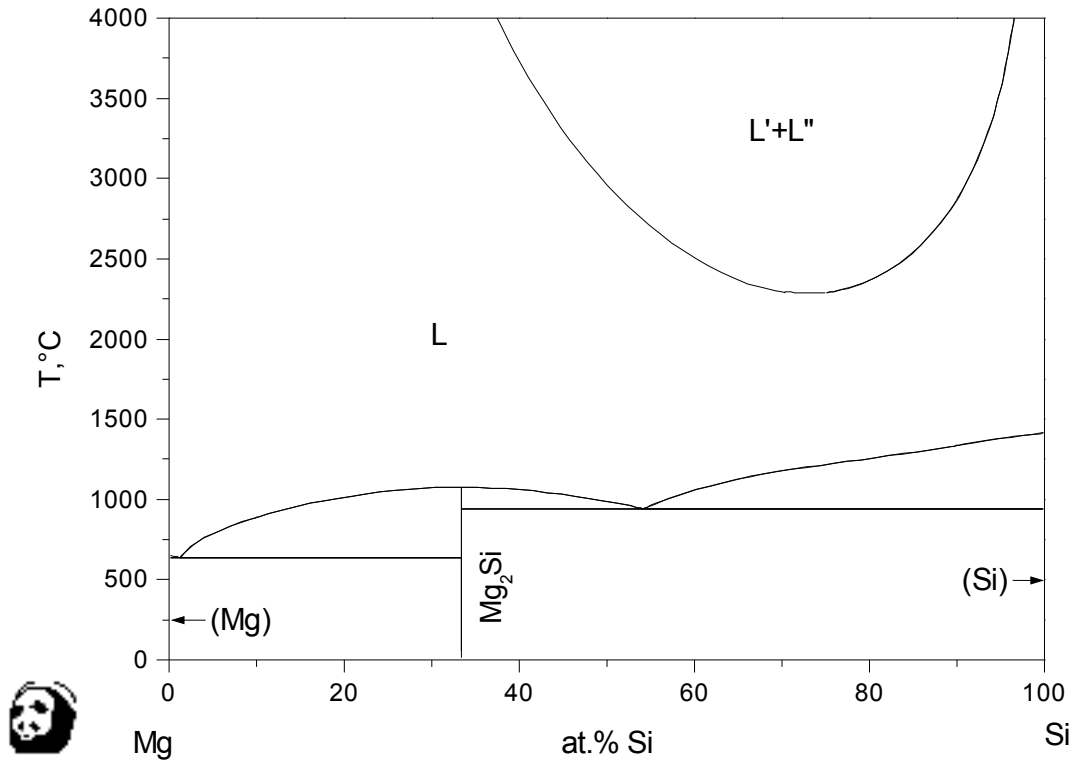


Fig. 3. Calculated phase diagram of the Mg-Si system using parameters of [1997Feu], producing an unrealistic liquid miscibility gap

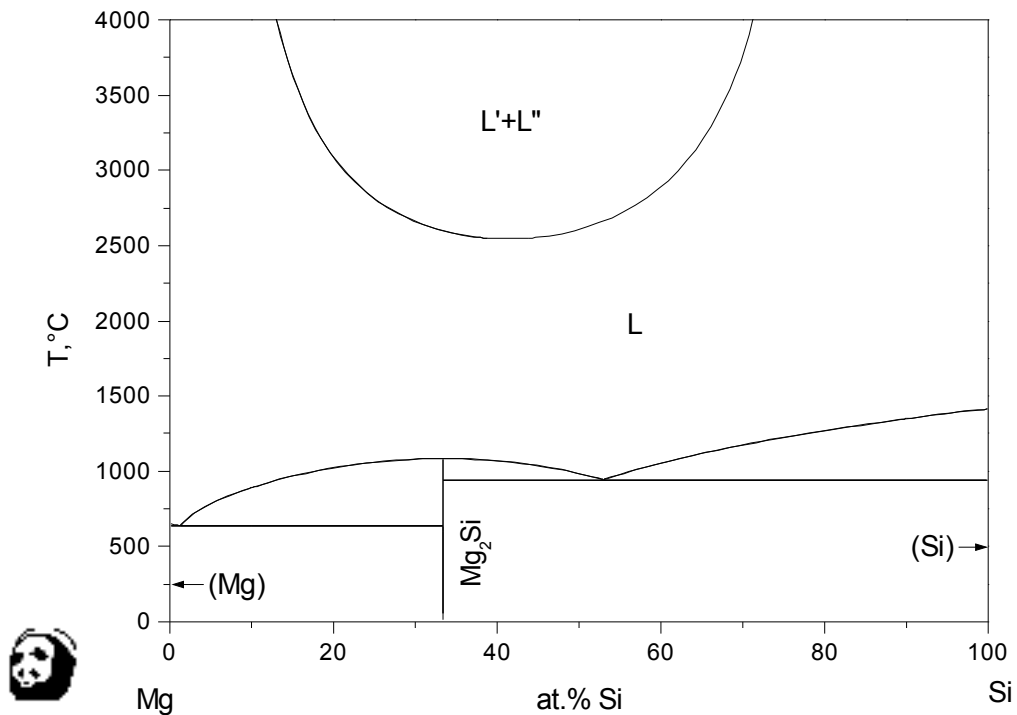


Fig. 4. Calculated phase diagram of the Mg-Si system using parameters of [2000Yan], producing an unrealistic liquid miscibility gap

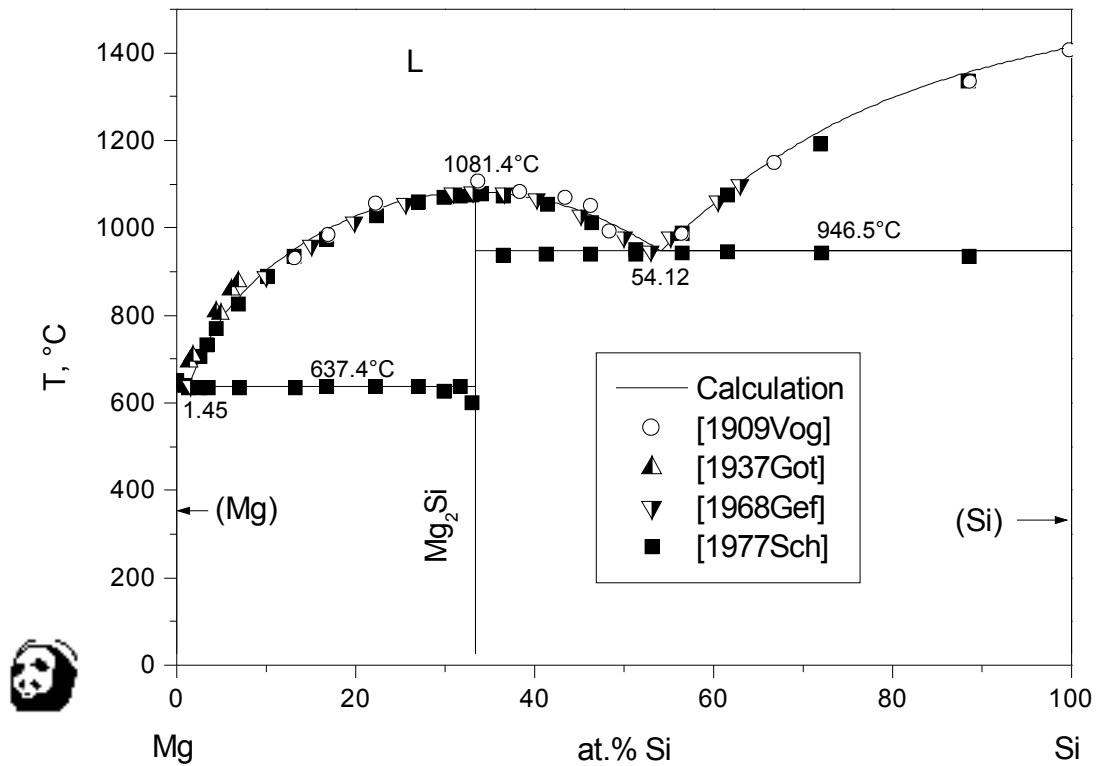


Fig. 5. Calculated phase diagram of the Mg-Si system (this work). The unrealistic inverted liquid miscibility gap at higher temperature does not occur, even if calculating beyond  $4000^{\circ}\text{C}$ .

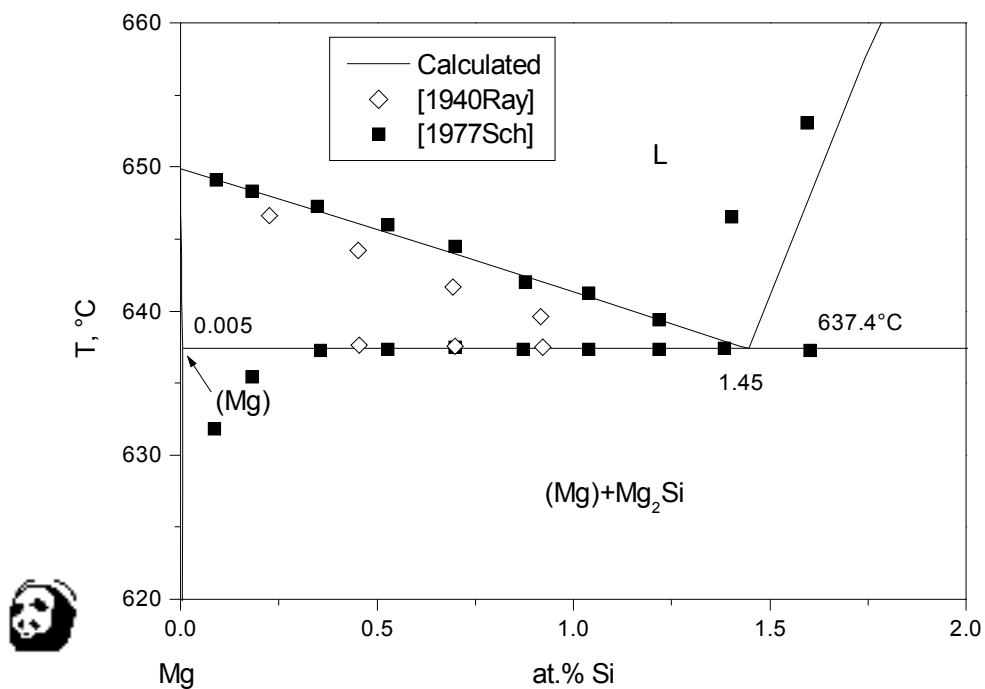


Fig. 6. Calculated Mg-rich side of the Mg-Si phase diagram (this work)

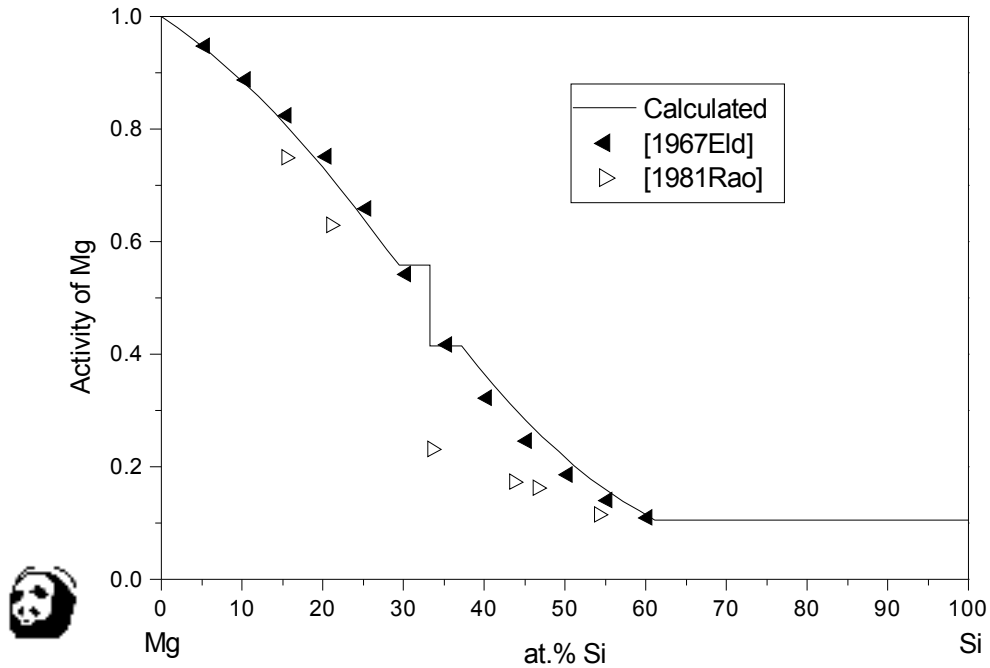


Fig. 7. Activity of Mg in liquid Mg-Si alloy at 1077°C referred to Mg(l)

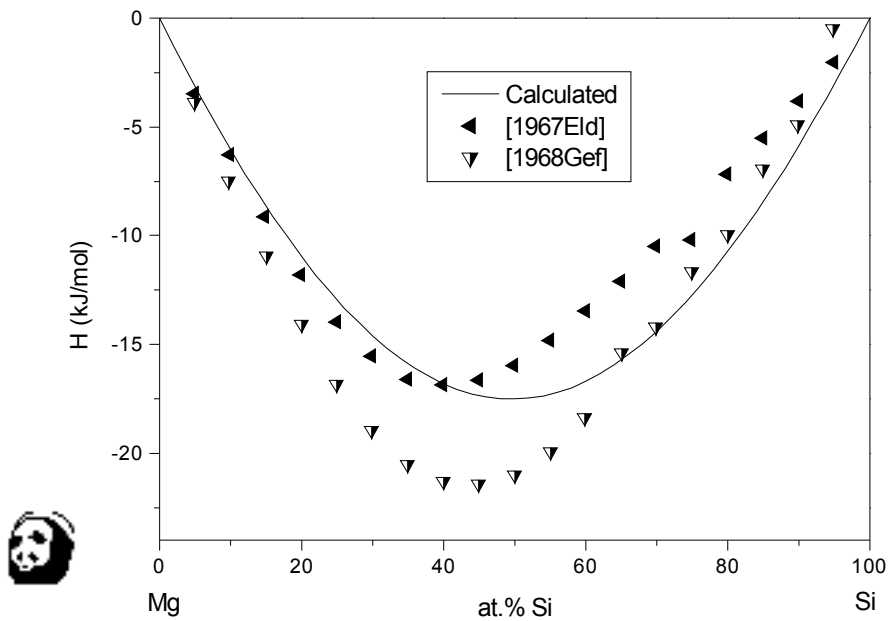


Fig. 8. Enthalpy of the liquid phase at 1077°C, referred to Mg(l) and Si(l)

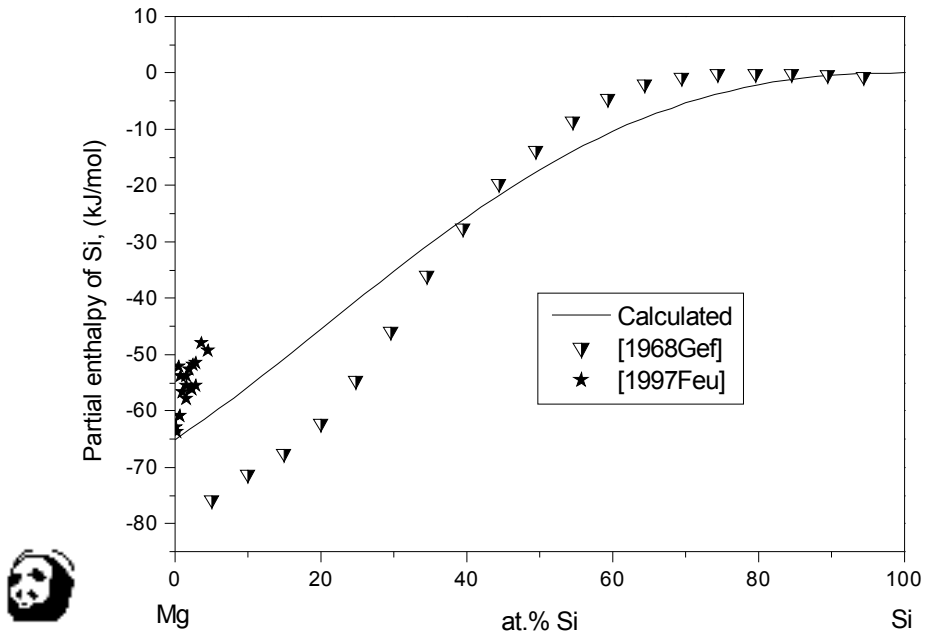


Fig. 9. Partial enthalpy of solution of Si in the liquid phase at 1077°C, referred to Si(l)

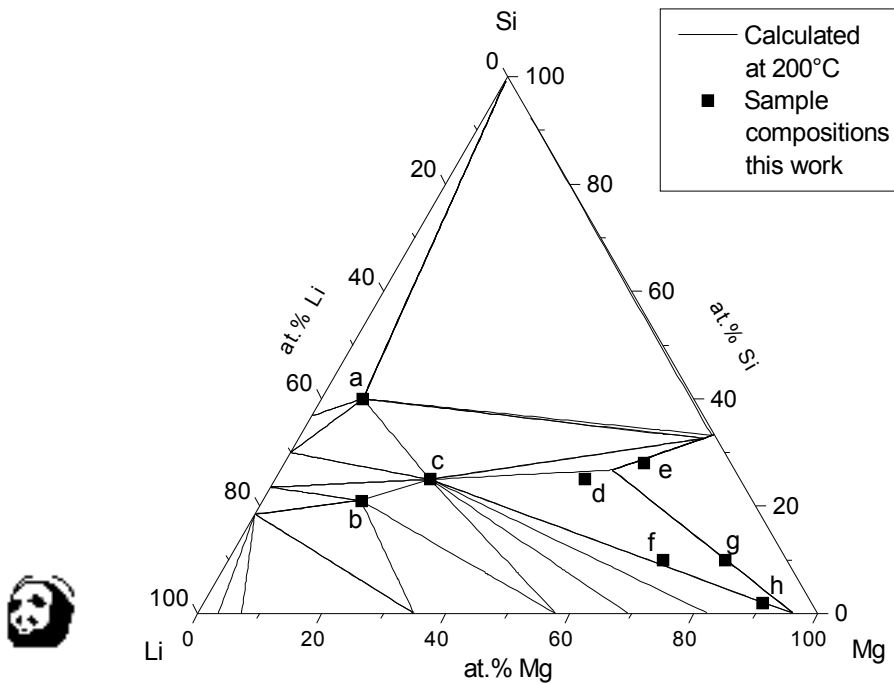


Fig. 10. Calculated isothermal section of the Li-Mg-Si phase diagram at 200°C; details of the investigated samples are given in Table 1; details of phase fields are given in Fig. 22.

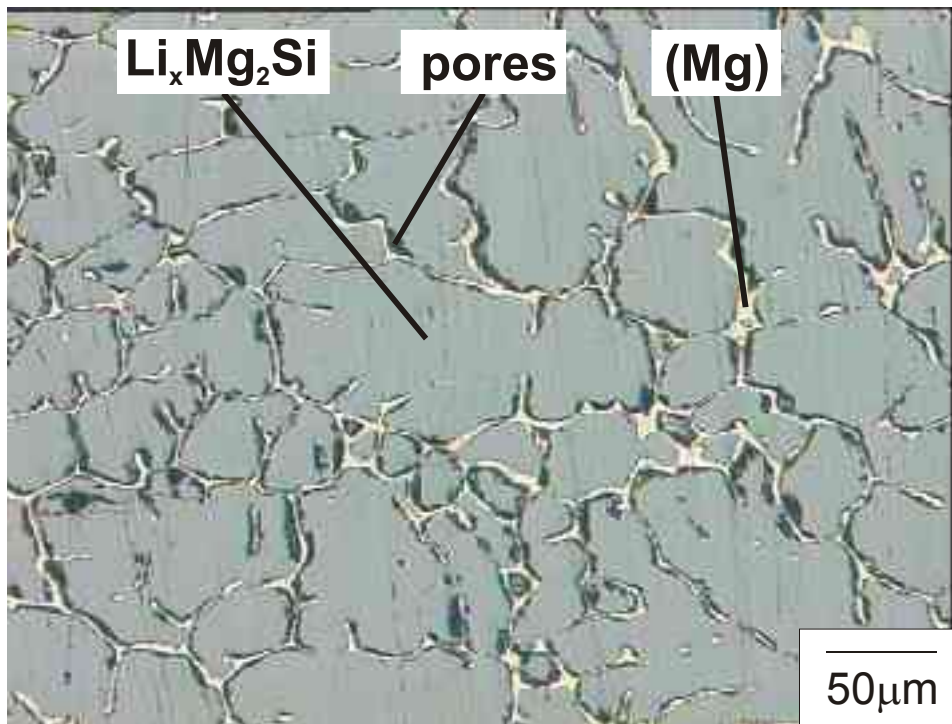


Fig. 11. Microstructure of the as-cast sample “e” with the composition  $\text{Li}_{14}\text{Mg}_{58}\text{Si}_{28}$  showing the  $\text{Li}_x\text{Mg}_2\text{Si}$  solid solution (grey) and small amount of (Mg) (light) in agreement with phase equilibria of Fig. 10.

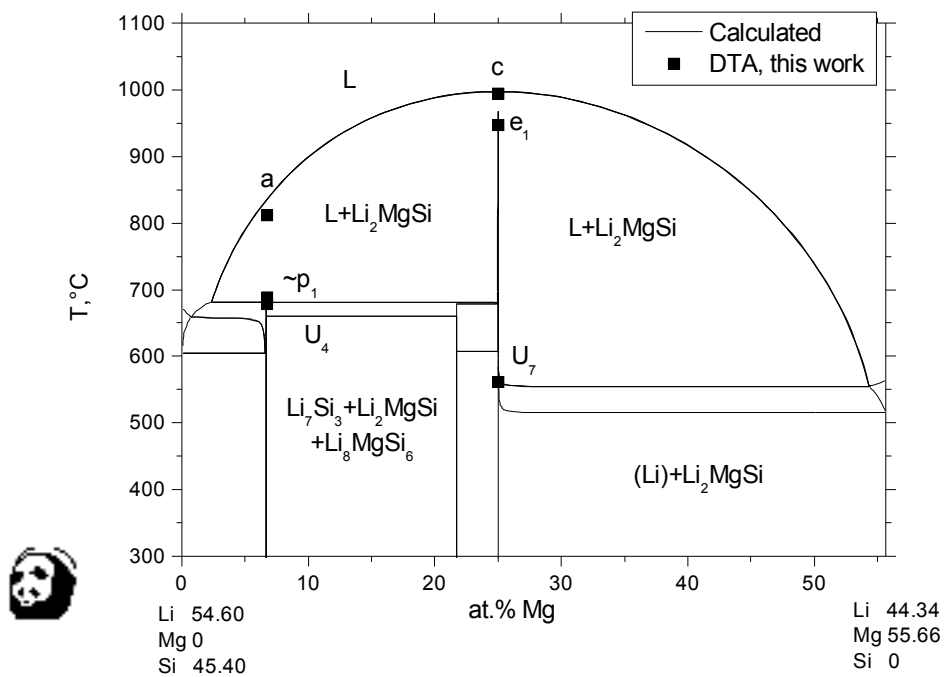


Fig. 12. Calculated polythermal section compared to the DTA measurements for samples “a” and “c”. The section deviates slightly from stoichiometric compositions at  $\tau_1$  and  $\tau_3$ .

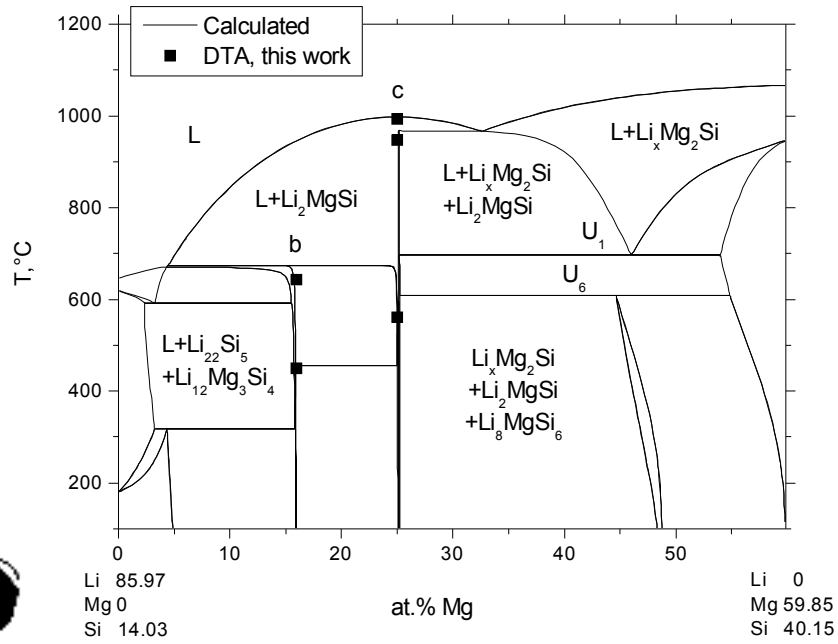


Fig. 13. Calculated polythermal section compared to the DTA measurements for samples “b” and “c”. The section deviates slightly from stoichiometric compositions at  $\tau_2$  and  $\tau_3$ .

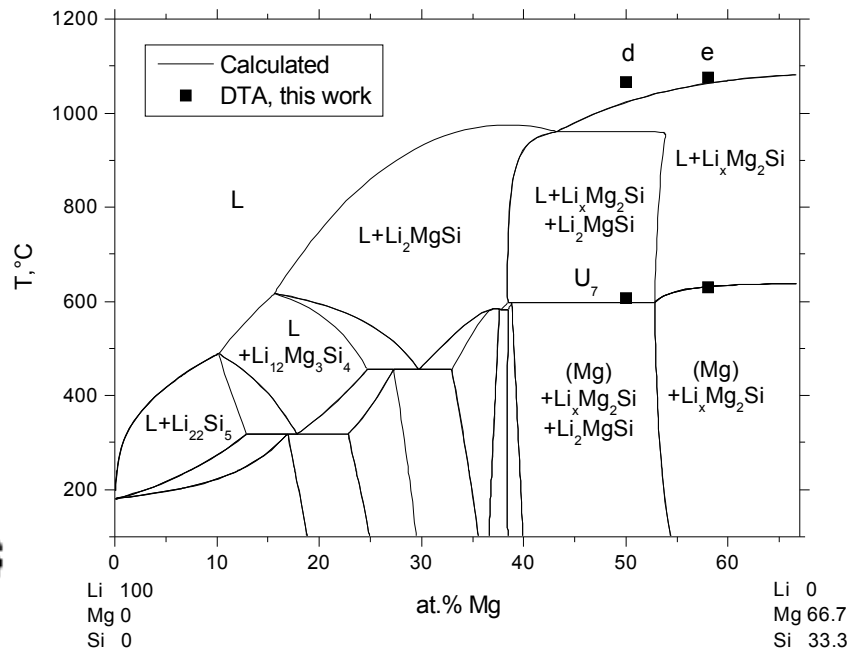


Fig. 14. Calculated polythermal section compared to the DTA measurements for samples “d” and “e”. This section is slightly more Mg-rich than the section Li-Mg<sub>2</sub>Si.



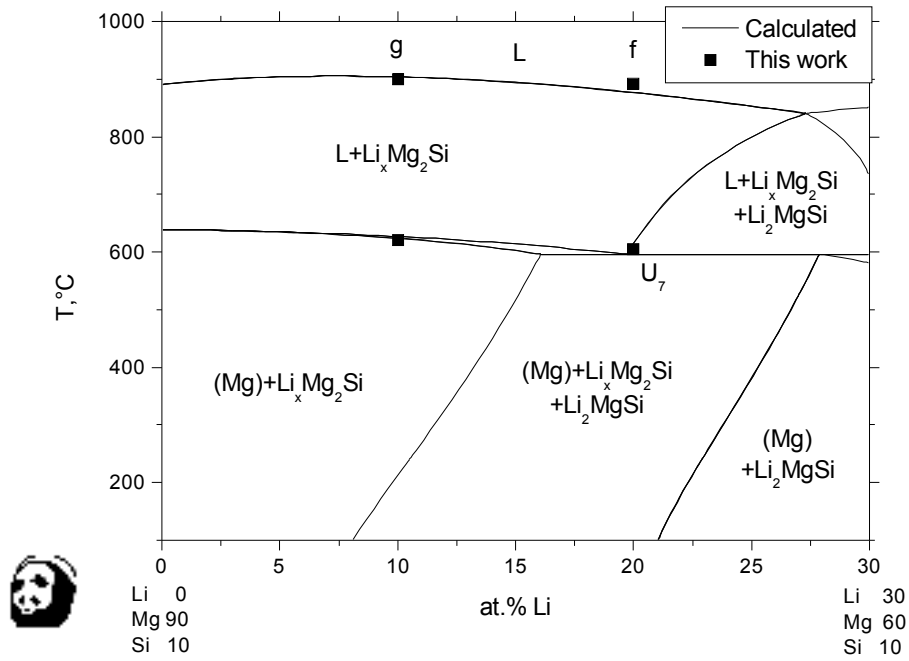


Fig. 15. Calculated partial polythermal section of the Li-Mg-Si system at 10 at.% Si compared to the DTA measurements for samples “f” and “g”.

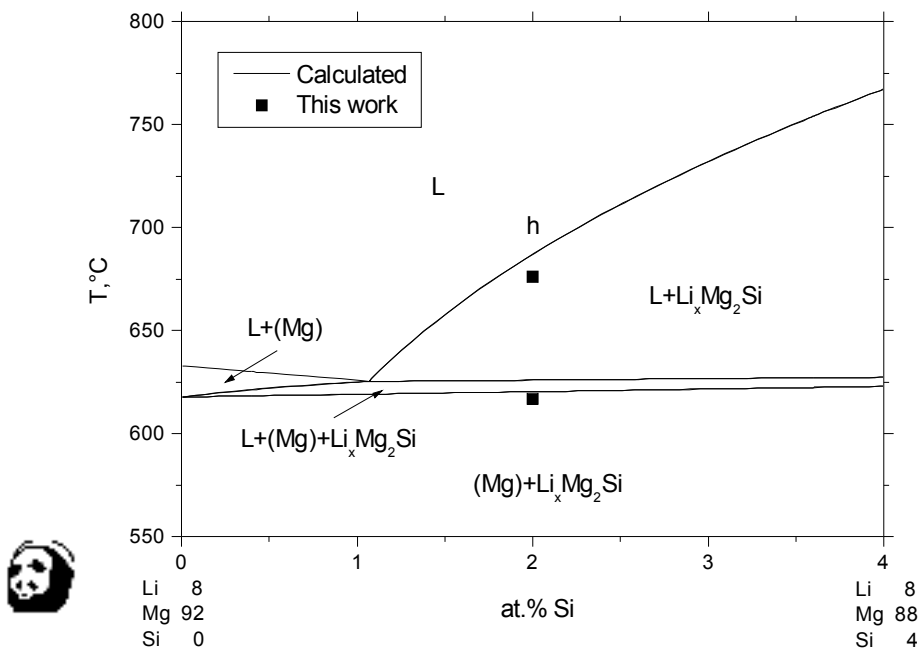


Fig. 16. Calculated partial polythermal section of the Li-Mg-Si system at 8 at.% Li compared to the DTA measurements for sample “h”.

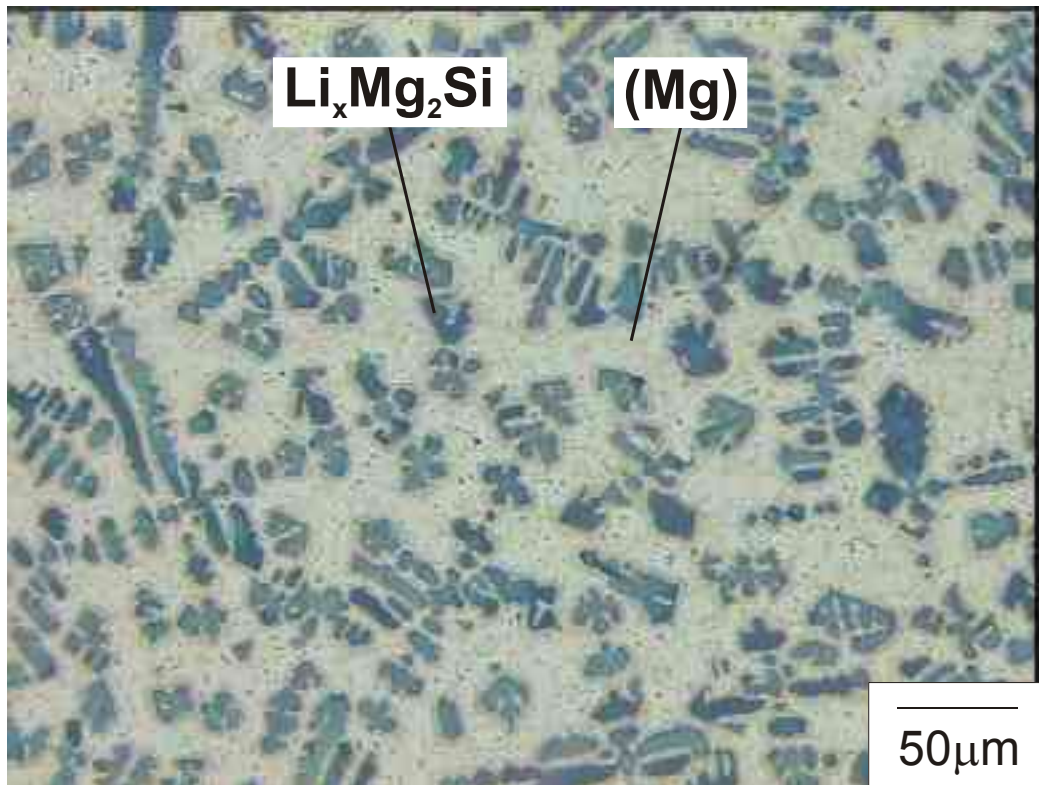


Fig. 17. Microstructure of Mg<sub>80</sub>Li<sub>10</sub>Si<sub>10</sub> as-cast sample "g" after 20 h on dry air

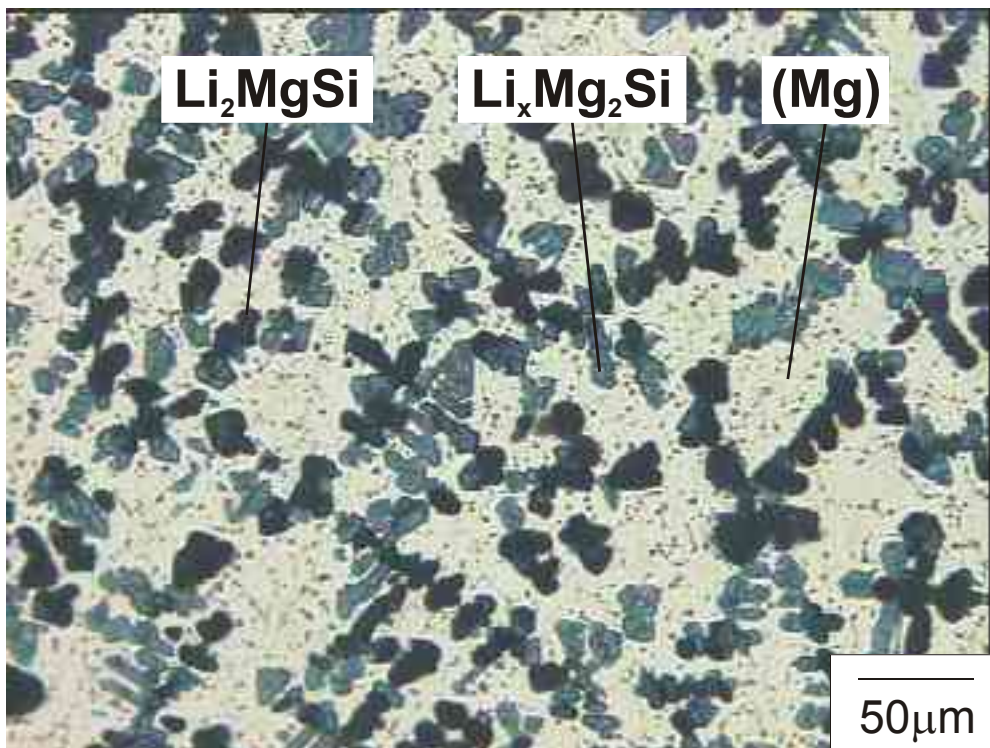


Fig. 18. Microstructure of Mg<sub>70</sub>Li<sub>20</sub>Si<sub>10</sub> as-cast sample "f" after 20 h on dry air

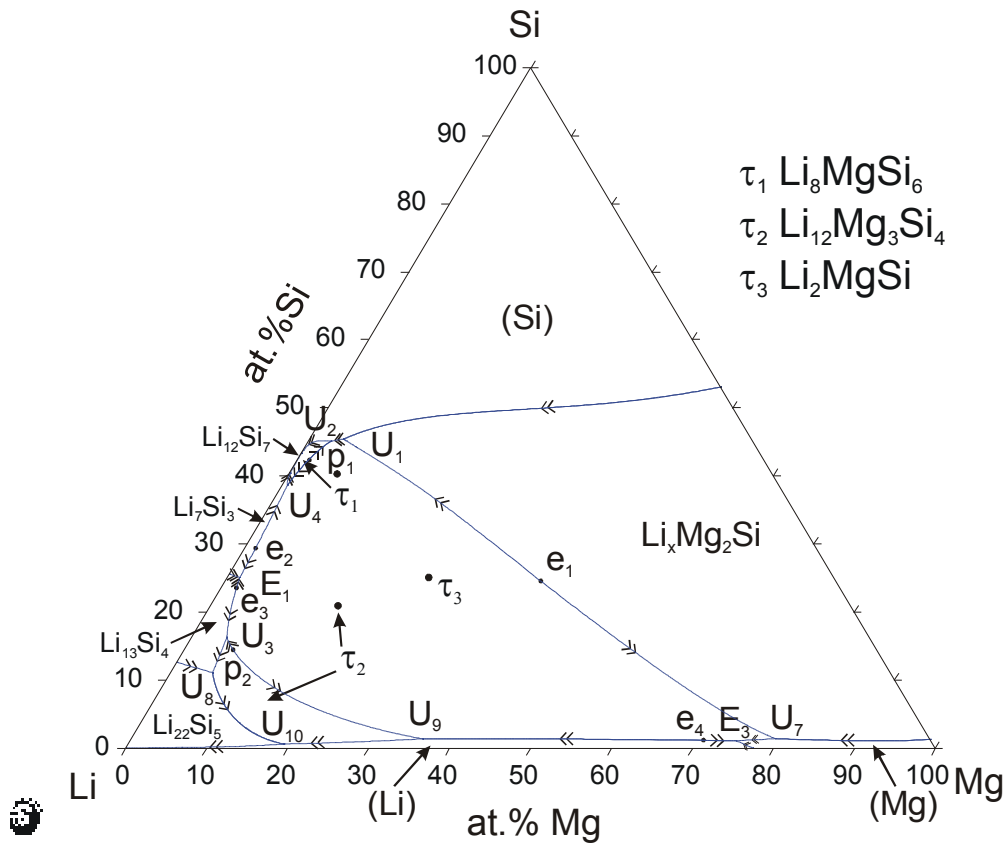


Fig. 19. Li-Mg-Si phase diagram: calculated liquidus surface. Invariant reactions and fields of primary crystallization are marked.

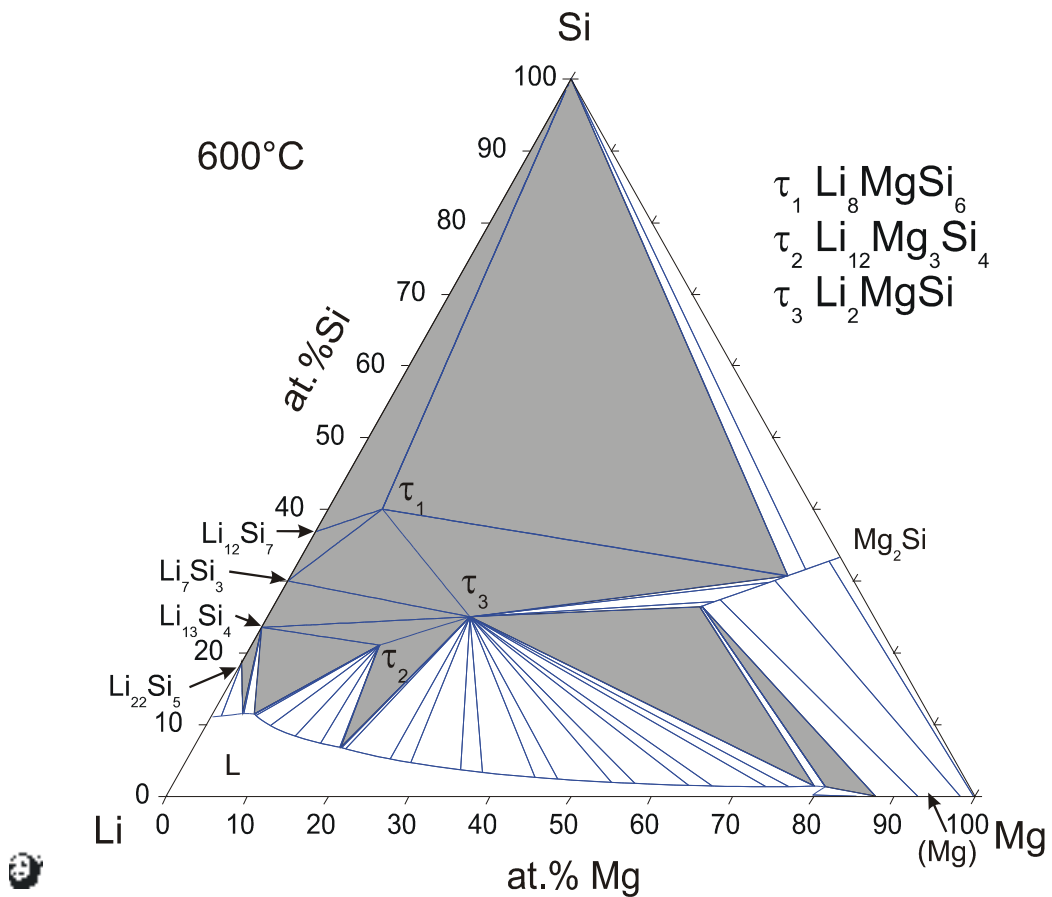


Fig. 20. Calculated isothermal section of Li-Mg-Si phase diagram at 600°C

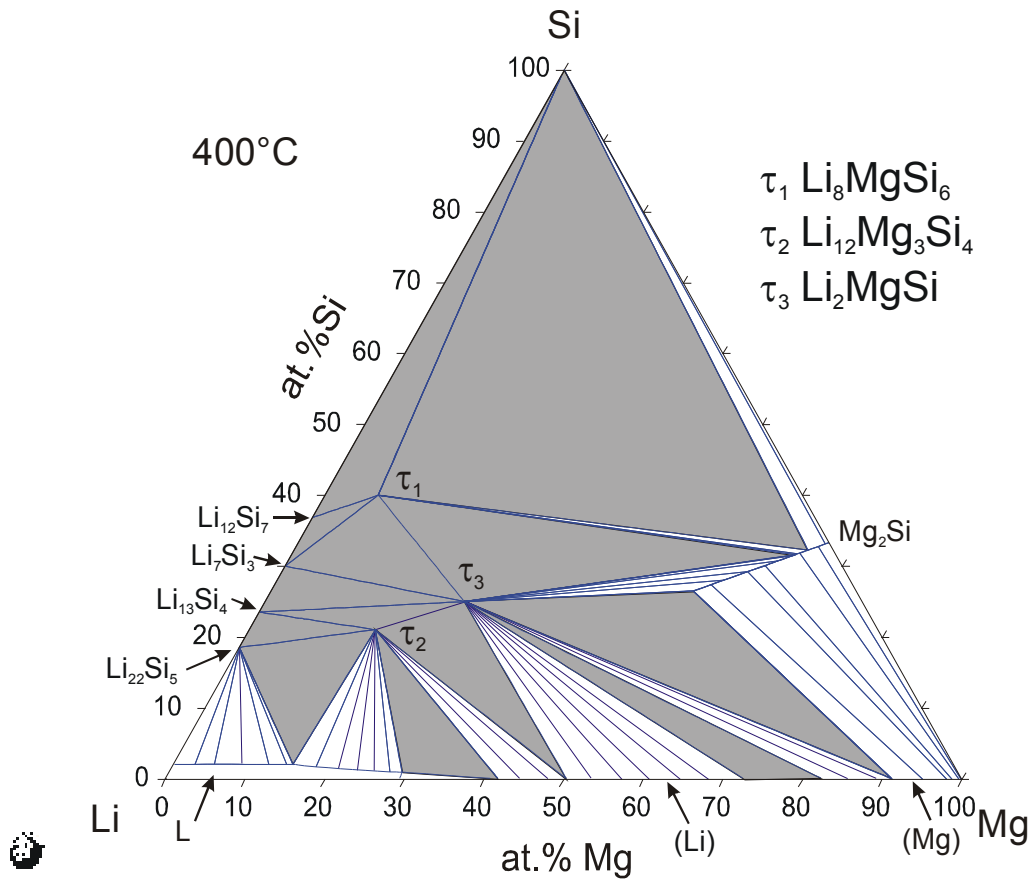


Fig. 21. Calculated isothermal section of Li-Mg-Si phase diagram at 400°C

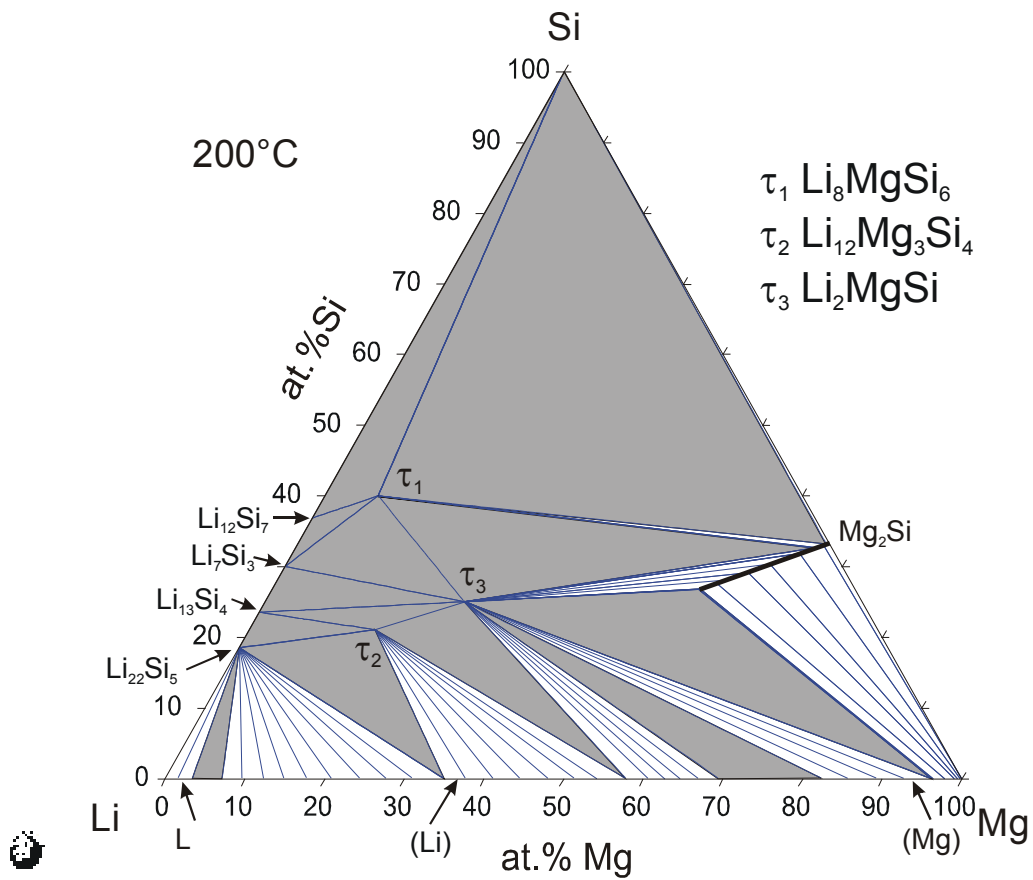


Fig. 22. Calculated isothermal section of Li-Mg-Si phase diagram at 200°C