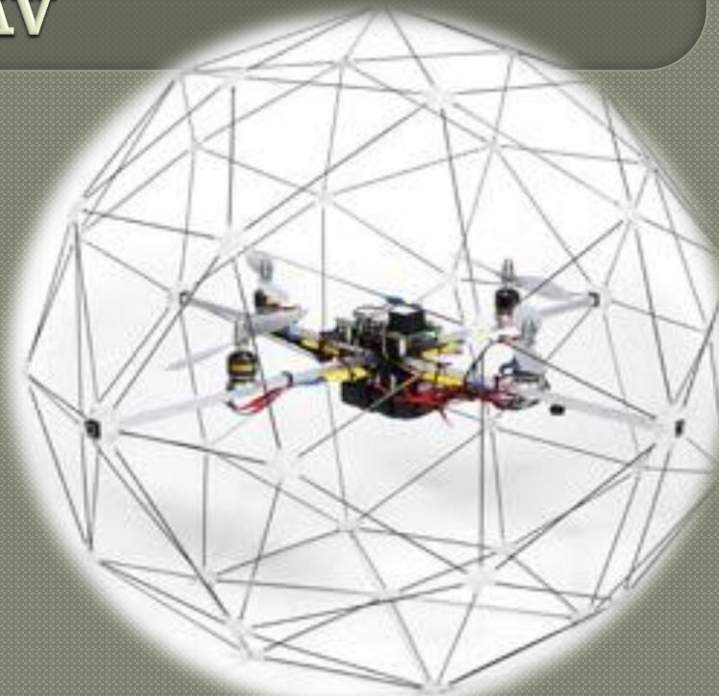




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FDD AND FTC DESIGN AND IMPLEMENTATION TO A QUAD-ROTOR UAV

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ENGR 691X: Fault Diagnosis and Fault-Tolerant Control Systems
Final Project - Fall 2010



Camera: Olympus E-P2 4/3rds sensor
Camera art filter: Diorama
Settings:
ISO 400, 17mm, 0EV, f/2.8, 1/60



DRAGANFLYER X8

OUTLINE

- Objectives
- Equations of motions
- LQR & PID controller concepts
- AFTCS concepts
- AFTCS implementation
- Conclusion



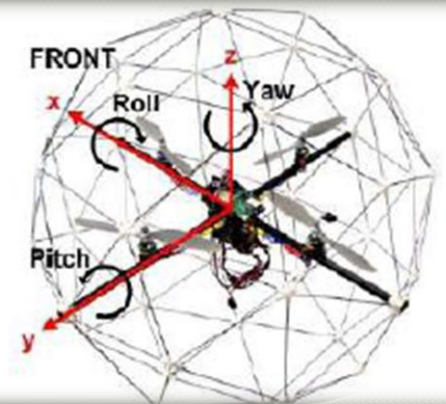
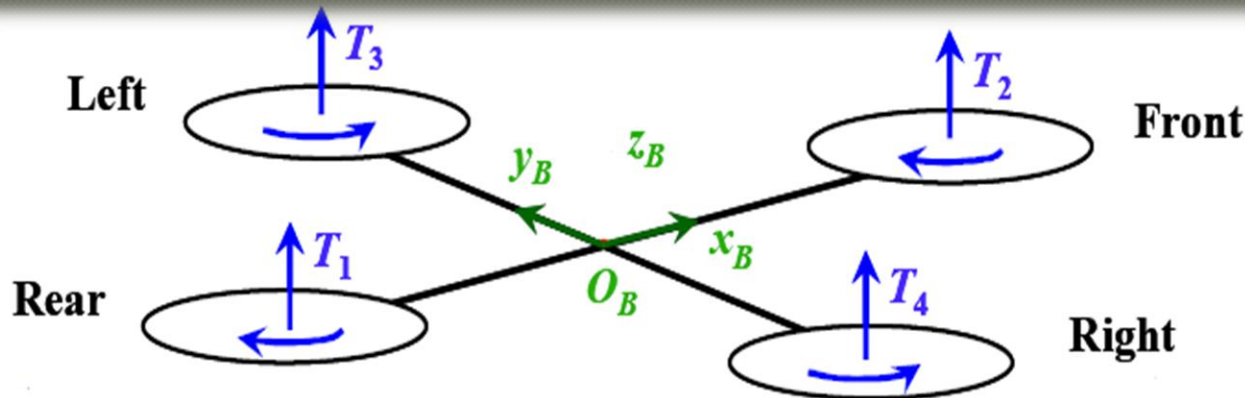
Project Objectives

- *Apply AFTCS to Q-Ball, so it can maintain a certain attitude despite of partial loss in Actuator*
- *Use two different approaches for Reconfigurable Controller part*
- *Post failure system can maintain stability and performance*
- *Hardware Implementation (Fault-free)*



Equations of Motions:

- The Quad-rotor has 6-DOF, it is equipped just with 4 propellers
- Four Basic Movements :
- **Throttle $U1$** ($\Omega_1 = \Omega_2 = \Omega_3 = \Omega_4$)
- **Roll $U2$** ($\Omega_3 \uparrow$ & $\Omega_4 \downarrow$)
- **Pitch $U3$** ($\Omega_1 \uparrow$ & $\Omega_2 \downarrow$)
- **Yaw $U4$** ($\Omega_1 \Omega_2 \uparrow$ & $\Omega_3 \Omega_4 \downarrow$)



Cont.

○ Simplified Models:

$$\begin{bmatrix} U1 \\ U2 \\ U3 \\ U4 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 0 & L & -L \\ L & -L & 0 & 0 \\ C & C & -C & -C \end{bmatrix} \begin{bmatrix} T1 \\ T2 \\ T3 \\ T4 \end{bmatrix} \quad T_i = K \frac{w}{s+w} u_i$$

$$\begin{aligned} \ddot{x} &= (\sin \Psi \sin \Phi + \cos \Psi \sin \theta \cos \Phi) \frac{U1}{M} & \ddot{\Phi} &= \frac{U2}{J_{xx}} \\ \ddot{y} &= (\sin \Psi \sin \theta \cos \Phi - \cos \Psi \sin \Phi) \frac{U1}{M} & \ddot{\theta} &= \frac{U3}{J_{yy}} \\ \ddot{z} &= -g + (\cos \theta \cos \Phi) \frac{U1}{M} & \ddot{\Psi} &= \frac{U4}{J_{zz}} \end{aligned}$$



(Linear Quadratic Regulator) LQR

I. LQR – Regulation Problem

$$\dot{x} = Ax + Bu$$

$$u = -Kx + v$$

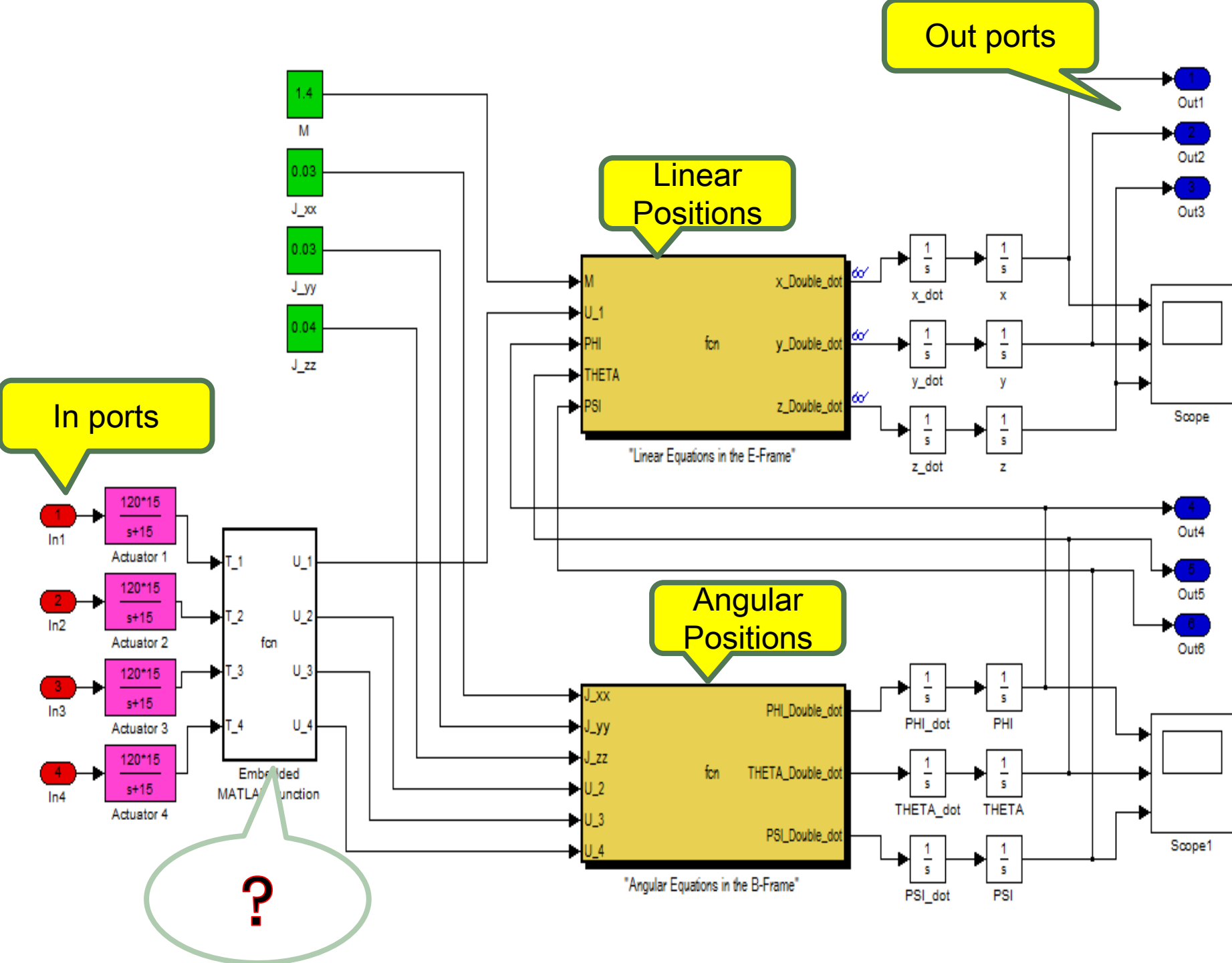
$$\dot{x} = (A - BK)x + Bv = A_{NEW}x + Bv$$

- The "cost function" is defined as a sum of the deviations of key measurements from their desired values.
- Still needs to specify the weighting Q & R factors and compare the results with the specified design goals

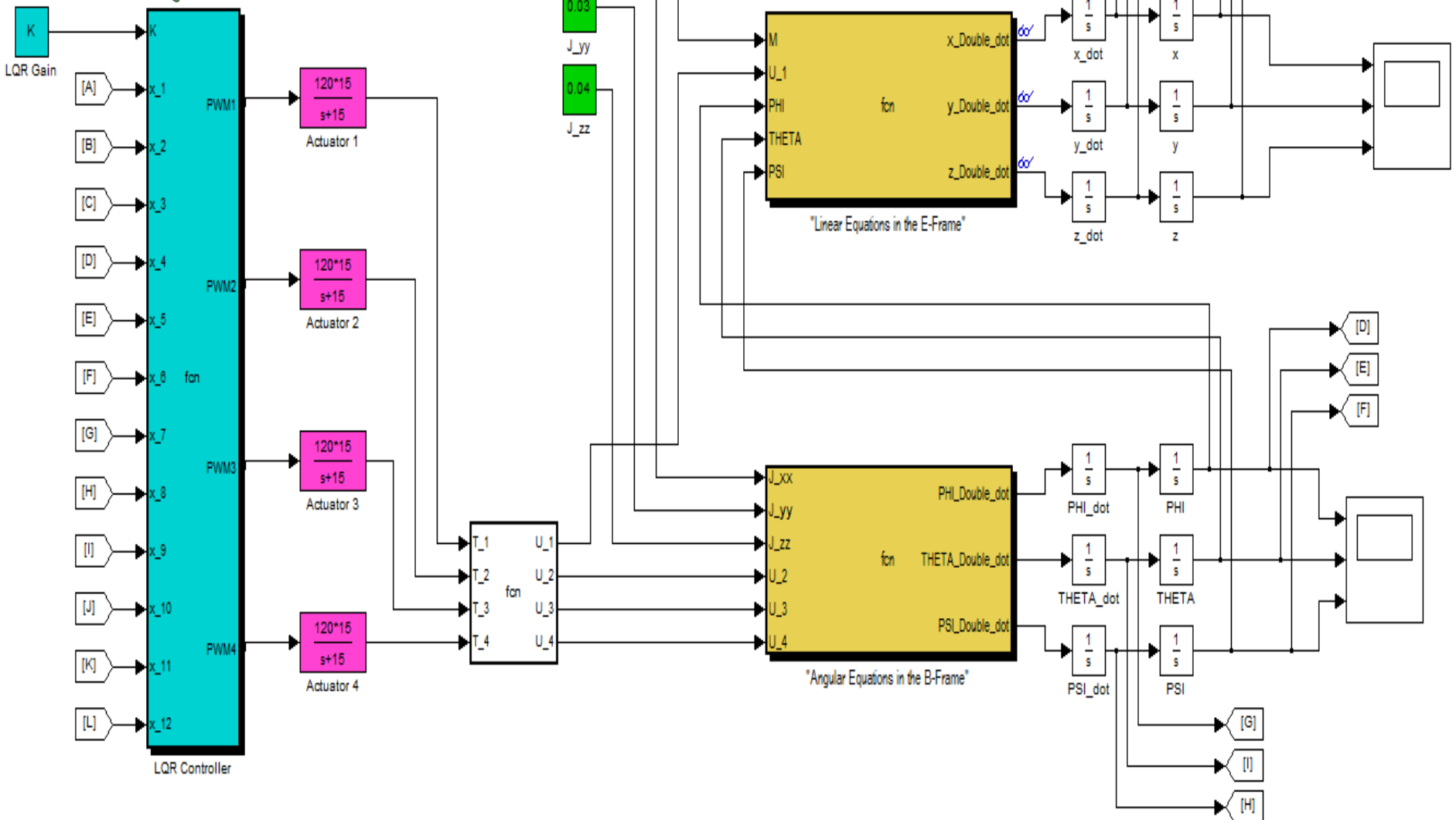


Cont.

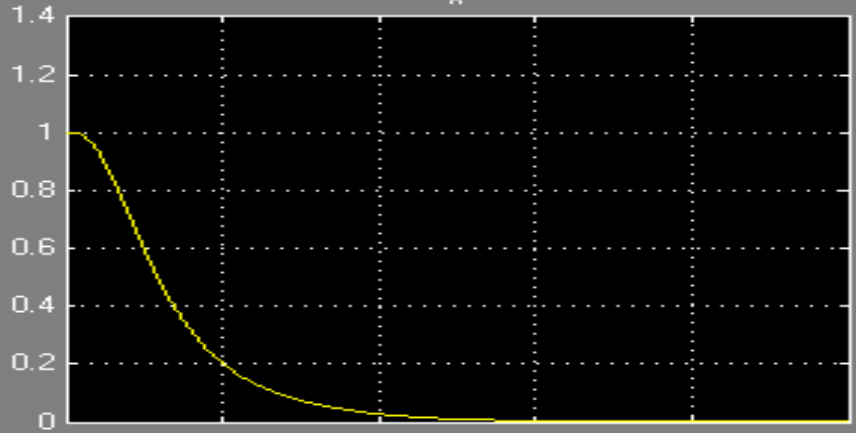
- **LQR - Regulator** implies that brings all state variables to zero and stabilizes the control system
- $K = lqr(A, B, Q, R)$ in MATLAB
- LQR controller is its limited applicability to just linear systems.
- In our project it was required to obtain linearized equations of motion of Q-Ball
- **MATLAB** routine “*linmod*” has been employed
- A “*Trim*” command used before linearization . **Trim Point**, also known as an equilibrium point, is a point in the parameter space of a dynamic system at which the system is in a steady state



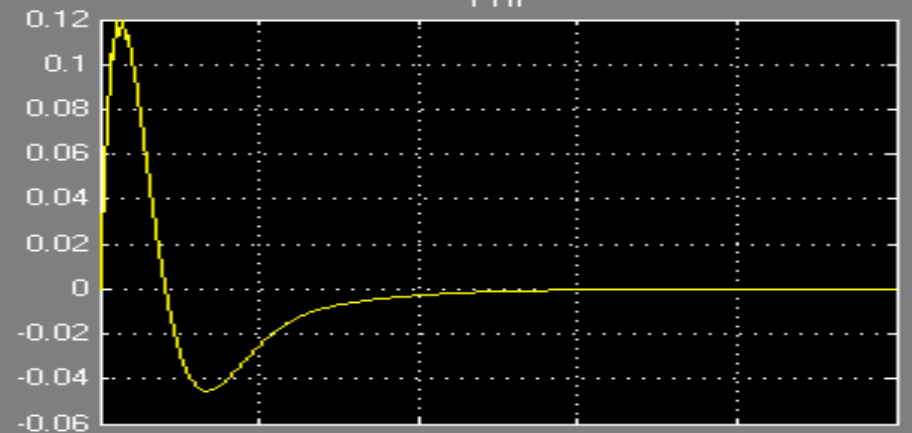
LQR Controller



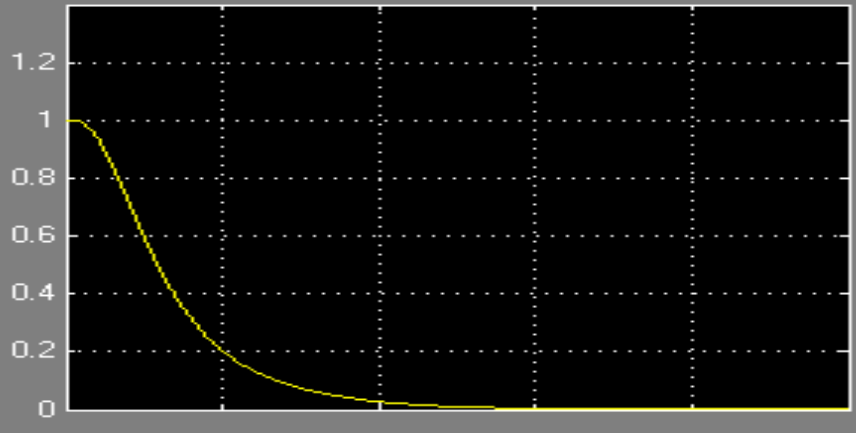
" x "



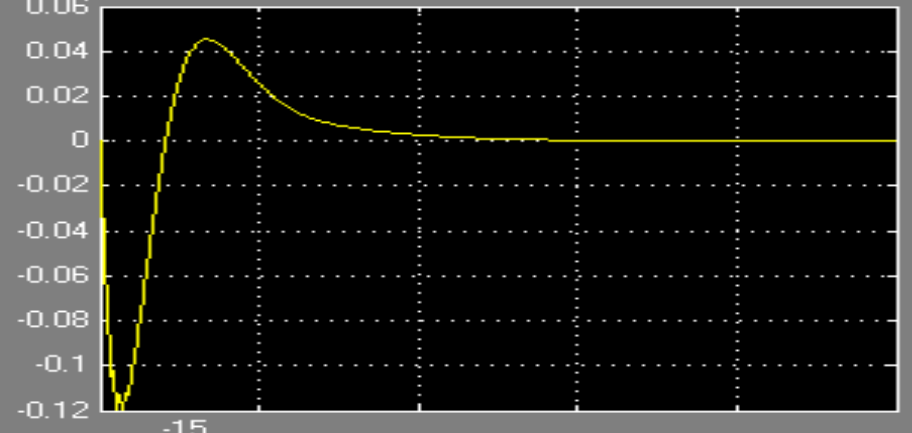
" PHI "



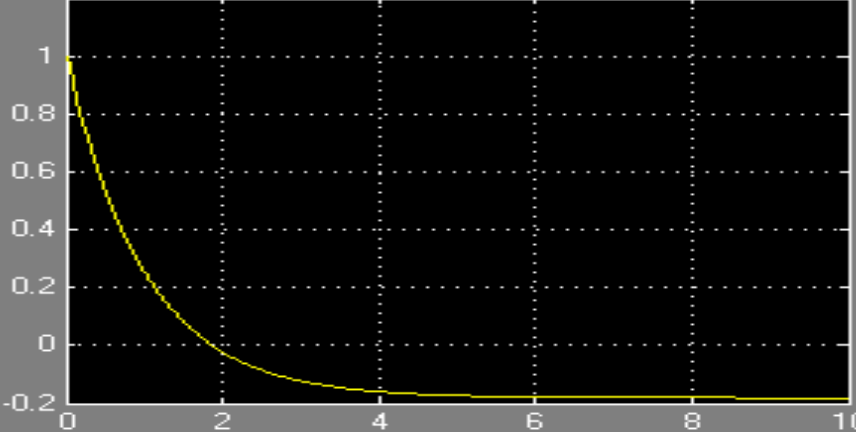
" y "



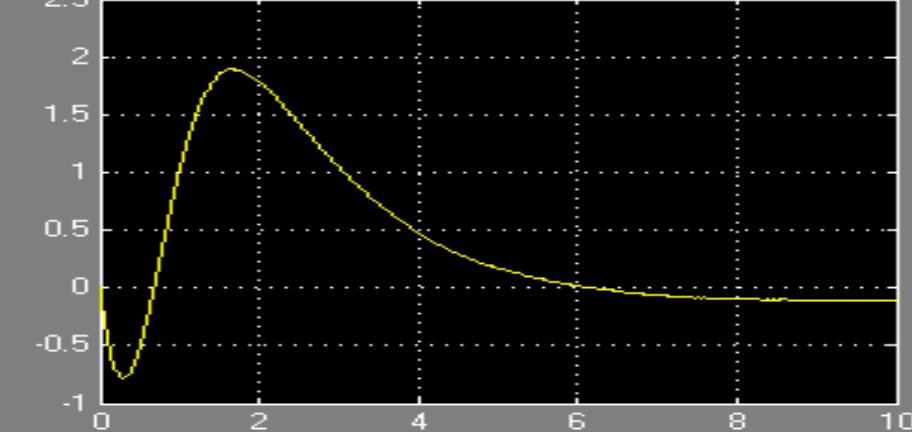
" THETA "



" z "



" PSI "



LQR – Tracking Problem

- Imagine a control system expressed in state space format as follows:

$$\dot{x} = Ax + Bu$$

- The same as for non-tracking problem/regulator, here the control signal is:

$$u = -KX$$

- Let's assume $x = [x_1 \ x_2 \ x_3 \ \dots \ x_n]$, indicating n state variables.
- Also, imagine that there are reference values for x_{1d} , x_{2d} , x_{3d} , ..., and x_{md} for which the controller is responsible:

$$X = [x_1, x_2, x_3, \dots, x_n, z_{1d}, z_{2d}, z_{3d}, \dots, z_{md}]$$

$$z_{id} = \int x_i - x_{id} dt$$

LQR

- With this definition the new representation of the system becomes:

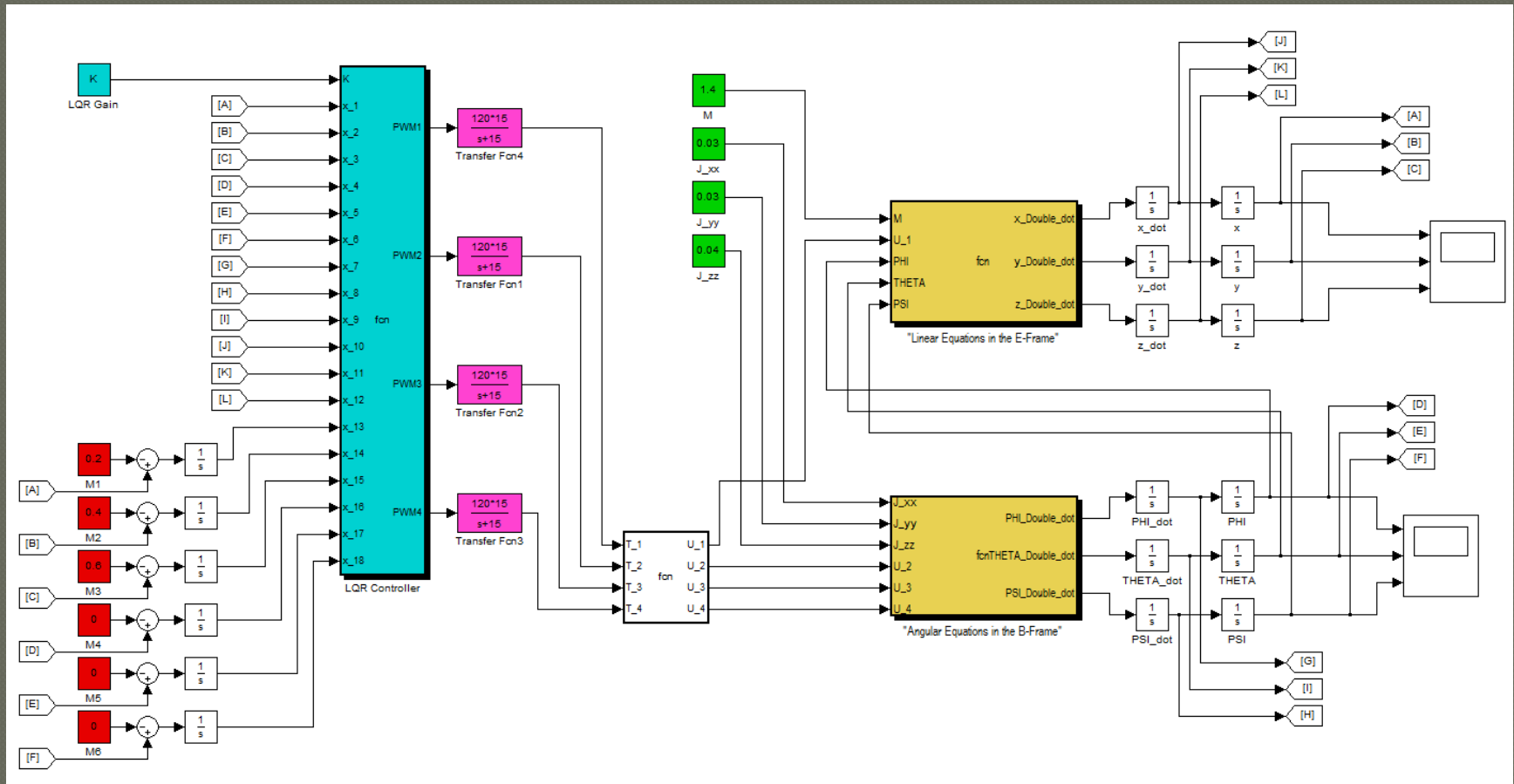
$$\dot{X} = \begin{bmatrix} & [A] & [0] \\ [1] & \dots & 0 \\ \vdots & \ddots & \vdots \\ [0] & \dots & 1 \end{bmatrix}_{m \times m} X + \begin{bmatrix} [B] \\ 0 \end{bmatrix} u + \begin{bmatrix} [0]_{n \times m} \\ [-1] & \dots & 0 \\ \vdots & \ddots & \vdots \\ [0] & \dots & -1 \end{bmatrix}_{m \times m} \begin{bmatrix} x_{d1} \\ x_{d2} \\ x_{d3} \\ \vdots \\ x_{dm} \end{bmatrix}$$

Or in a more compact form:

$$\dot{X} = \bar{A}X + \bar{B}u + B_d P_d$$

- Again, once the state space representation of the control system is obtained, design of LQR Controller is almost straight forward. $K = lqr(A_bar, B_bar, Q, R)$.

Application of Design Methodology to QBall



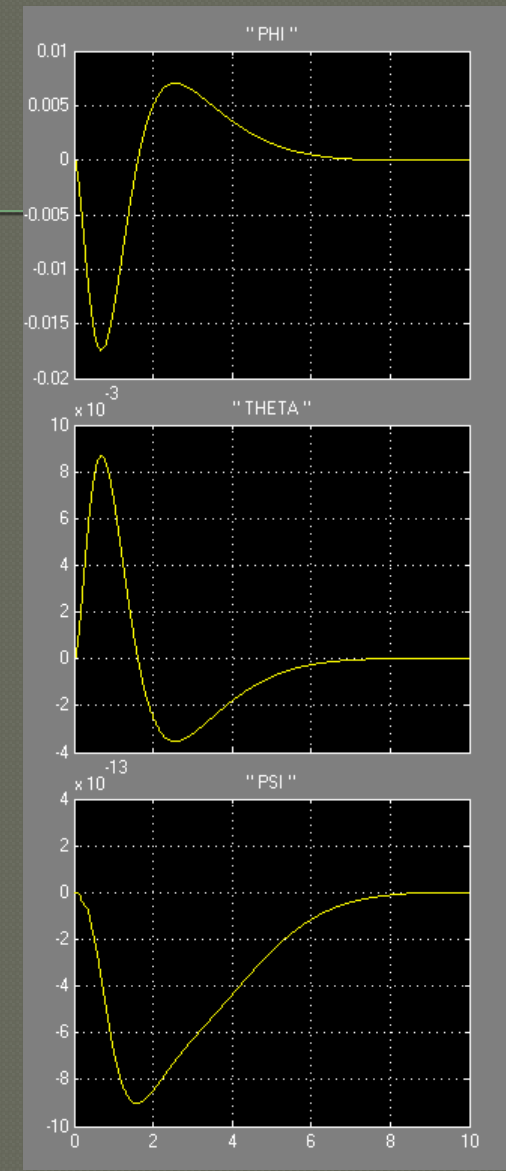
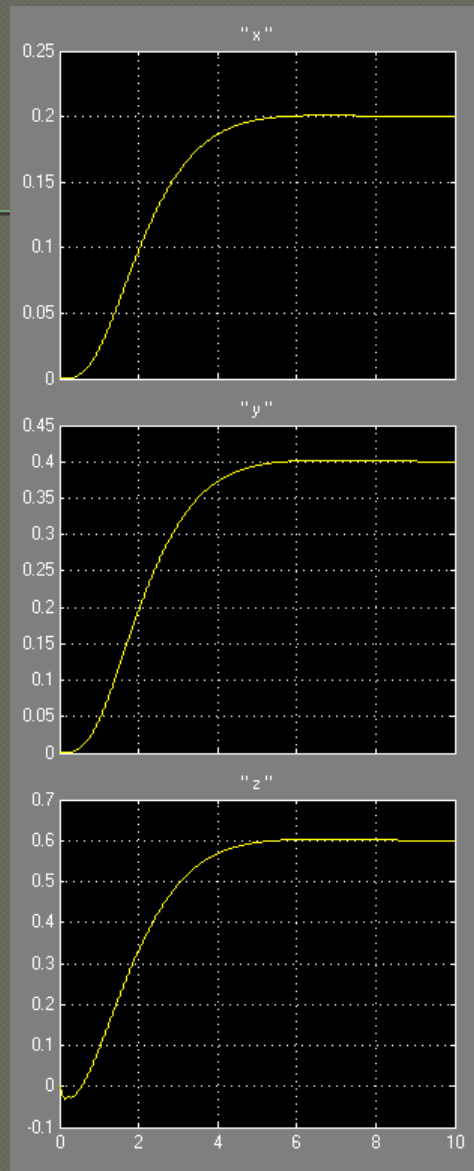
- Having chosen the values of these weighting matrices to be

$$Q = \text{eye}(16)$$

And

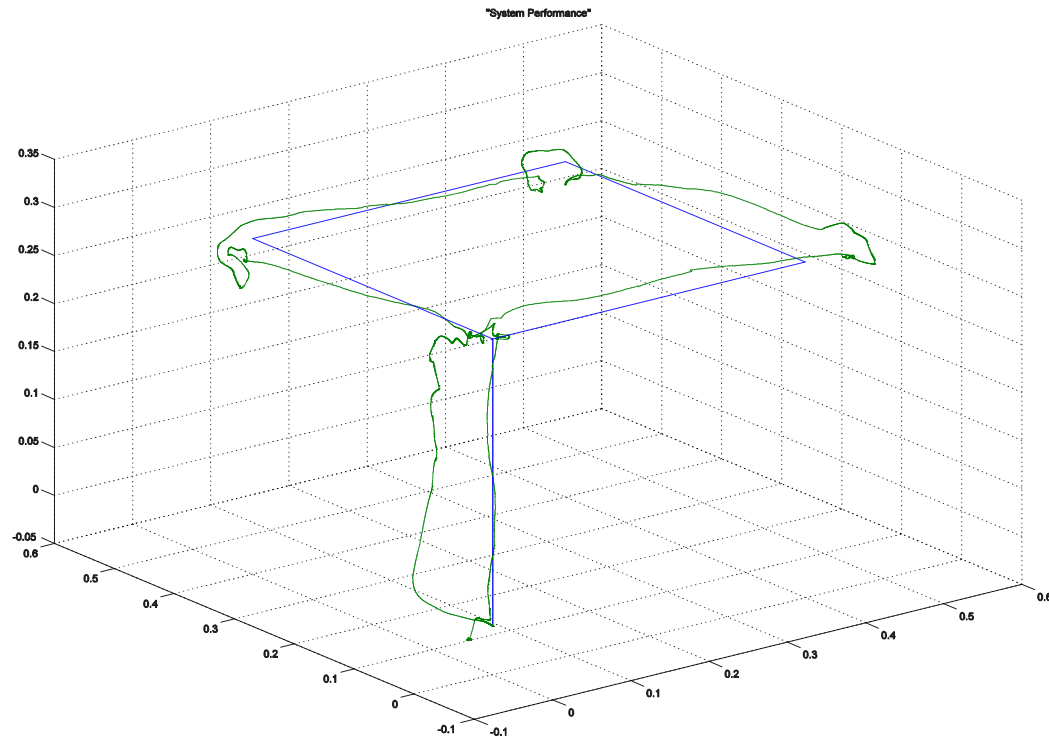
$$R = \text{eye}(4)$$

- Next is the time response of the system for the following reference inputs.



Time Response of the System

LQR - Real System Results (Fault-Free)



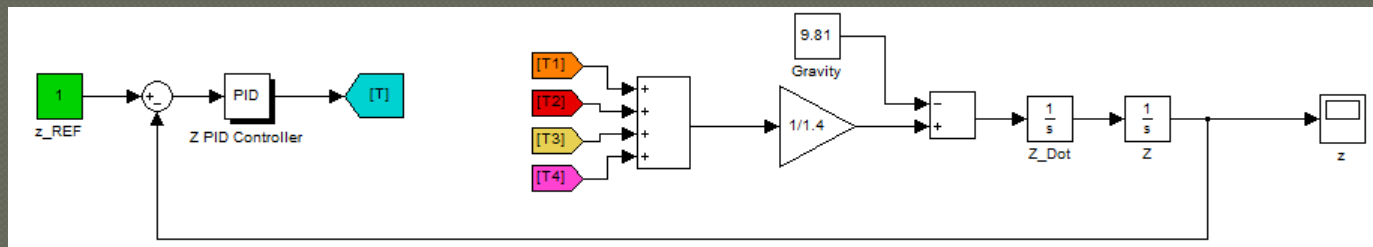
PID Controller

- In this section some assumptions are made to make the equations of motion of the plant (Q-Ball) simpler.
- This simplification let us neglect some cross-couplings effects among the equations of motion describing dynamics of the system.
- This way, the motion of the system is broken down into four independent channels:
 - Vertical Motion along the Z Axis Forwards and
 - Backwards Motion along the X Axis Coupled with Pitching Motion
 - Side Motion along the Y Axis Coupled with Rolling Motion And
 - Pure Yawing Motion

PID Controller : Decoupled, Simplified Equation of Motion

Vertical Motion along the Z Axis

$$M\ddot{Z} = (T1 + T2 + T3 + T4) - Mg$$



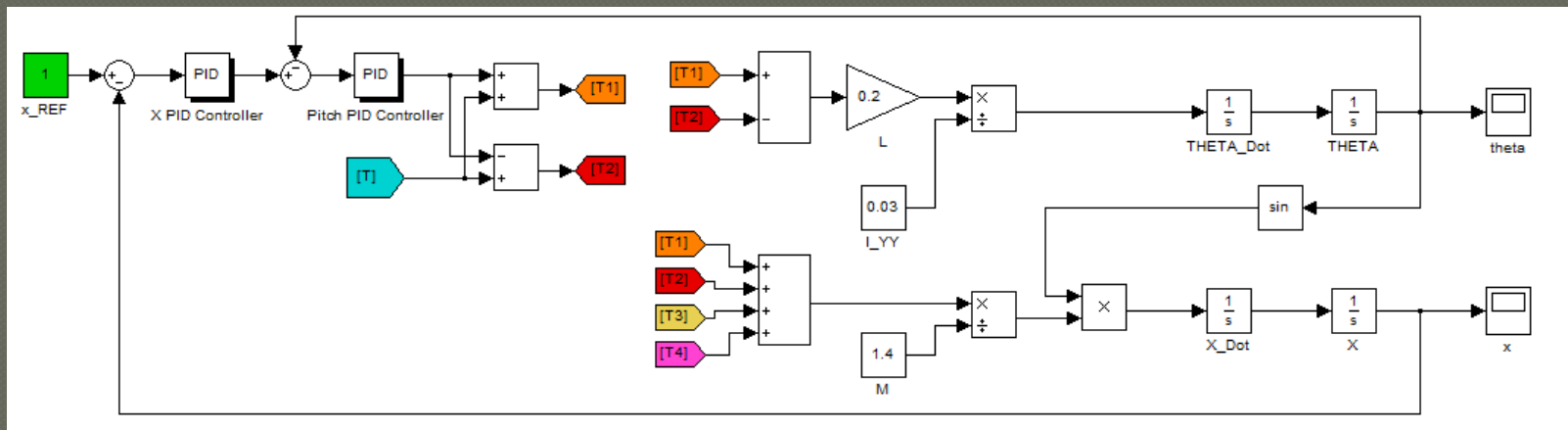
It should be notified that this modeling is valid as long as the Yaw Angle is automatically controlled to be zero.

PID Controller

- Forwards and Backwards Motion along the X Axis Coupled with Pitching Motion

$$M\ddot{X} = (T1 + T2 + T3 + T4) \sin \theta$$

$$I_{yy}\ddot{\theta} = (T1 - T2)L$$

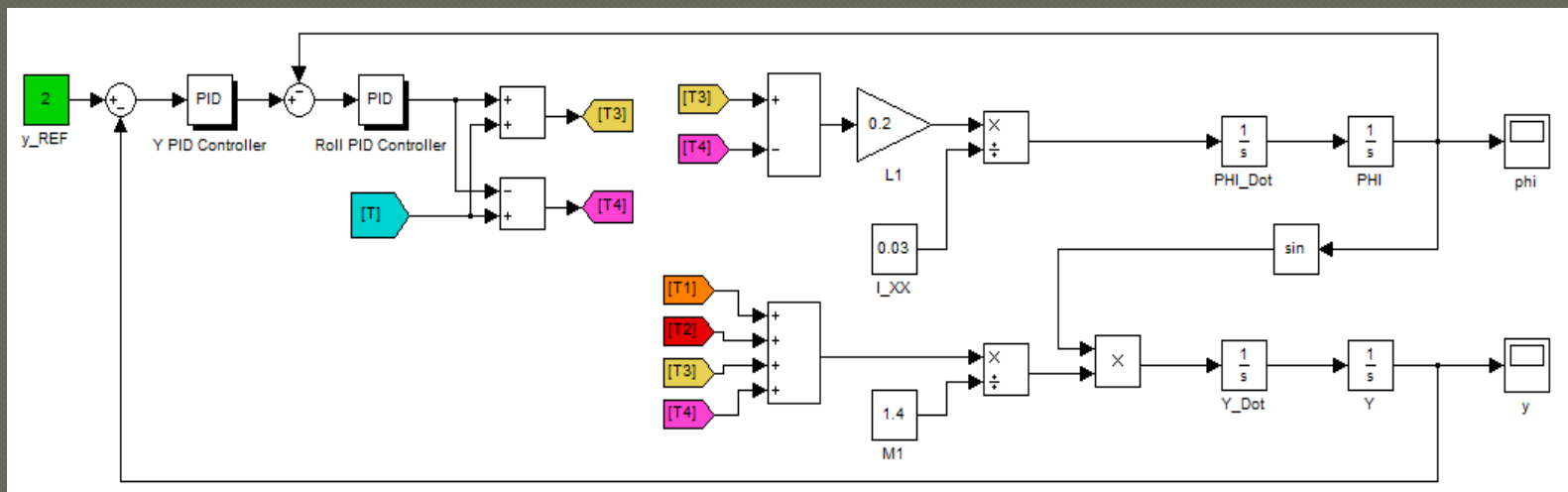


$$[(T1 - \Delta T) + (T2 + \Delta T) + T3 + T4] = [T1 + T2 + T3 + T4]$$

PID Controller

Side Motion along the Y Axis Coupled with Rolling Motion

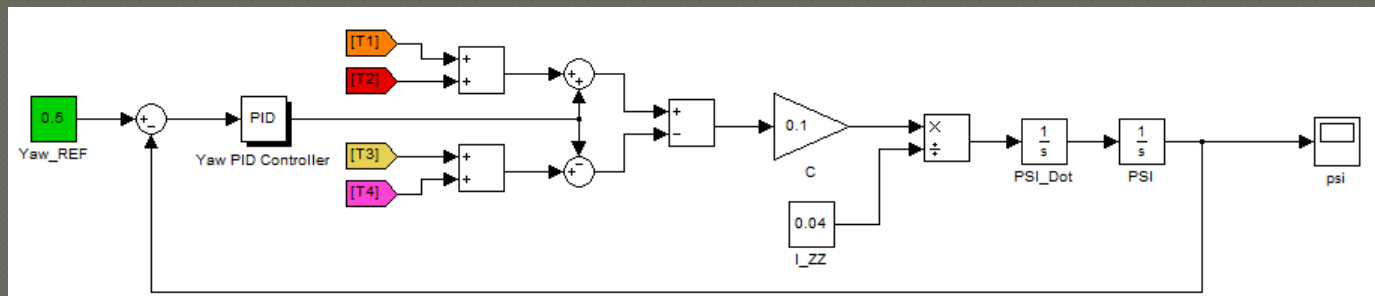
$$M\ddot{Y} = (T1 + T2 + T3 + T4)\phi$$
$$I_{xxx}\ddot{\phi} = (T3 - T4)L$$



PID Controller

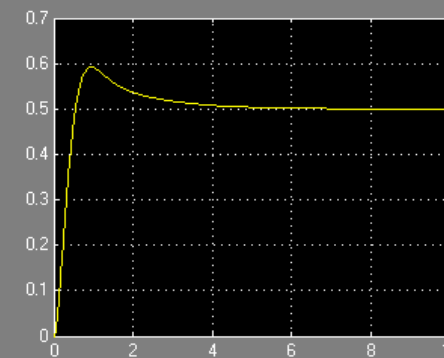
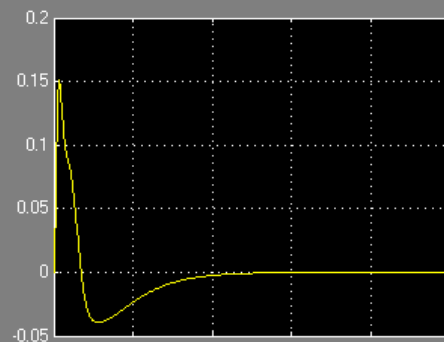
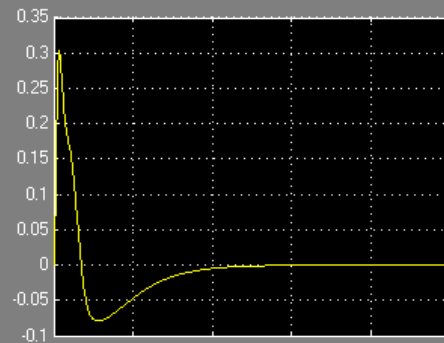
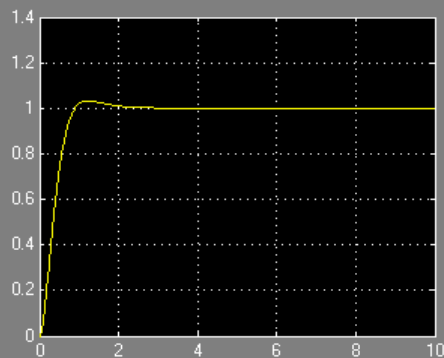
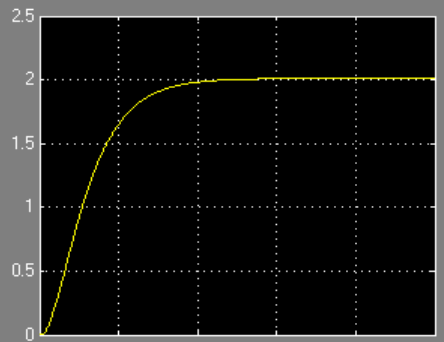
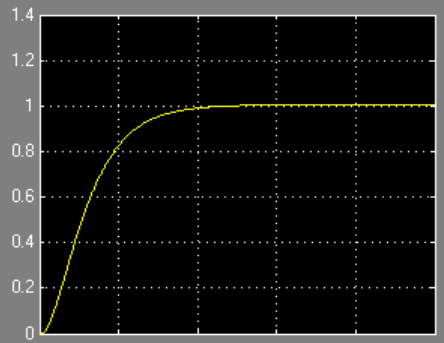
● Pure Yawing Motion

$$J_{zz}\ddot{\psi} = (T1 + T2 - T3 - T4)C$$



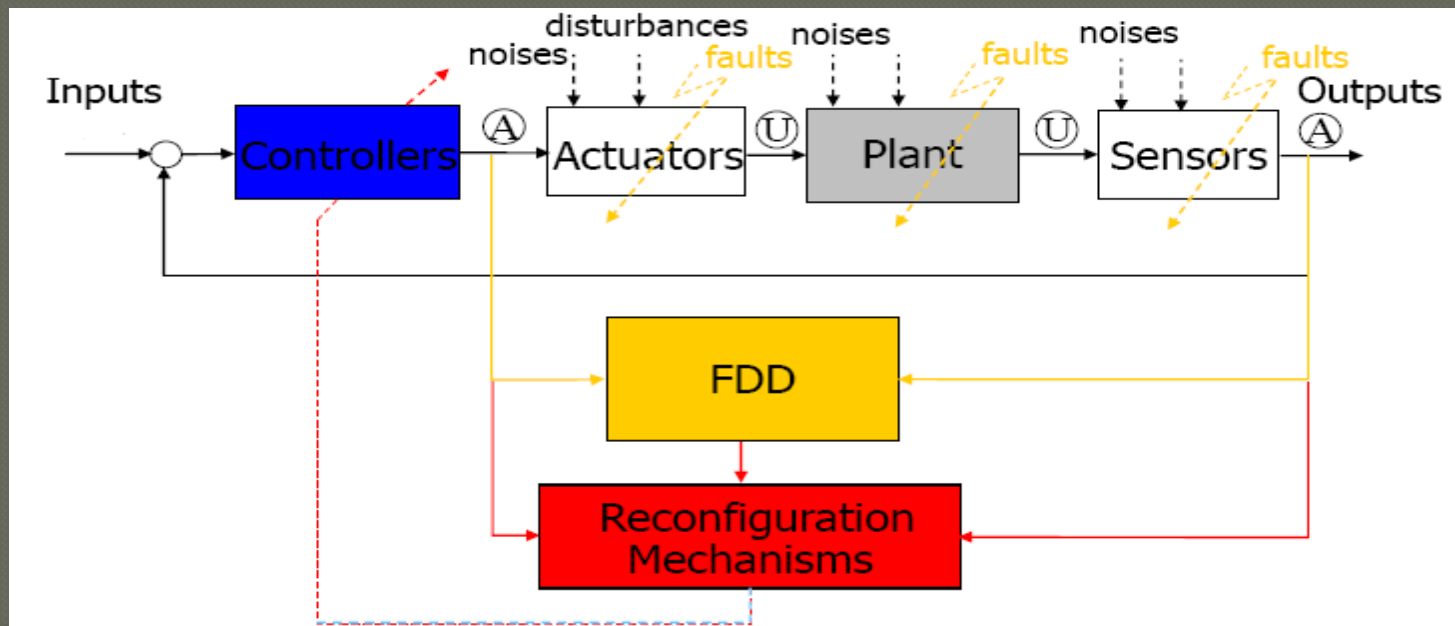
- ***A Remark on PID Tuning:*** Tuning of the inner loop PID Controller prior to tuning of the outer loop PID Controller is required for the sake of fine and effective tuning.

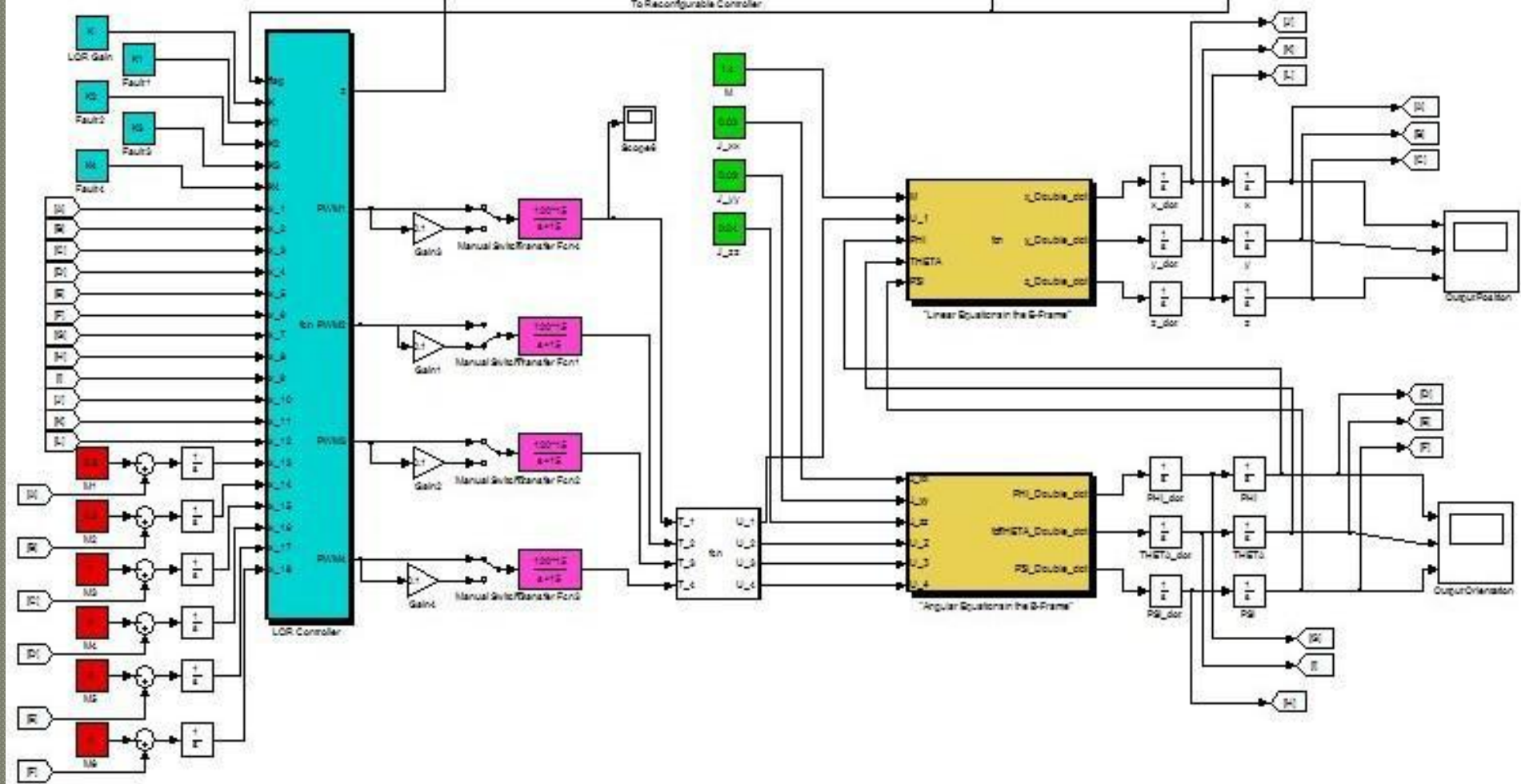
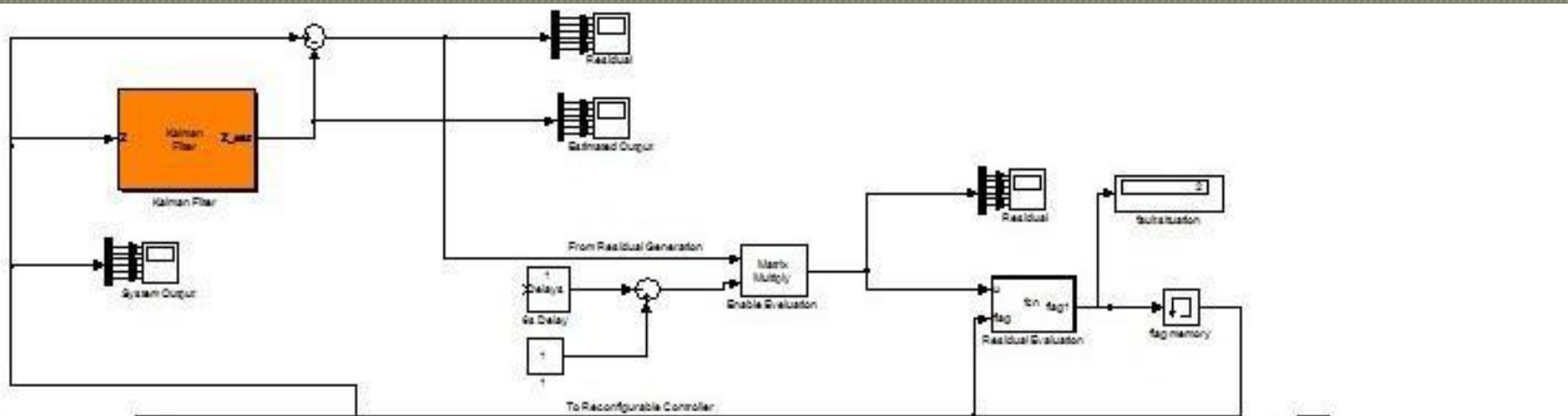
PID Controller :Results



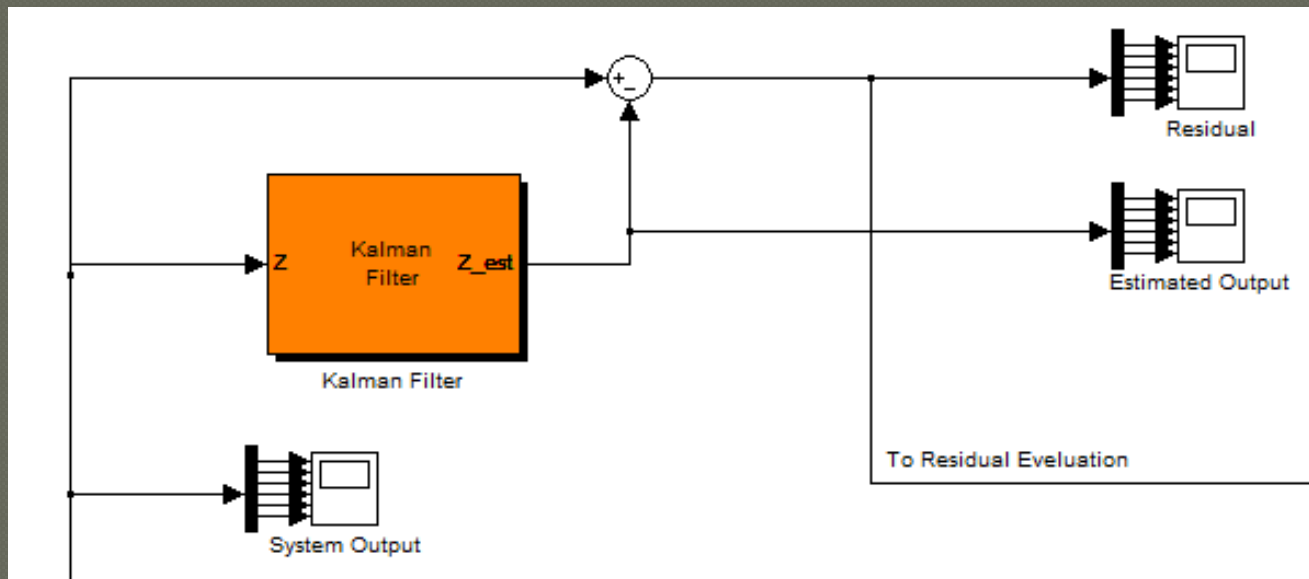
AFTCS Concepts

- **AFTCS** is combined by three parts:
 1. FDD part
 2. Reconfiguration Mechanism
 3. Reconfigurable Controller.



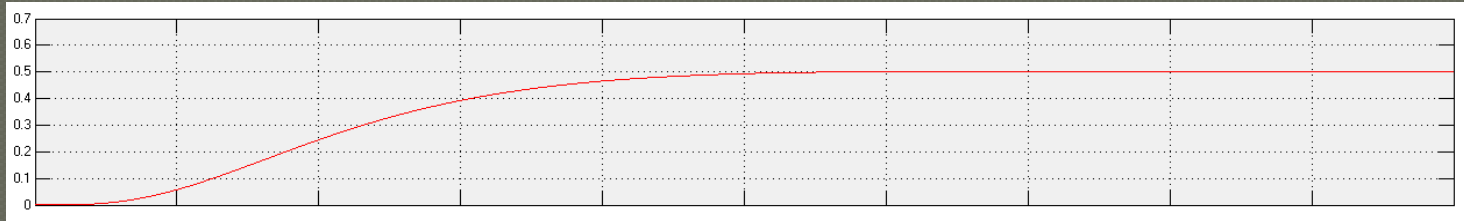


LQR-FDD



- **General Frame of Residual Generation**

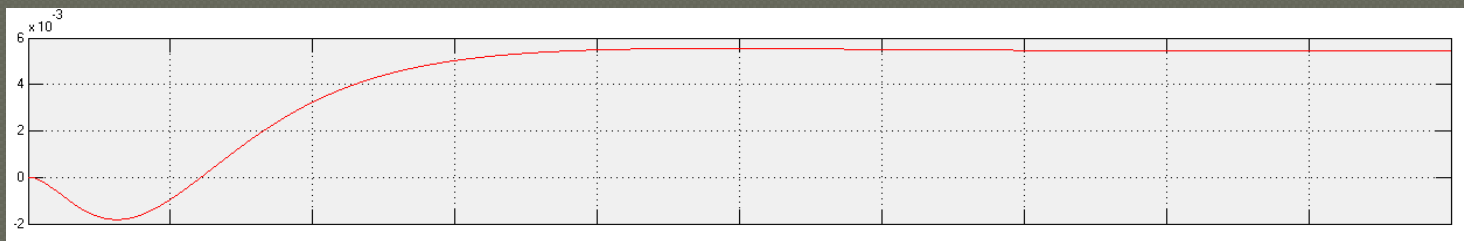
Residual Generation



System output

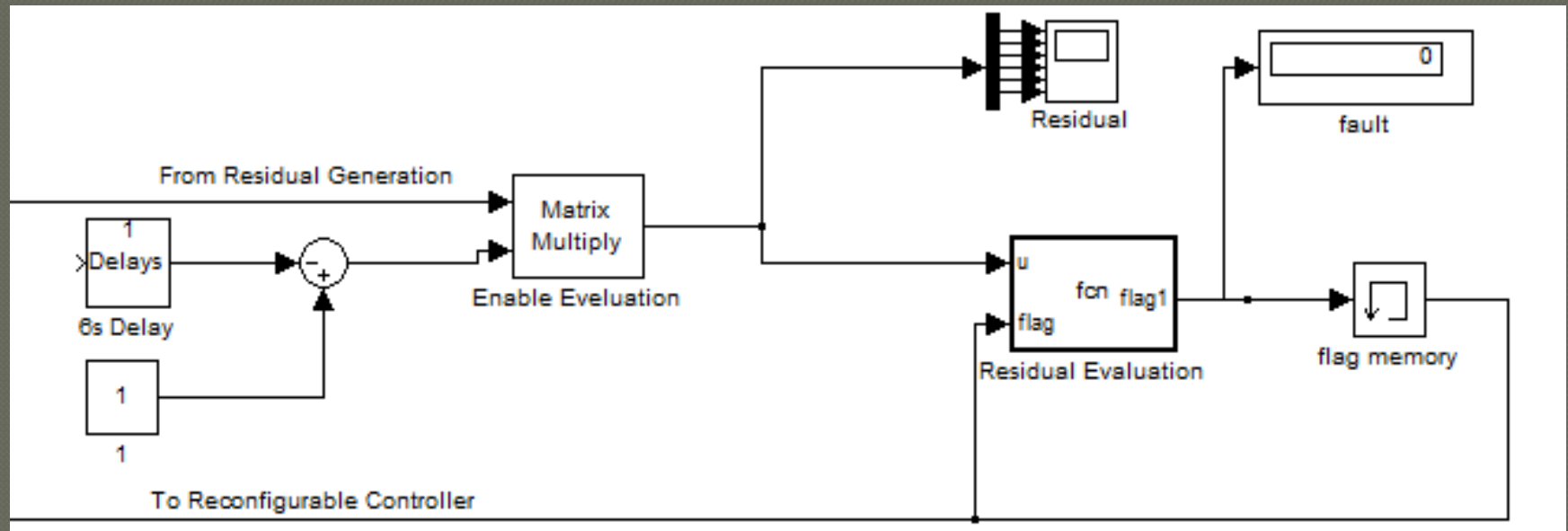


Estimated output



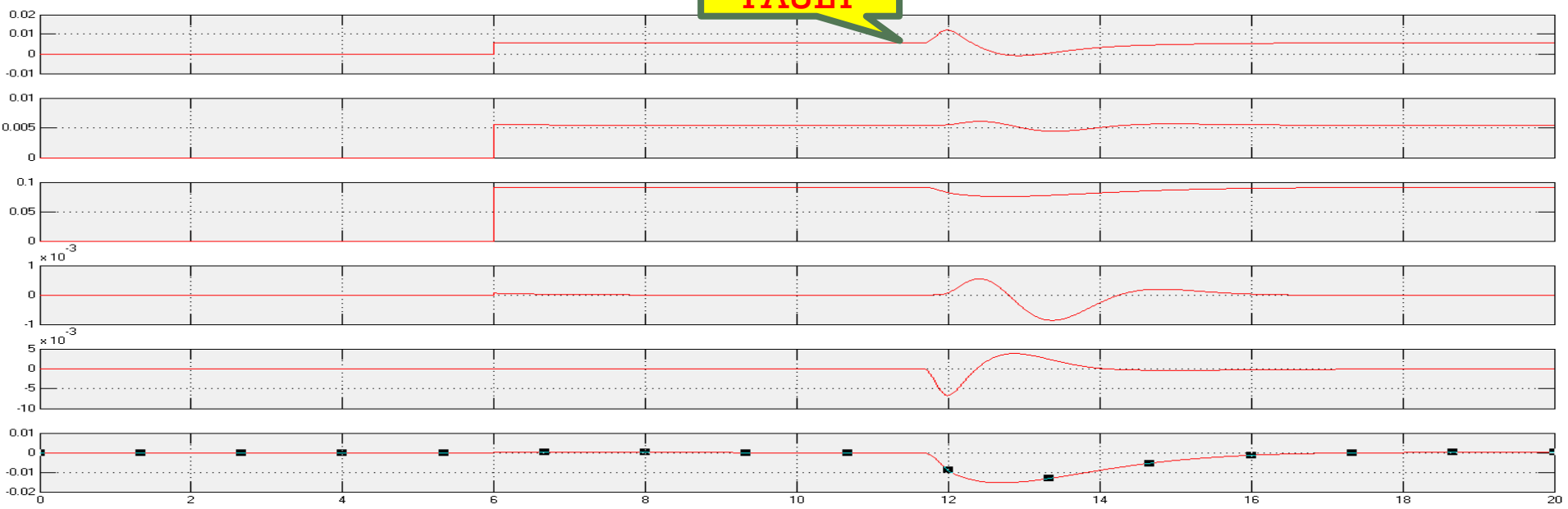
Residual (Fault-Free)

Residual Evaluation Part

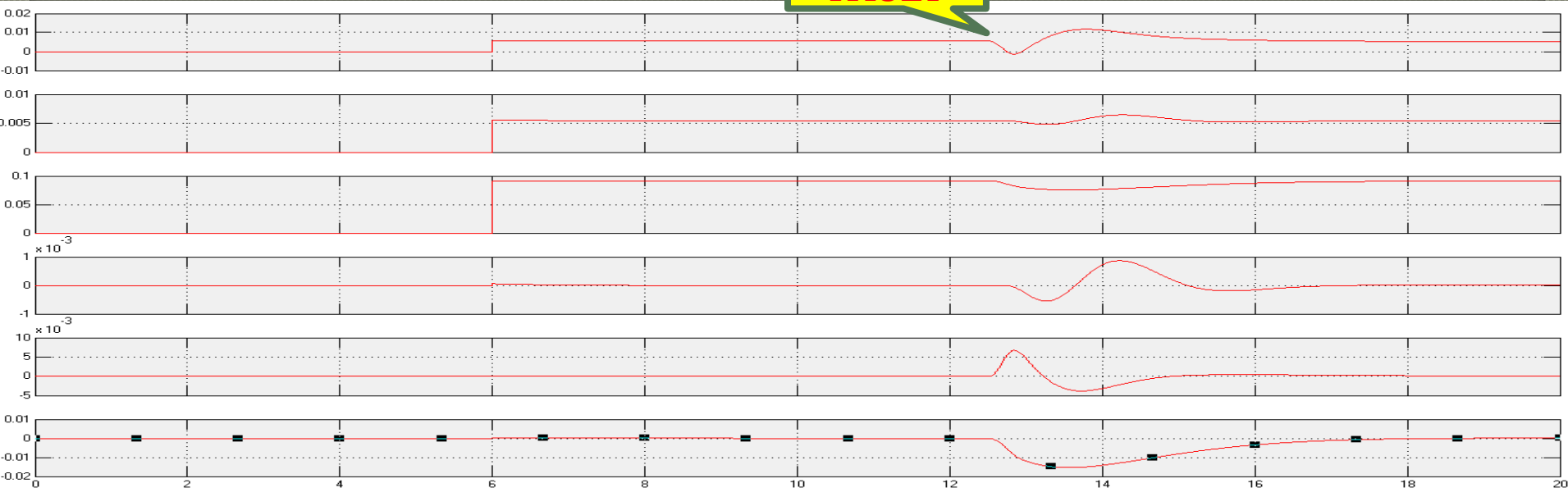


Residual Evaluation and Reconfigurable Mechanism

FAULT

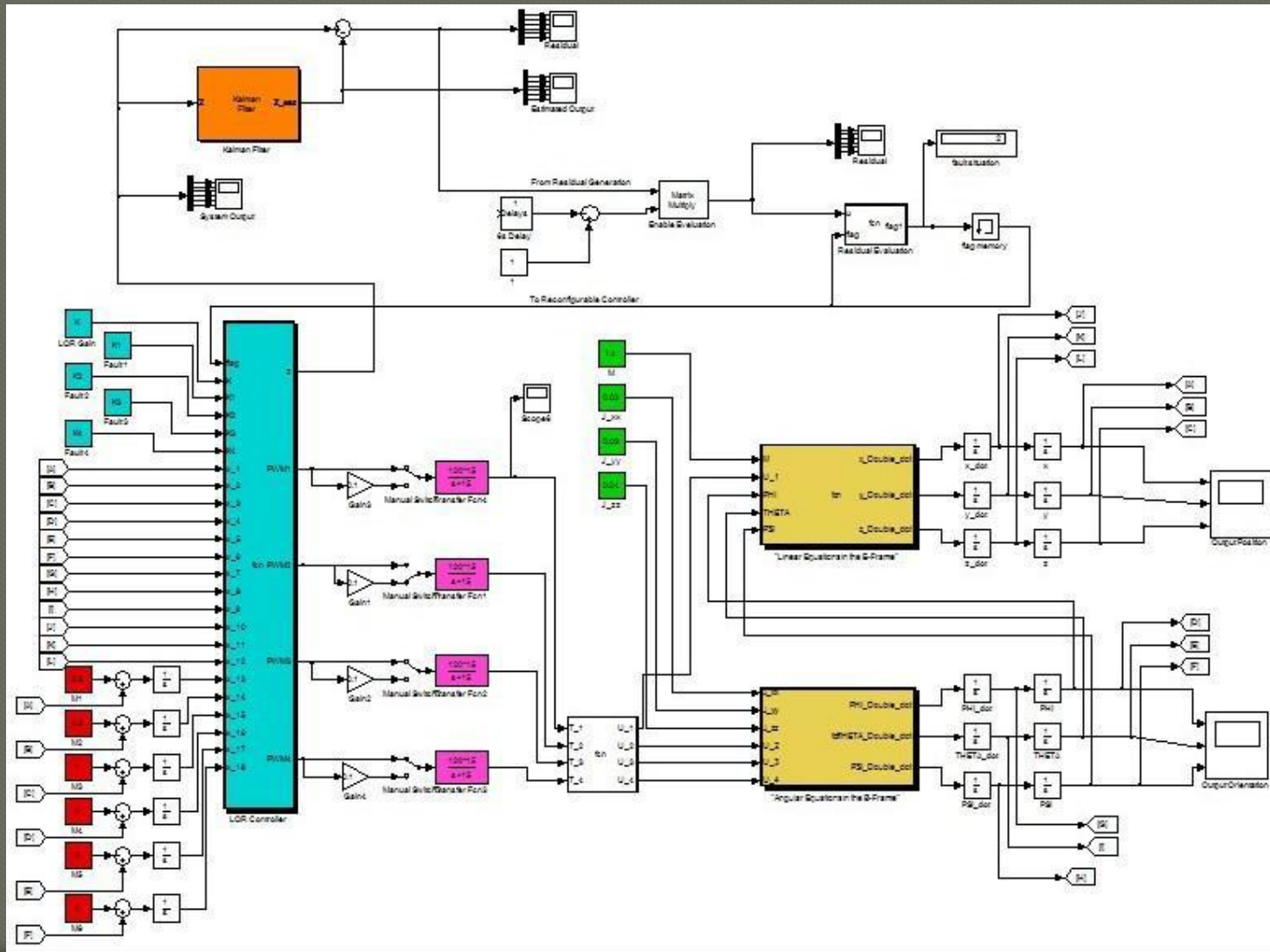


Residual of a **FAULT** fault



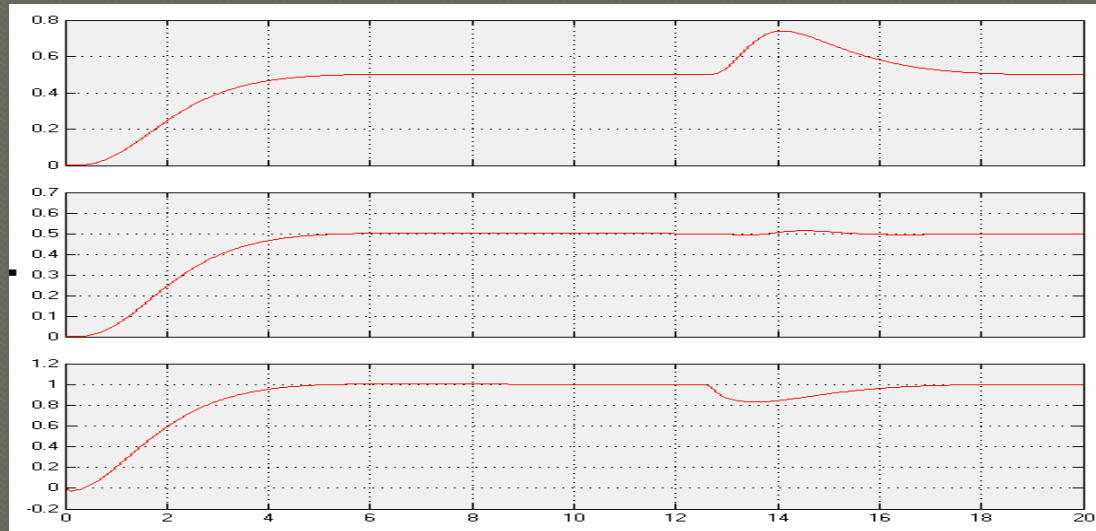
Residual of actuator 2 fault

LQR-Reconfigurable Controller

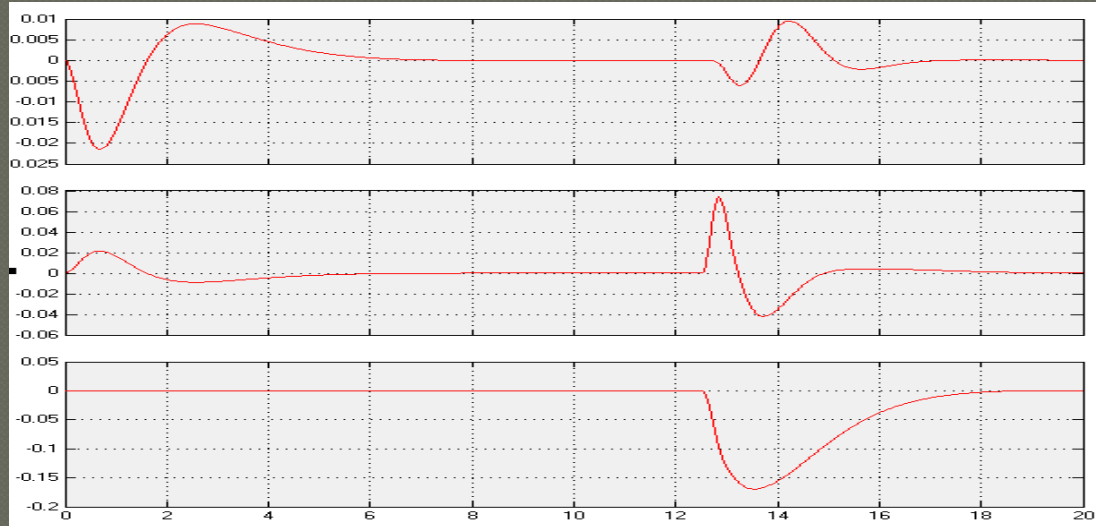


LQR AFTCS results

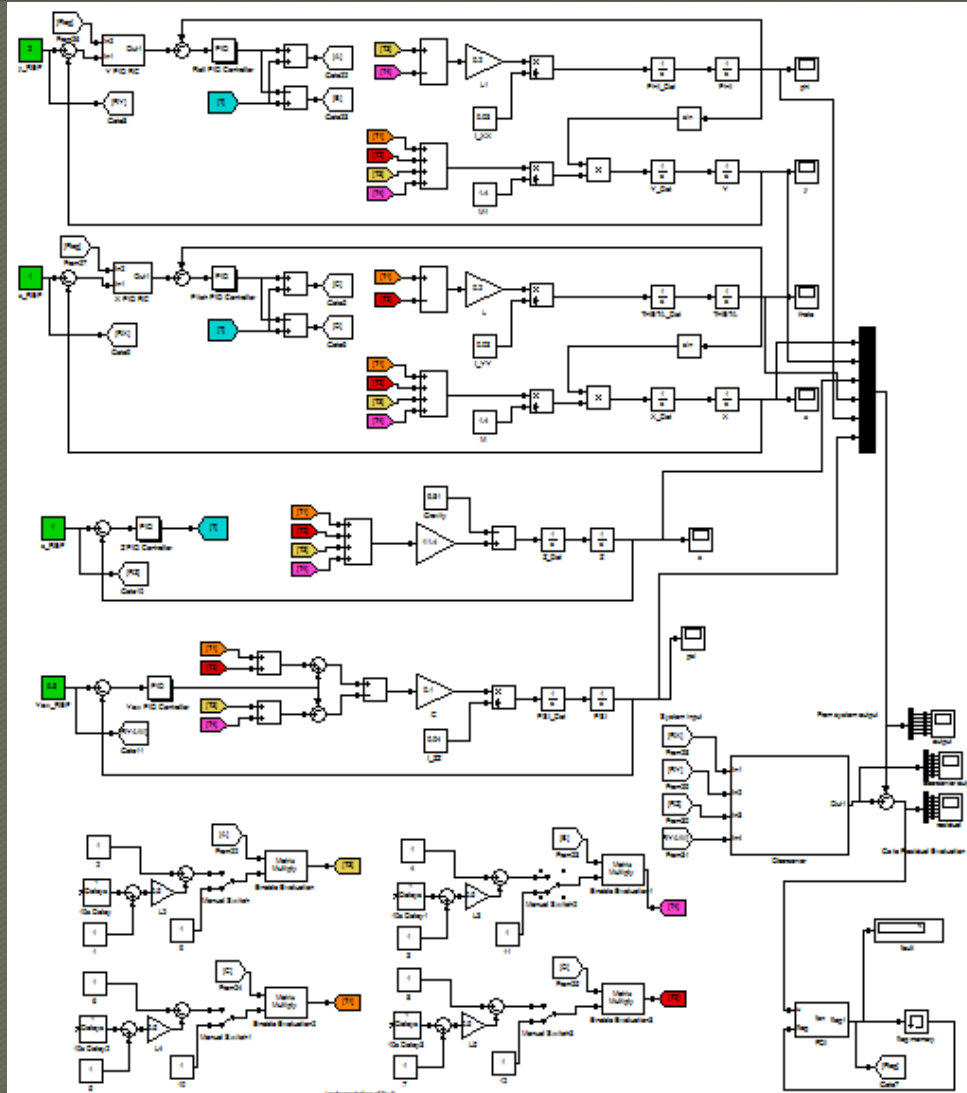
Output of actuator 2 fault (x , y , z)



Output of actuator 2 fault (φ , θ , Ψ)

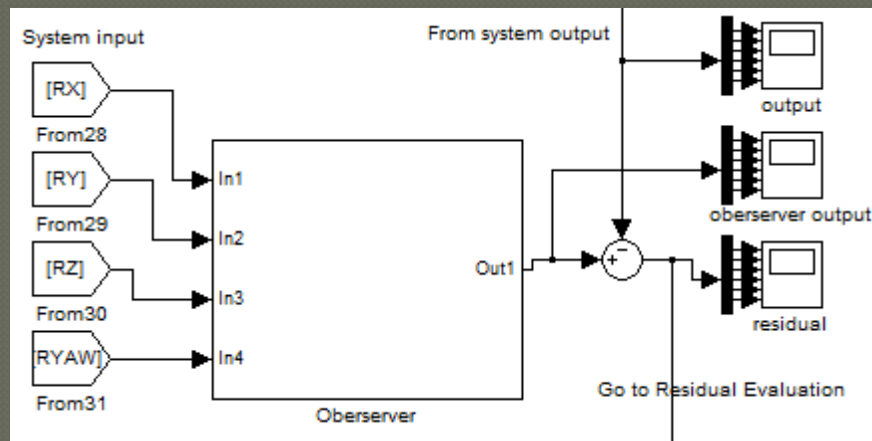


PID AFTCS simulink block

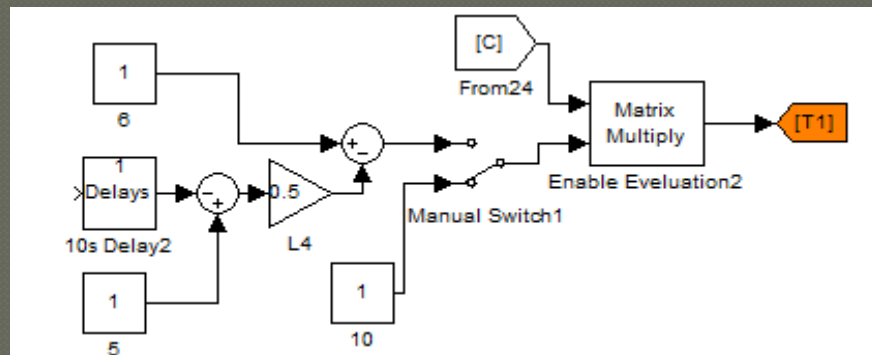


PID - FDD

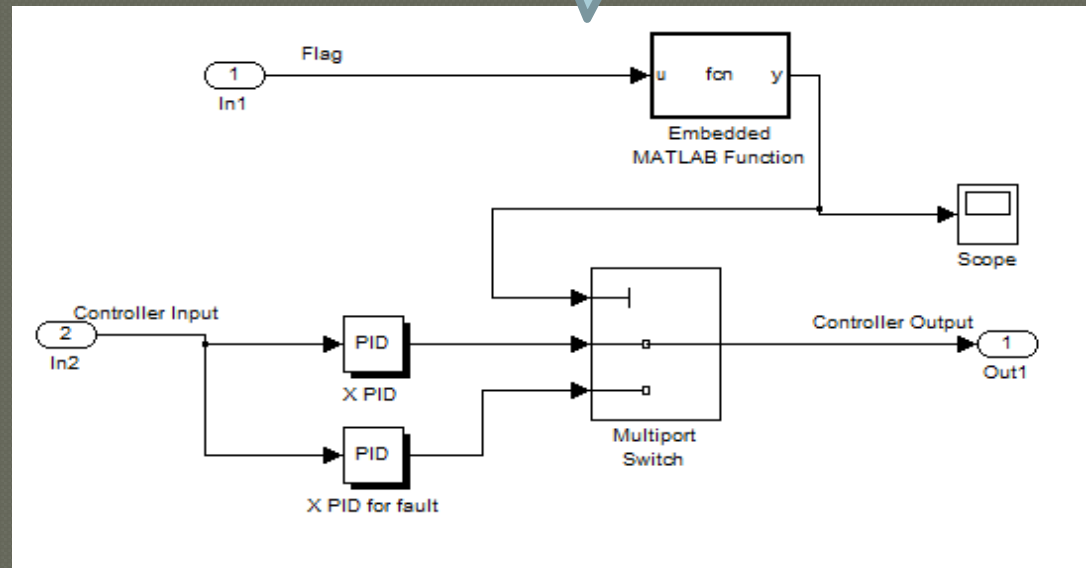
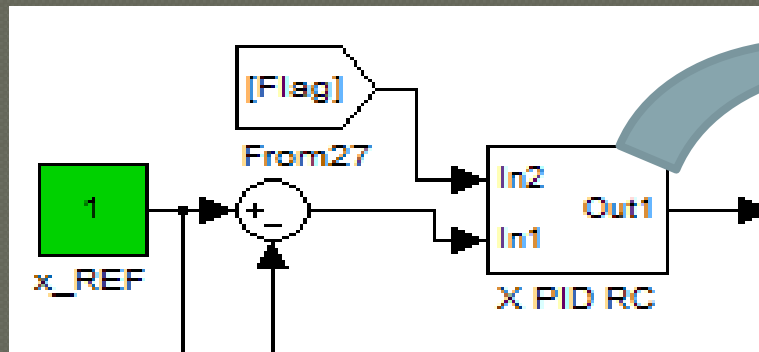
General frame of Analytical Redundancy



Fault Implementation

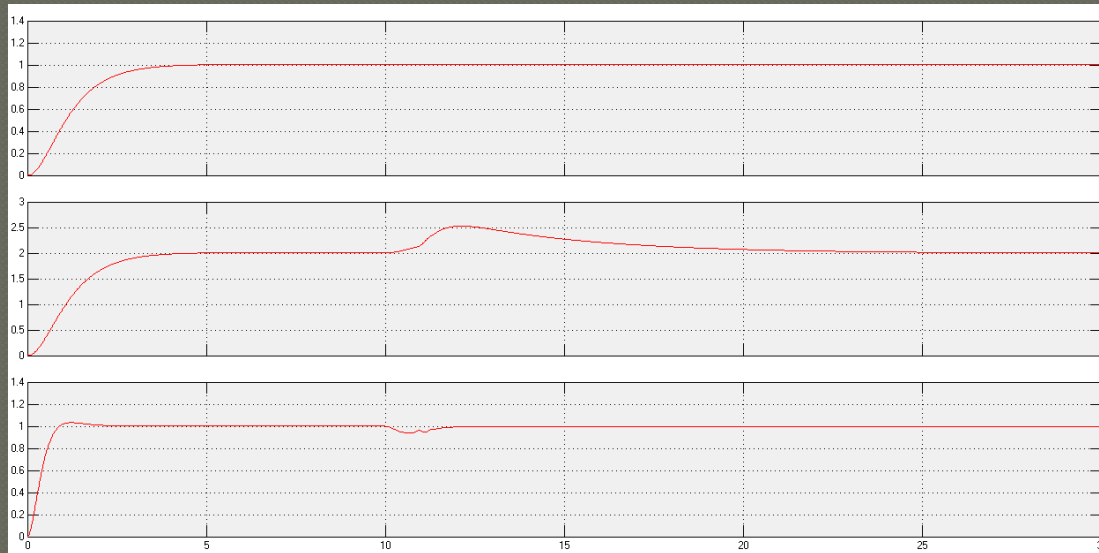


PID-Reconfigurable Controller

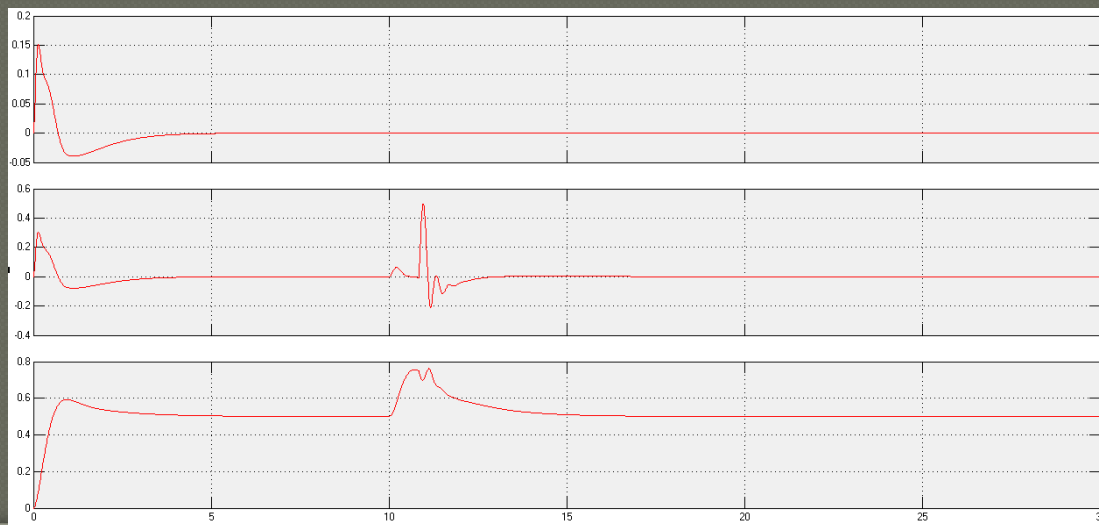


PID AFTCS results

Output of actuator 4 fault (x , y , z)



Output of actuator 4 fault (φ , θ , Ψ)



Conclusion

- Two AFTCS have been designed for the Q-Ball to rectify performance of the system and maintain stability in the presence of actuator partial loss.
- Only actuator faults have been considered, however the system could be extended to deal with sensor and system component faults.
- Implementation on the Real system.

Thank you

Questions!