

**Concordia University**  
**ELEC372 Fundamentals of Control Systems**  
**Homework #7**  
**Professor Amir G. Aghdam**

1. Problem E7.23 from the 8<sup>th</sup>, 9<sup>th</sup>, 10<sup>th</sup>, 11<sup>th</sup>, 12<sup>th</sup>, 13<sup>th</sup> or 14<sup>th</sup> edition of the main textbook.
2. (Automatic Control Systems by Farid Golnaraghi and Benjamin C. Kuo, Eighth Edition, John Wiley & Sons, Inc., 2010) “The characteristic equation of a linear control system is given as follows. Construct the root loci for  $K \geq 0$ .”

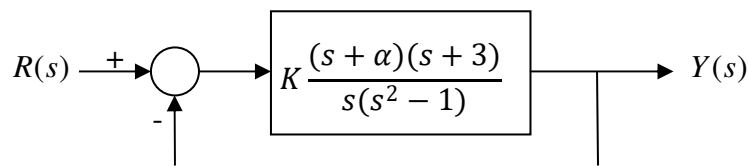
$$s^3 + 2s^2 + 2s + K(s^2 - 1)(s + 2) = 0$$

3. (Automatic Control Systems by Farid Golnaraghi and Benjamin C. Kuo, Eighth Edition, John Wiley & Sons, Inc., 2010) “The forward-path transfer function of a unity-feedback control system is:

$$G(s) = \frac{K(s + 3)}{s(s^2 + 4s + 4)(s + 5)(s + 6)}$$

Construct the root loci for  $K \geq 0$ . Find the value of  $K$  that makes the relative damping ratio of the closed-loop system (measured by the dominant complex characteristic equation roots) equal to 0.707 if such solution exists.”

4. Problem AP7.3 from the 8<sup>th</sup>, 9<sup>th</sup>, 10<sup>th</sup>, 11<sup>th</sup>, 12<sup>th</sup>, 13<sup>th</sup> or 14<sup>th</sup> edition of the main textbook.
5. (Automatic Control Systems by Farid Golnaraghi and Benjamin C. Kuo, Eighth Edition, John Wiley & Sons, Inc., 2010) Consider the following system:



- a) “Construct the root loci for  $K \geq 0$  with  $\alpha = 5$ .”
- b) “Construct the root loci for  $\alpha \geq 0$  with  $K = 10$ .”

6. Problem DP7.5 from the 8<sup>th</sup>, 9<sup>th</sup>, 10<sup>th</sup>, 11<sup>th</sup>, 12<sup>th</sup>, 13<sup>th</sup> or 14<sup>th</sup> edition of the main textbook, but in the 14<sup>th</sup> edition you will need to replace the denominator of the aircraft dynamics with  $(s - 1)(s^2 + 10s + 41)$ .

*Note:* You do not need to predict the step response and compare it to the actual response.