Line intersecting a plane

If the line is not parallel to the plane, it should intersect the plane and the common point is called the piercing point



Edge View Method to see piercing points



Edge View Method to see piercing points



Edge View Method to see piereing points



Edge View Method to see piereing points









Cutting Plane Method to see piercing points



- Line RS is in the since the EV of CP coincides RS
- If the two lines are in a plane and if they are not parallel, they must intersect in the plane

Vertical Cutting Plane N





- Information about visibility is collected in adjacent view
- Point 5 on edge 1-3 is nearer to the observer. So edge 1-3 is visible in view B
- Point 7 on edge 1-3 is nearer to the observer. So edge 1-3 is visible in view A



















Cutting Plane Method







рF











MECHANICAL ENGINEERING GRAPHICS

MECH 211 LECTURE #7

Content of the Lecture

- Polyhedrons and curved surfaces discussion
- Intersection of a plane with a polyhedron visibility
- Intersection of a line with a polyhedron visibility
- Location of a plane perpendicular to a line through a point
- Projection of a point to a plane
- Intersection of a line with a cone
- Intersection of a cylinder with a plane
- Intersection of two prisms
- Intersection of two cylinders

Polyhedrons and curved surfaces

- Surface is 2D. It has area, no volume
 - Surface is generated by moving a line (straight or curved). This is called generatrix
 - Every position of this generatrix is called the element of the surface
- Divided as Ruled and Double Curved Surfaces
 - Ruled Surface Generated by moving straight lines
 - Plane Surfaces Polyhedrons
 - Single Curved surfaces Cylinders or Cones
 - Warped Surfaces adjacent lines are skewed lines (Hyperboloid)
 - Double curved surface generated by moving curved lines (Sphere, Torus, ellipsoid)

Polyhedrons and curved surfaces



Polyhedrons and curved surfaces









abcd is the polyhedron

efg is the plane that intersects the polyhedron abc

CP1 is the cutting plane whose EV coincides with line cd of the polyhedron in the FV. project the points of intersctions on to the TV and find the piercing point 1



abcd is the polyhedron

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CP1 is the cutting plane whose EV coincides with line cd of the polyhedron in the FV. project the points of intersctions on to the TV and find the piercing point 1

CP2 is the cutting plane whose EV coincides with line db of the polyhedron in the FV.

project the points of intersctions on to the TV and find the piercing point 2






abcd is the polyhedron



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In the EV method, draw the EV of the plane



abcd is the polyhedron

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In the EV method, draw the EV of the plane

Project the points abcdefg, parallel to the TL line in the plane



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In the EV method, draw the EV of the plane

Project the points abcdefg, parallel to the TL line in the plane

Complete the polyhedron in that view and the EV of the plane efg. Here you can find the piercing points 1 2 and 3



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In the EV method, draw the EV of the plane

Project the points abcdefg, parallel to the TL line in the plane

Complete the polyhedron in that view and the EV of the plane efg. Here you can find the piercing points 1 2 and 3

Project the piercing points 1, 2, 3 back to the FV from the aux view based on the edges in the polyhedron



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In the EV method, draw the EV of the plane

Project the points abcdefg, parallel to the TL line in the plane

Complete the polyhedron in that view and the EV of the plane efg. Here you can find the piercing points 1 2 and 3

Project the piercing points 1, 2, 3 back to the FV from the aux view based on the edges in the polyhedron

Join the points 1, 2, 3 in propoer order to get the plane of intersection in the FV



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Project the piercing points 1, 2, 3 back to the FV from the aux view based on the edges in the polyhedron

Join the points 1, 2, 3 in propoer order to get the plane of intersection in the FV

Project the points from the FV to the TV and complete the plane in the TV as well







abcd is the polyhedron

ef is the line intersecting the polyhedron abcd. A line must intersect the surface of a polyhedron at two points. An plane containing the given line will help us determine the two points of intersection.



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An plane containing the given line will help us determine the two points of intersection.

To simplify the solution we will use a plane that appears as an edge in one of the views (CP1). Project the points where line intersects the edges of the polyhedron to the TV. This will give the plane of intersection 123



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The line of intersection should be within this plane. So mark the piercing poings g and h where the line intersects the plane 123.

Project the points to the TV. This will give the line of intersection between polygon abcd and line ef.



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ef is the line intersecting the polyhedron abcd. A line must intersect the surface of a polyhedron at two points.

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The line of intersection should be within this plane. So mark the piercing poings g and h where the line intersects the plane 123.

Project the points to the TV. This will give the line of intersection between polygon abcd and line ef.

To see the line in the correct visibility with the points of intersection with the polyhedron marked by crosses turn off layer A10FF and turn on layer A4.

perpendicular to a line through a point



perpendicular to a line through a point



perpendicular to a line through a point



Through the points I and E respectively draw planes that are perpendicular to line AB

I belongs AB, E does not belong AB

Draw lines perpendicular to line ab from point I in both FV and TV

perpendicular to a line through a point



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Draw lines perpendicular to line ab from point I in both FV and TV

Perpendicular line must be a TL line. so to make it true length the projection in the adjacent view needs to be parallel to the folding line.

perpendicular to a line through a point



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Complete the plane based on the points obtained

perpendicular to a line through a point



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Draw lines perpendicular to line ab from point e in both FV and TV

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Projection of a point on a plane is like a shadow of point on the plane due to light shining perpedicular to the plane



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This problem may be conviniently subdivided into two:

- 1. Construction of a perpendicular from a geven point (D)
- to the plane (ABC).
- 2. Location of the point of intersection of the perpendicular with the plane.



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2. Location of the point of intersection of the perpendicular

1. A perpendicular to a plane must be perpendicular to any two lines in that plane.

A right angle is seen as such if one of the lines forming it is a True Length.

The horizontal projection of the perpendicular from D to ABC



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The horizontal projection of the perpendicular from D to ABC is located.

Similarly the frontal projection of the perpendicular is located.











Project line DF onto plane ABC. A line can be located by determining the position of two points of that line. Therefore a projection of the line can be obtained by projecting any two points of that line. (See L05T05 for details on construction of projection of a point on a line).

Projections of points:

- 1. Construction of a perpendicular from given points (D, F) to the plane (ABC).
- 2. Location of the points of intersection of the perpendiculars with the plane.

1. A perpendicular to a plane must be perpendicular to any two lines in that plane.

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The horizontal projections of the perpendiculars from D and F to ABC are located.





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2. The intersection of the perpendiculars from E and F with the plane are located with the help of cutting planes CP1 and CP2 respectively.





Single curved surfaces

Location of a point on a Cone/Cylinder












Front and top views of an Oblique cylinder is seen



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a b is the line that passes through the cylinder and we have to locate the piercing points to find the line of intersection



Front and top views of an Oblique cylinder is seen

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Construct a plane through AB || to the cylinder;



Front and top views of an Oblique cylinder is seen

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Construct a plane through AB || to the cylinder;

Draw the cylinder elements ∈ to the plane.



Front and top views of an Oblique cylinder is seen

a b is the line that passes through the cylinder and we have to locate the piercing points to find the line of intersection

Construct a plane through AB || to the cylinder;

Draw the cylinder elements ∈ to the plane.

Trace P and Q to Front view and mark lines according to visibility



a b is the line that intersects the oblique cone with vertex at V. to find the intersection of the line with the cone, we must find the piercing points and join them.



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Imagine a cutting plane that passes through the line and vertex of the cone; two lines of that plane will intesect AB and the base plane at points 1, 2, 3, 4.



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Determine the position of the lines in the Horizontal view by locating points 1 and 2.



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Find the intersection of the forementioned cutting plane and the base plane of the cone. Points 5 and 6 define the elements of the cone through which the cutting plane passes;



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7 and 8 are the points of intersection between line AB and the cone since they belong both to the cone and the line AB.



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Visibility of the lines are shown in 'this color

Magenta lines show the extreme elements of the cone beyond which we cannot see on the Frontal view.



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project the piercing point of EV of plane on the cone in extreme line 1V and 9V in the FV back to same lines in TV



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project the piercing point of EV of plane on the cone in line 3V and 15V in the FV back to same lines in TV



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project the piercing point of EV of plane on the cone in line 3V and 15V in the FV back to same lines in TV

project the piercing point of EV of plane on the cone in line 7V and 11V in the FV back to same lines in TV



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with available points, draw a curve with irregular curves. the more no. of points, the smooth the curve is.



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Look for Visibility



A vertical prism is intersected by a inclined prism. how will the intersection lines be



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The lateral edge of the veritcal prism is seen as EV in the front view. To see the lateral surface of the inclined prism, an aux view is drawn



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The number of the edges in aux view come from the points of intersection of the vertical prism with the edges of the inclined prism in the top view



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The number of the edges in aux view come from the points of intersection of the vertical prism with the edges of the inclined prism in the top view

Trace the points 7, 8, 9, 10 which show the face of the inclined prism intersecting the edges of the vertical prism, back to the front view.



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Trace the points 7, 8, 9, 10 which show the face of the inclined prism intersecting the edges of the vertical prism, back to the front view.

To be visible in the front view, a point must lie on a visible edge of one prism and on a visible face of the other;

For example pt.1 is visible and pt.4 is hidden. 1, 3, 7, 8 visible



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For example pt.1 is visible and pt.4 is hidden. 1, 3, 7, 8 visible

Connecting the lines in proper sequence is the key to completion. The line should be traced around each prism in all views. like when you see in aux view there is a line from 3,4 to 9, but tin TV there is no line from 4 to 9.

So a line is drawn between 3 and 9 in front view



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Cutting plane method The problem shows one vertical and one inclined prism,

we must find

figures

the intersection



The CP is chosen across one edge RS of the prism

This plane cuts the lower surface at VT, and the other prism at AB and CD

The 4 points WZYX line in both the prisms and also on the cutting plane

These are the points of intersection required



The cutting plane shown in multi view projection. The visibility of the points are seen in the 3D



Total number of cutting planes required is 6 and locate the intersection points from the cutting planes and locate the points in the front view



The points are connected in the front view based on the visibility and sequence


